

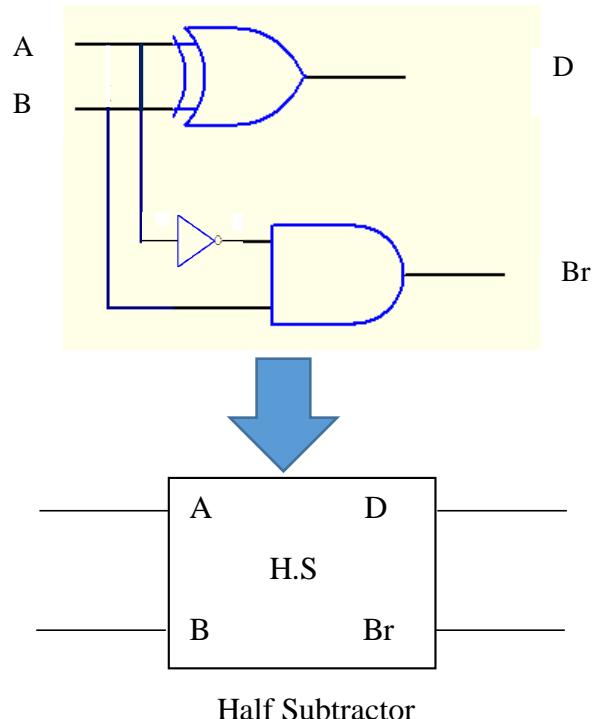
Half Subtractor:

H.S is used to subtract two bit numbers.

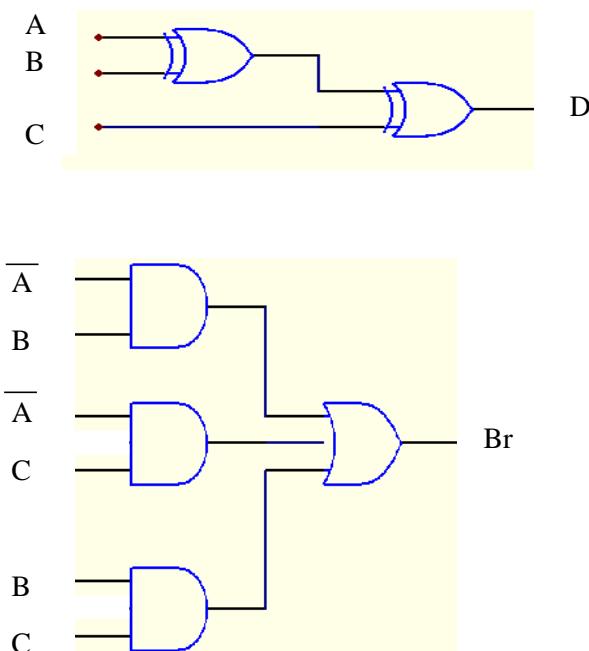
A	B	D	Br
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

$$D = A \oplus B$$

$$Br = \overline{AB}$$



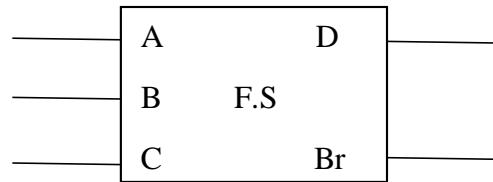
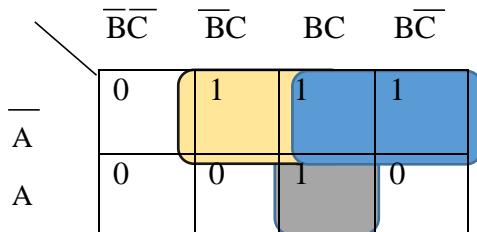
Full subtractor: Full Subtractor is used to subtract three bits.



