

## CHAPTER FIVE: COOLING TOWERS

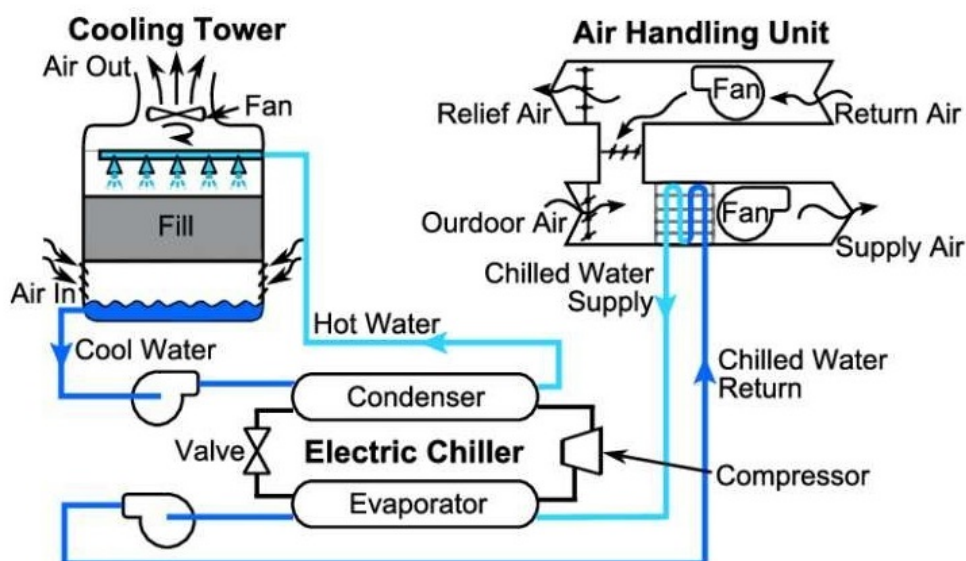
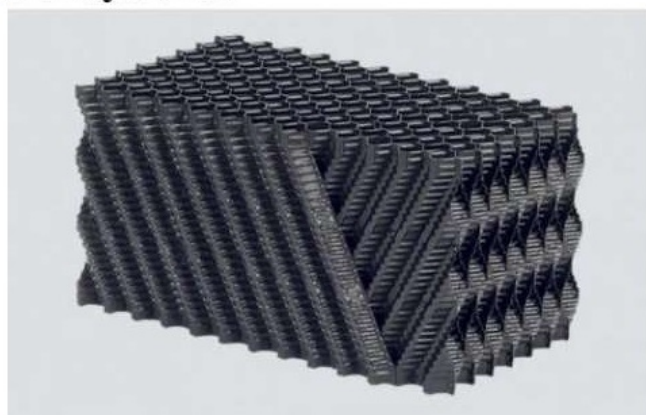
### INTRODUCTION

#### 1. What is cooling tower?

- A cooling tower is a specialized heat exchanger in which air and water are brought into direct contact with each other in order to reduce the water's temperature.
- As this occurs, a small volume of water is evaporated, reducing the temperature of the water being circulated through the tower.

#### 2. Explain the cooling tower role in refrigeration systems?

- In water – cooled chiller in which the condenser is water – cooled type, the refrigerant is hot while the water is cooled. The refrigerant loss its heat to the water.
- As soon as the water absorb this heat, its temperature will rise. So the water will go into a cooling tower and enters the tower from the top and flow through the fills while the air will be moved from bottom side into the top of the tower to make direct exchange between the hot water and cold air in which the water will lose its heat to the air which lead the water to be cooled and enters the water – cooled condenser again and the cycle will repeated in this manner.

