

SIMPLE STRESS AND STRAIN

The stress in simple tension or compression

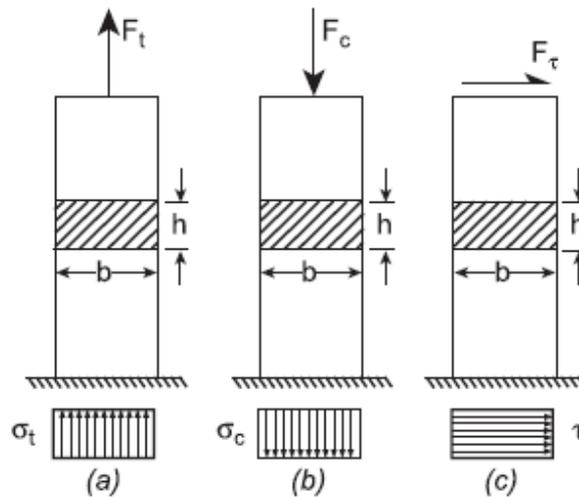
$$\sigma_t = \frac{F_t}{A}; \quad \sigma_c = \frac{F_c}{A}$$

The total elongation of a member of length L

$$\delta = \frac{Fl}{AE}$$

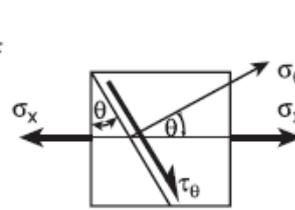
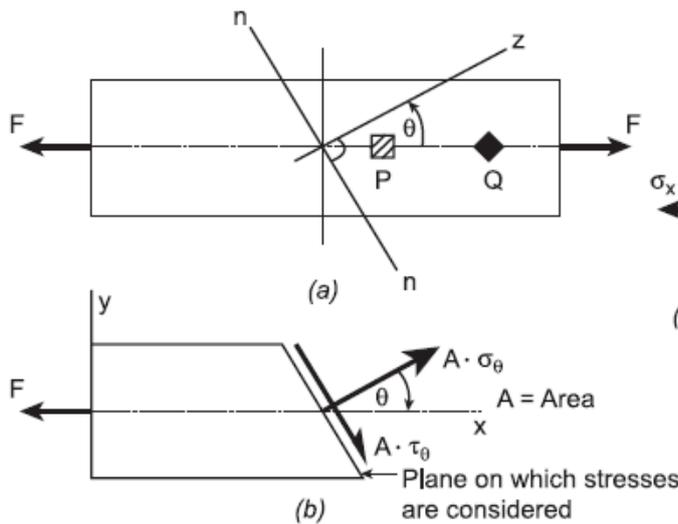
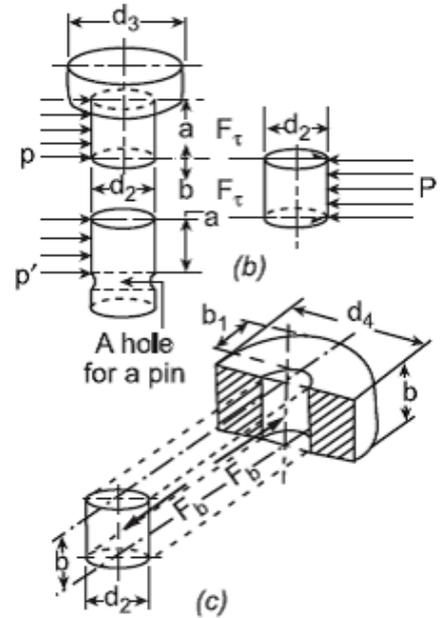
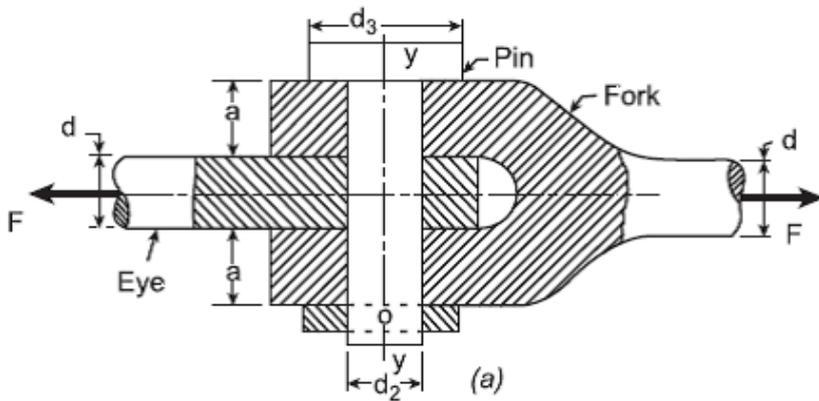
Strain, deformation per unit length