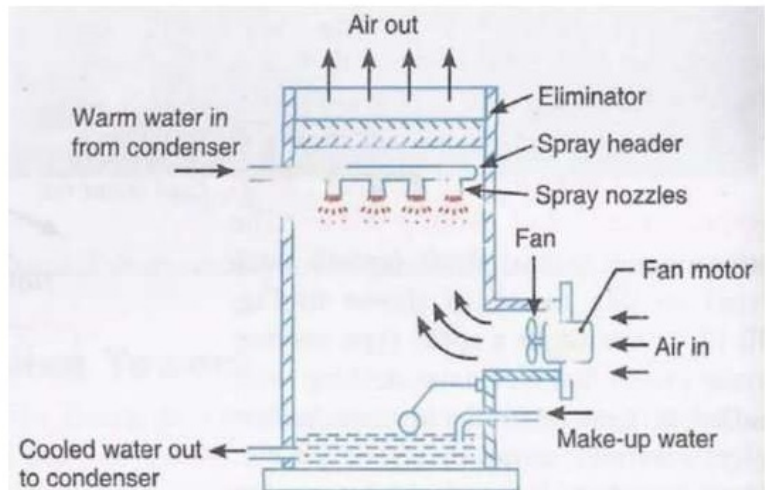
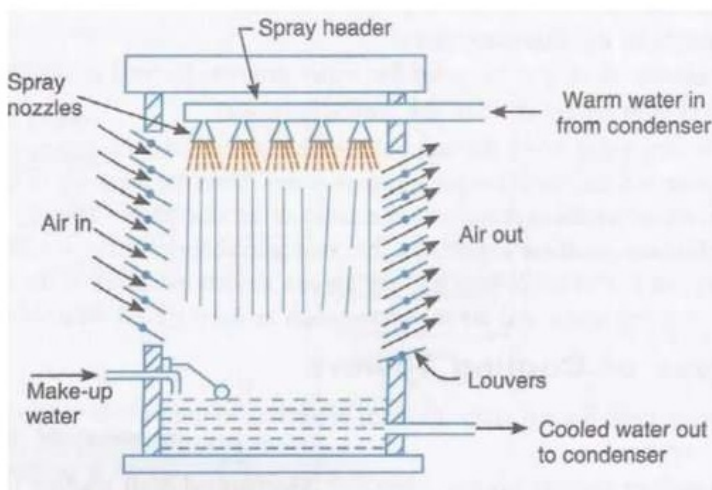


### 3. Types of cooling tower

The cooling towers are mainly divided, according to their method of air circulation, into the following two groups :

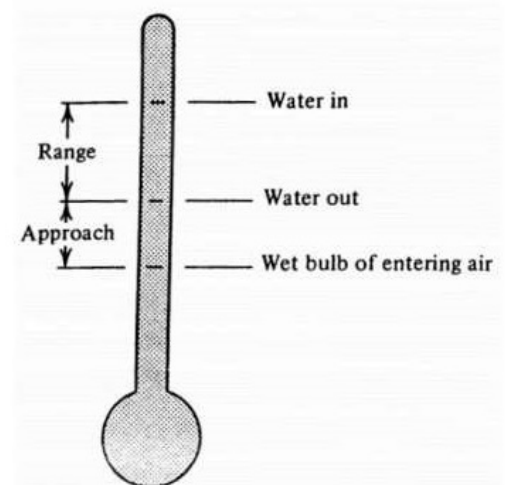
1. Natural draft cooling towers, and
2. Mechanical draft cooling towers.

In *natural draft cooling towers*, the air circulates through the tower by natural convection whereas in *mechanical draft cooling towers*, the air is forced through the tower by means of fans



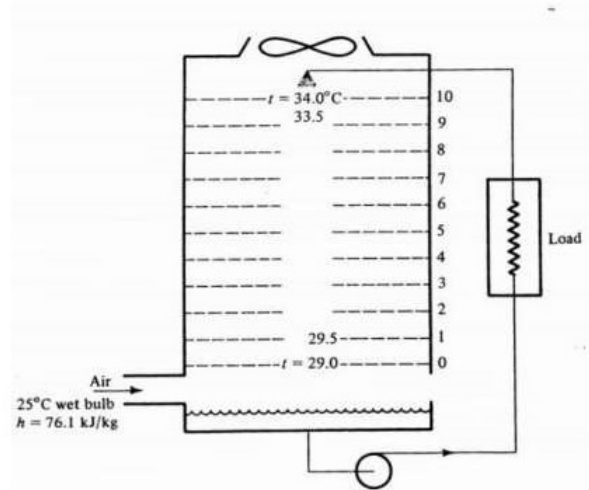
### 4. Range and Approach in Cooling Towers

- The **range** is the reduction in temperature of the water through the cooling tower.
- The **approach** is the difference between the wet-bulb temperature of the entering air and temperature of the leaving water.