$$\epsilon = \frac{\delta}{l} = \frac{\sigma}{E}$$

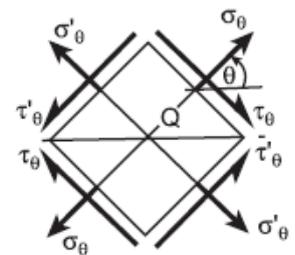


The normal stress on the plane at any angle θ with x

$$\sigma_{\theta} = \sigma_x \cos^2 \theta$$



(c) Stress acting on an element at P



(d) Stress acting on an element at Q



Class: 3rd

Subject: Mechanical Engineering Design

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The shear stress on the plane at any angle θ with x axis

$$\tau_{\theta} = \frac{\sigma_x}{2} \sin 2\theta$$

Principal stresses

$$\sigma_1 = \sigma_x \text{ and } \sigma_2 = 0$$

Angles at which principal stresses act

$$\theta_1 = 0^\circ \text{ and } \theta_2 = 90^\circ$$

Maximum shear stress

$$\tau_{\max} = \frac{\sigma_x}{2}$$

Angles at which maximum shear stresses act

$$\theta_1 = 45^\circ \text{ and } \theta_2 = 135^\circ$$

The normal stress on the plane at an angle

$$\sigma'_{\theta} = \sigma_x \cos^2 \left(\theta + \frac{\pi}{2} \right) = \sigma_x \cos^2 \theta$$

The shear stress on the plane at an angle

$$\tau'_{\theta} = \sigma_x \sin \left(\theta + \frac{\pi}{2} \right) \cos \left(\theta + \frac{\pi}{2} \right) = \frac{1}{2} \sigma_x \sin 2\theta$$

$$\sigma_{\theta} = \sigma'_{\theta} \text{ and } \tau_{\theta} = -\tau'_{\theta}$$

PURE SHEAR

The normal stress on the plane at any angle

$$\sigma_{\theta} = \tau_{xy} \sin 2\theta$$

The shear stress on the plane at any angle

$$\tau_{\theta} = \tau_{xy} \cos 2\theta$$

The principal stress

$$\sigma_1 = \tau_{xy} \text{ and } \sigma_2 = -\tau_{xy}$$

Angles at which principal stresses act

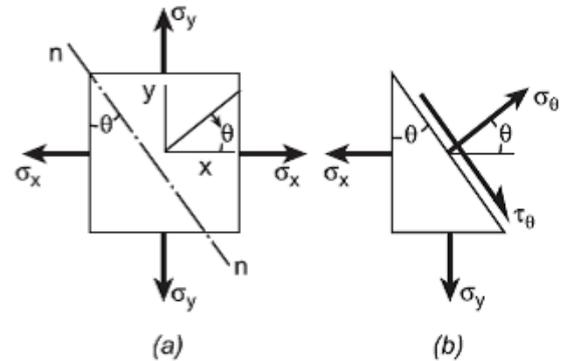
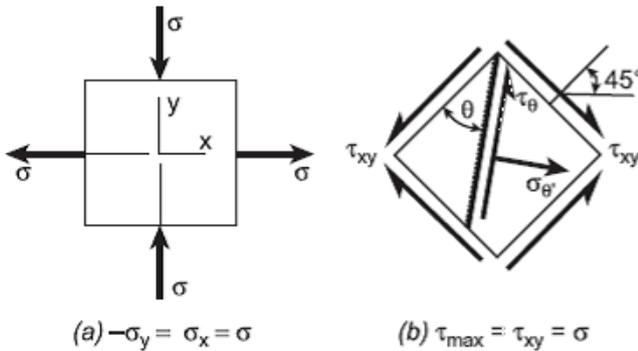
$$\theta_1 = 45^{\circ} \text{ and } \theta_2 = 135^{\circ}$$

Maximum shear stresses

$$\tau_{\max} = \tau_{xy} = \sigma$$

Angles at which maximum shear stress act

$$\theta_1 = 0 \text{ and } \theta_2 = 90^{\circ}$$





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BIAXIAL STRESSES

The normal stress on the plane at any angle

$$\sigma_{\theta} = \frac{\sigma_x + \sigma_y}{2} + \frac{\sigma_x - \sigma_y}{2} \cos 2\theta$$

The shear stress on the plane at any angle

$$\tau_{\theta} = \frac{\sigma_x - \sigma_y}{2} \sin 2\theta$$

The shear stress τ_{θ} at $\theta = 0$

$$\tau_{\theta} = 0$$

The shear stress τ_{θ} at $\theta = 45^{\circ}$

$$\tau_{\max} = (\sigma_x - \sigma_y)/2$$

The normal stress on the plane at any angle

$$\sigma_{\theta} = \frac{\sigma_x + \sigma_y}{2} + \frac{\sigma_x - \sigma_y}{2} \cos 2\theta + \tau_{xy} \sin 2\theta$$

The shear stress in the plane at any angle

$$\tau_{\theta} = \frac{\sigma_x - \sigma_y}{2} \sin 2\theta - \tau_{xy} \cos 2\theta$$

The maximum principal stress

$$\sigma_1 = \frac{\sigma_x + \sigma_y}{2} + \left[\left(\frac{\sigma_x - \sigma_y}{2} \right)^2 + \tau_{xy}^2 \right]^{1/2}$$

The minimum principal stress

$$\sigma_2 = \frac{\sigma_x + \sigma_y}{2} - \left[\left(\frac{\sigma_x - \sigma_y}{2} \right)^2 + \tau_{xy}^2 \right]^{1/2}$$

Angles at which principal stresses act

$$\theta_{1,2} = \frac{1}{2} \arctan \frac{2\tau_{xy}}{\sigma_x - \sigma_y}$$

where θ_1 and θ_2 are 180° apart

Maximum shear stress

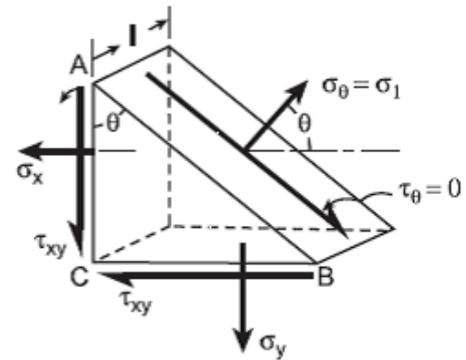
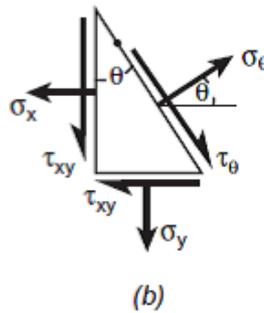
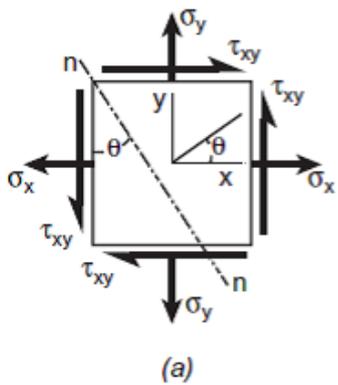
$$\tau_{\max} = \left[\left(\frac{\sigma_x - \sigma_y}{2} \right)^2 + \tau_{xy}^2 \right]^{1/2} = \frac{\sigma_1 - \sigma_2}{2}$$

Angles at which maximum shear stress acts

$$\theta = \frac{1}{2} \arctan \frac{\sigma_x - \sigma_y}{2\tau_{xy}}$$

The equation for the inclination of the principal planes in terms of the principal stress

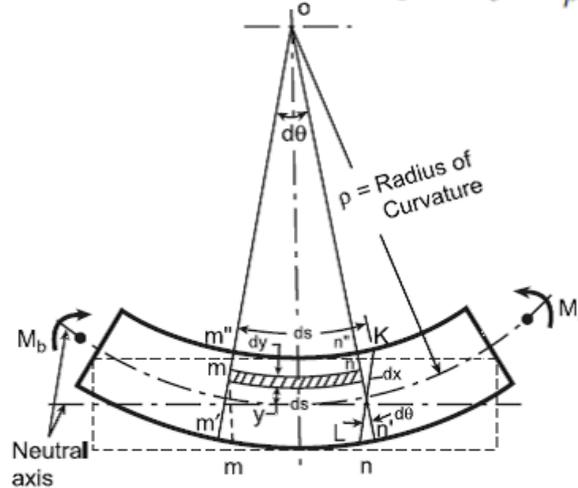
$$\tan \theta = \frac{\sigma_1 - \sigma_x}{\tau_{xy}}$$