## Applied Thermodynamics to Cooling Towers



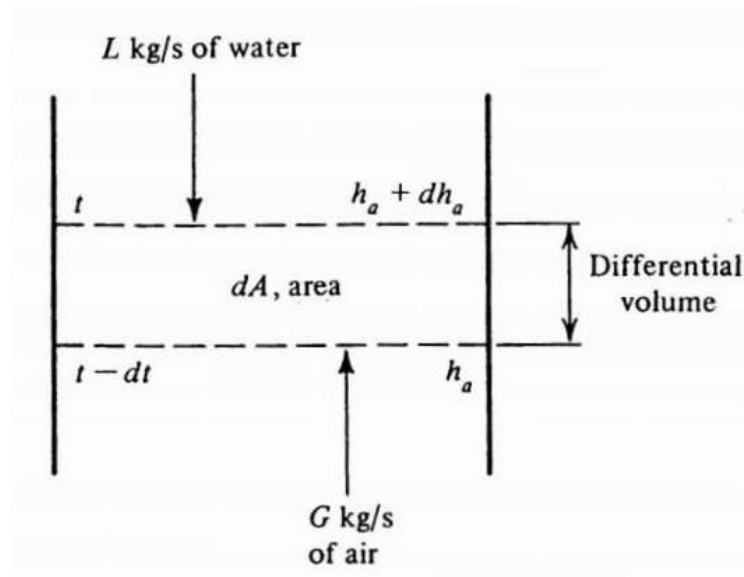
**19-3 Analysis of a counterflow cooling tower** One design of cooling tower is the counterflow type, in which air passes upward through a falling spray of water. Figure 19-3 shows a differential volume of a counterflow cooling tower with  $L$  kg/s of water entering from the top and  $G$  kg/s of air entering from the bottom. For simplicity, the small quantity of water which evaporates is neglected, so that both  $L$  and  $G$  remain constant throughout the tower.

Water enters the section at a temperature  $t^{\circ}\text{C}$  and leaves at a slightly lower temperature  $t - dt$ . Air enters the section with an enthalpy of  $h_a$  kJ per kilogram of dry air and leaves with an enthalpy of  $h_a + dh_a$ . The total area of the wetted surface  $dA$  includes the surface area of the drops of water as well as the wetted slats or other fill material.

The rate of heat removed from the water  $dq$  is equal to the rate gained by the air:

$$dq = G dh_a = L(4.19 \text{ kJ/kg} \cdot \text{K}) dt \quad \text{kW} \quad (19-1)$$

$$G(h_{a,1} - h_{a,0}) = L * 4.19 * \Delta t$$



From the principles of enthalpy potential in Sec. 3-15 another expression for  $dq$  is

$$dq = \frac{h_c dA}{c_{pm}} (h_i - h_a) \quad (19-2)$$

where  $h_c$  = convection coefficient,  $\text{kW/m}^2 \cdot \text{K}$

$h_i$  = enthalpy of saturated air at the water temperature,  $\text{kJ}/(\text{kg dry air})$

$h_a$  = enthalpy of air,  $\text{kJ}/(\text{kg dry air})$

$c_{pm}$  = specific heat of moist air,  $\text{kJ}/\text{kg} \cdot \text{K}$

**19-4 Stepwise integration** To find the rate of heat transferred by the entire cooling tower, Eq. (19-2) must be integrated. Both  $h_i$  and  $h_a$  vary with respect to the variable of integration  $A$ . Combining Eqs. (19-1) and (19-2), rearranging, and integrating gives

$$4.19 L \int_{t_{\text{out}}}^{t_{\text{in}}} \frac{dt}{h_i - h_a} = \int_0^A \frac{h_c dA}{c_{pm}} = \frac{h_c A}{c_{pm}} \quad (19-3)$$

where  $t_{\text{in}}$  and  $t_{\text{out}}$  are the water temperatures entering and leaving the tower, respectively.

$$\frac{h_c A}{c_{pm}} = 4.19 L \Delta t \sum \frac{1}{(h_i - h_a)_m} \quad (19-4)$$

### Cooling Tower

Example:

A counter flow cooling tower operates with a water flow rate of  $18.8 \text{ kg/s}$  and an air flow rate of  $15.6 \text{ kg/s}$ , when the wet bulb temperature of entering air is  $25^\circ\text{C}$  ( $h_a = 76 \text{ kJ/kg}$ ) and entering water temperature is  $34^\circ\text{C}$ , the leaving water temperature is  $28^\circ\text{C}$ . Calculate  $(h_c A / G_m)$  for three sections. Using Stepwise integration with  $2^\circ\text{C}$  increments change in water temperature