BENDING

The general formula for bending

$$\frac{M_b}{I} = \frac{\sigma_b}{c} = \frac{E}{\rho}$$



The maximum values of tensile and compressive bending stresses

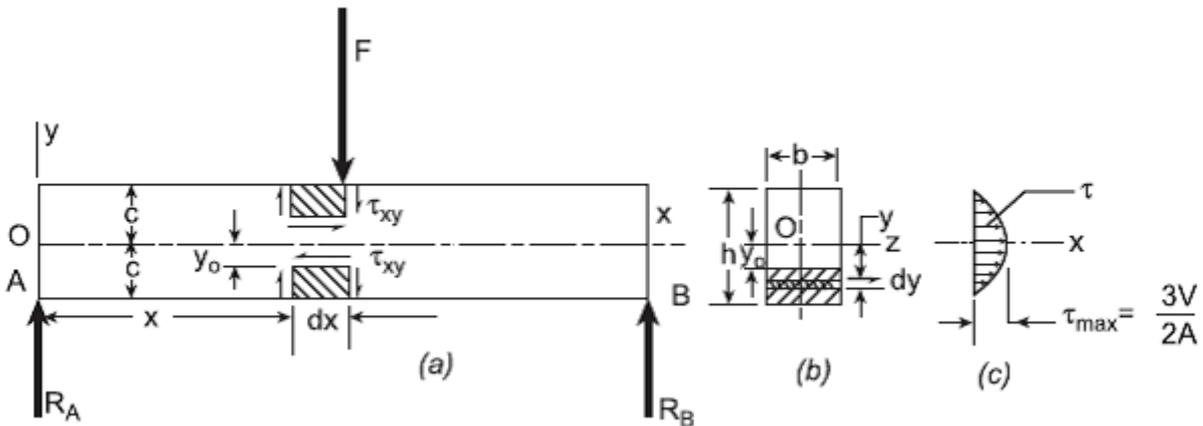
$$\sigma_b = \frac{M_b c}{I}$$

The shear stresses developed in bending of a beam

$$\tau = \frac{V}{Ib} \int_{y_0}^c y dA$$

The shear flow

$$q = \frac{VQ}{I}$$

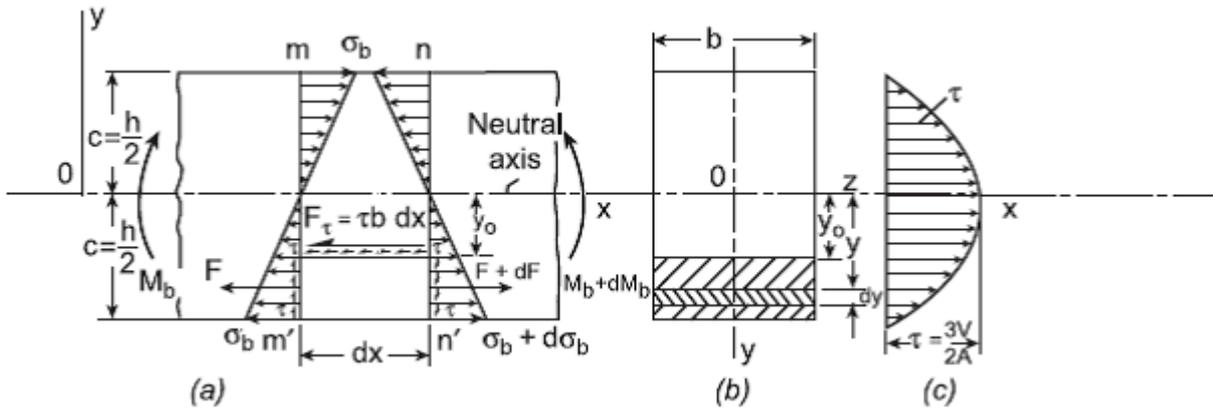


The first moment of the cross-sectional area outside the section at which the shear flow is required

$$Q = \int_{y_b}^c y dA$$

The maximum shear stress for a rectangular section

$$\tau_{\max} = \frac{3V}{2A}$$



For a solid circular section beam, the maximum shear stress

$$\tau_{\max} = \frac{4V}{3A}$$

For a hollow circular section beam, the expression for maximum shear stress

$$\tau_{\max} = \frac{2V}{A}$$

An appropriate expression for τ for structural beams, columns and joists used in structural industries

$$\tau_{\max} = \frac{V}{A_w}$$

where A_w is the area of the web

$$\sigma_{\max} = \frac{F}{A} + \frac{M_b}{Z} \text{ and } \sigma_{\min} = \frac{F}{A} - \frac{M_b}{Z}$$

$$\sigma_z = \pm \frac{F}{A} \pm \frac{M_{bx}e_y}{I_{xx}} \pm \frac{M_{by}e_x}{I_{yy}}$$

$$F_{cr} = \frac{n\pi^2 EA}{(l/k)^2} = \frac{n\pi^2 EI}{l^2}$$