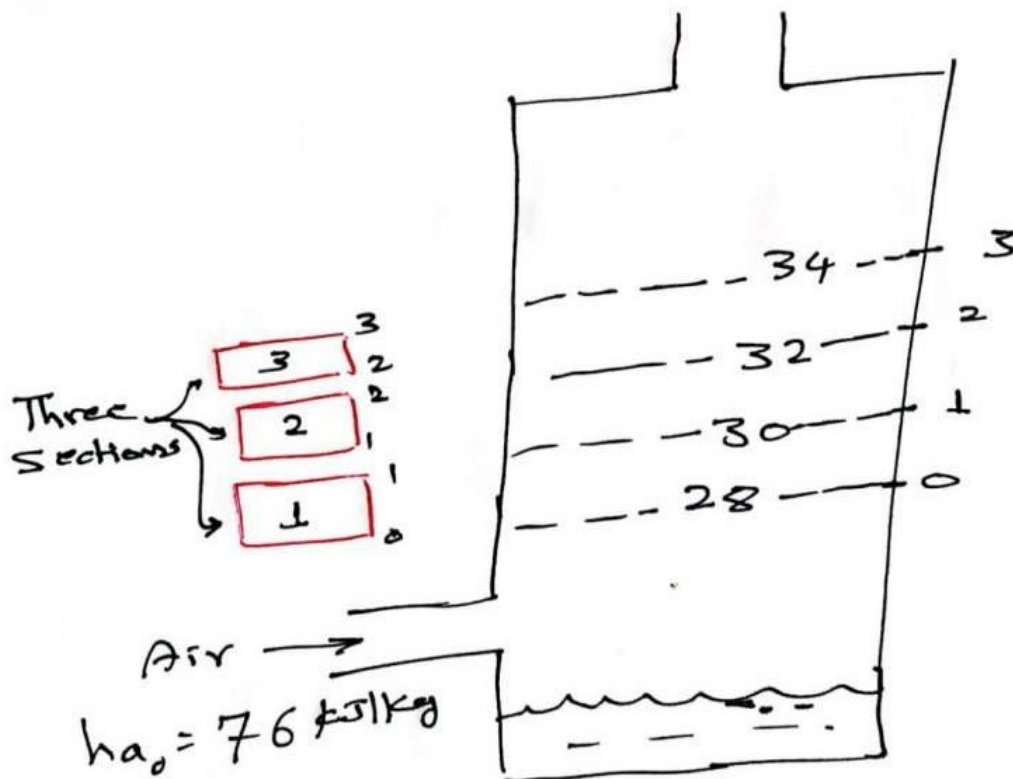
| $T [^\circ\text{C}]$                             | 28   | 29   | 30   | 31    | 32    | 33    | 34    | 35    | 36    |
|--|------|------|------|-------|-------|-------|-------|-------|-------|
| $h_i \left[ \frac{\text{kJ}}{\text{kg}} \right]$ | 89.9 | 94.8 | 99.9 | 105.3 | 110.9 | 116.8 | 122.9 | 129.4 | 136.1 |

Sol:  $L = 18.8 \text{ kg/s}$  ;  $G = 15.6 \text{ kg/s}$   
 $t_{w, \text{in}} = 34^\circ\text{C}$  ;  $h_{a,0} = 76 \text{ kJ/kg}$   
 $t_{w, \text{out}} = 28^\circ\text{C}$



$$\Delta t_{\text{water}} = \frac{t_{w,\text{in}} - t_{w,\text{out}}}{\text{number of sections}}$$

$$\Rightarrow \text{Number of Sections} = \frac{34 - 28}{2} = \frac{6}{2} = 3$$



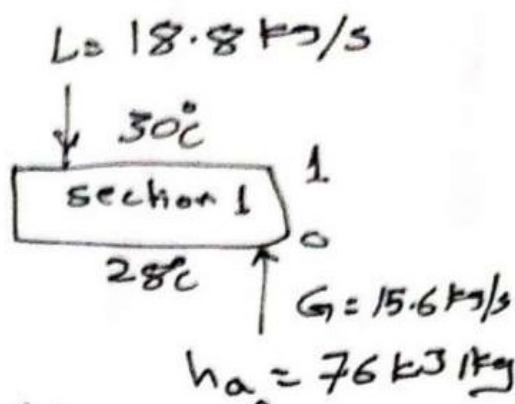
Schematic Diagram of the Computation Domain



Section 1

$$h_{a1} = ?$$

$$h_{a0} = 76 \text{ kJ/kg}$$



$$\therefore G(h_{a1} - h_{a0}) = L \times 4.19 \times \Delta t$$

$$h_{a1} - h_{a0} = \left(\frac{L}{G}\right)(4.19)(\Delta t)$$

$$\therefore h_{a1} = \left(\frac{L}{G}\right)(4.19)(\Delta t) + h_{a0}$$

$$= \left(\frac{18.8}{15.6}\right)(4.19)(2) + 76$$

$$\therefore h_{a1} = 86.09897436 \text{ kJ/kg}$$

$$h_{am} = \frac{h_{a1} + h_{a0}}{2} = \frac{86.0989 + 76}{2}$$

$$\Rightarrow h_{am} = 81.04948718 \text{ kJ/kg}$$

$$t_{wm} = \frac{30 + 28}{2} = 29^\circ\text{C}$$

From the given table in the example; we find: at  $t_{wm} = 29^\circ\text{C} \rightarrow h_{i,m} = 94.8 \text{ kJ/kg}$

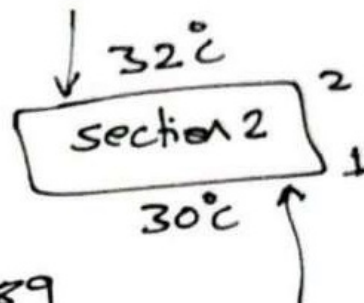
$$\therefore \frac{h_c A}{C_{pm}} = 4.19 \times L \times \Delta t_w \times \frac{1}{(h_i - h_a)_m}$$

$$\frac{h_c A}{C_{pm}})_1 = 4.19 \times 18.8 \times 2 \times \frac{1}{948 - 81.0494}$$

$$\frac{h_c A}{C_{pm}})_1 = 11.4572 \text{ kW/(KJ/kg of enthalpy diff)}$$

Similarly; For Section 2:

$$L = 18.8 \text{ kg/s}$$



$$h_{a2} = \frac{L}{G} \times 4.19 \times \Delta t + h_{a1}$$

$$= \frac{18.8}{15.6} \times 4.19 \times 2 + 860989$$

$$G = 15.6 \text{ kg/s}$$

$$h_{a1} = 860989 \frac{\text{KJ}}{\text{kg}}$$

$$\therefore h_{a2} = 96.1978 \text{ KJ/kg}$$

$$h_{am} = \frac{h_{a2} + h_{a1}}{2} = \frac{96.1978 + 860989}{2}$$

$$\Rightarrow h_{am} = 91.1483 \text{ KJ/kg}$$

$$t_{wm} = \frac{32 + 30}{2} = 31^\circ\text{C}$$

$$\text{From Table 2 } t_{wm} = 31^\circ\text{C} \rightarrow h_m = 105.3 \text{ KJ/kg}$$

$$\therefore \frac{h_c A}{C_{pm}})_2 = 4.19 \times 18.8 \times 2 \times \frac{1}{105.3 - 91.1483}$$

$$\Rightarrow \frac{h_c A}{C_{pm}})_2 = 11.13258 \text{ kW/(KJ/kg)}$$

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Finally; For Section 3:

$$h_{a3} = \frac{L}{G} * 4.19 * \Delta t + h_{a2}$$

$$h_{a3} = \frac{18.8}{15.6} * 4.19 * 2 + 96.1978$$

$$\Rightarrow h_{a3} = 106.2967 \text{ kJ/kg}$$

$$h_{am} = \frac{h_{a3} + h_{a2}}{2} = \frac{106.2967 + 96.1978}{2}$$

$$\Rightarrow h_{am} = 101.2472 \text{ kJ/kg}$$

$$\text{Again; } t_{wm} = \frac{32 + 34}{2} = 33^\circ\text{C}$$

From Table at  $t_{wm} = 33^\circ\text{C}$ :

$$h_{i|m} = 116.8 \text{ kJ/kg}$$

$$\therefore \left. \frac{h_c A}{C_{pm}} \right|_3 = 4.19 * 18.8 * 2 * \frac{1}{116.8 - 101.2472}$$

$$= 10.1296 \text{ kW/(kJ/kg)}$$

$$\therefore \frac{h_c A}{C_{pm}} = \left. \frac{h_c A}{C_{pm}} \right|_1 + \left. \frac{h_c A}{C_{pm}} \right|_2 + \left. \frac{h_c A}{C_{pm}} \right|_3$$

$$= 11.4572 + 11.1325 + 10.1296$$

$$= 32.7193 \text{ kW/(kJ/kg)}$$