A	B	C	D	Br
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

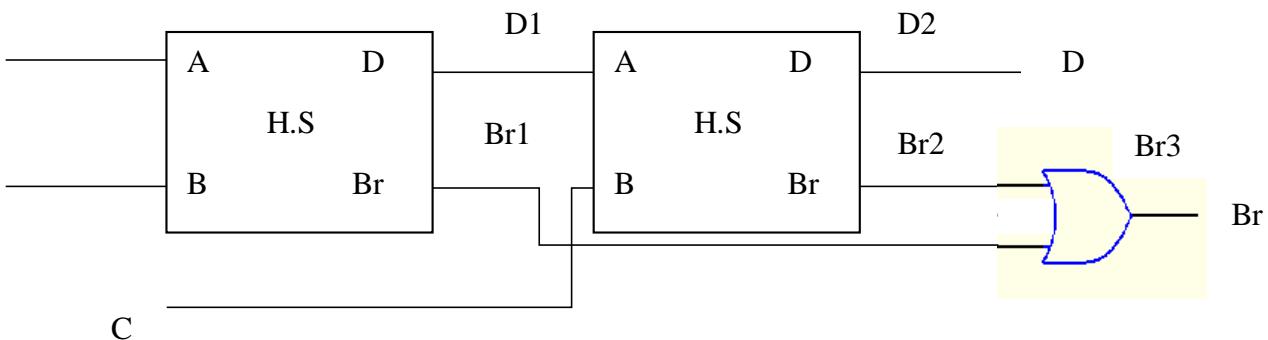
$$D = A \oplus B \oplus C$$

$$Br = \overline{AB} + \overline{AC} + BC$$



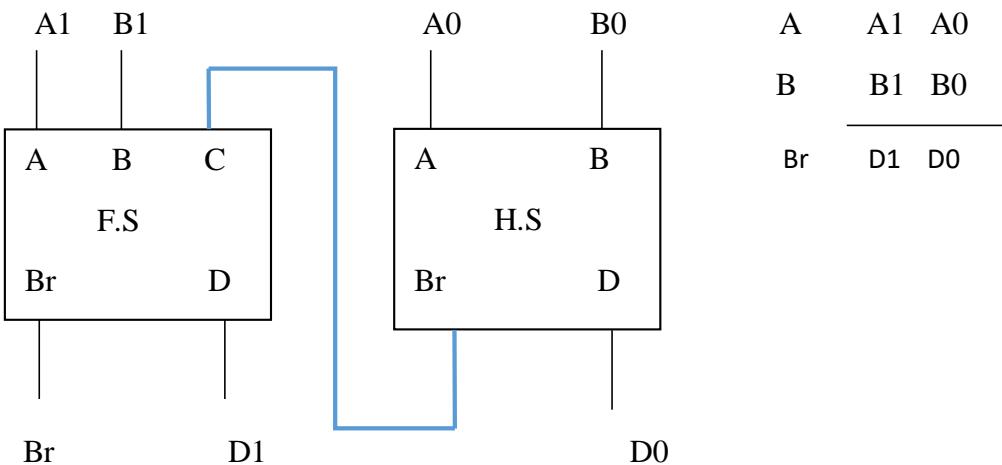
Full Subtractor

Ex1: Designing F.S using H.S's and OR gate



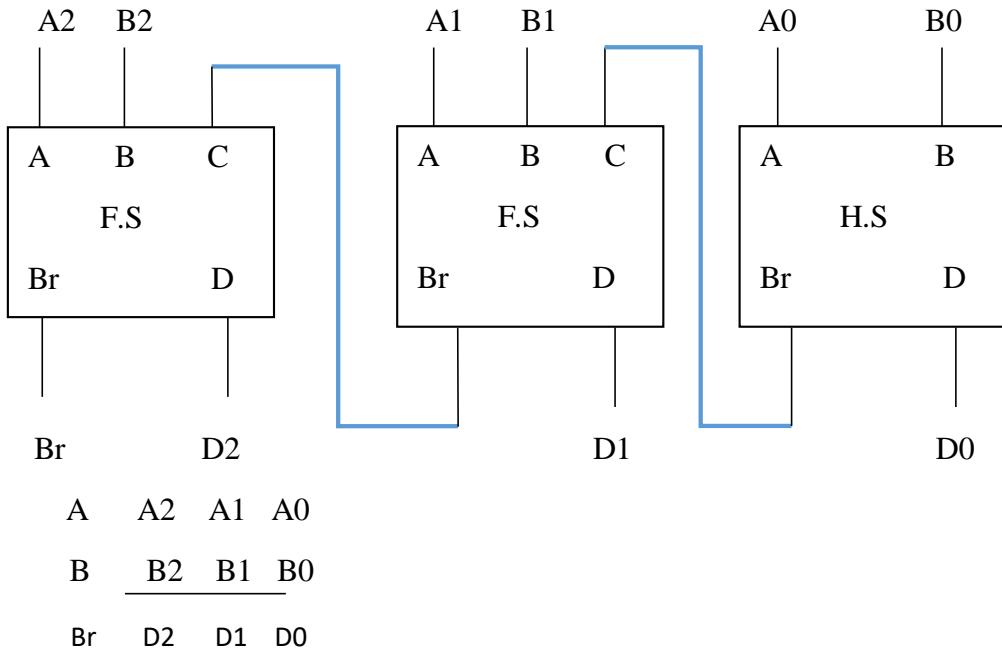
Ex2:

Design a logic circuit to subtract two 2-bit numbers using subtractions:



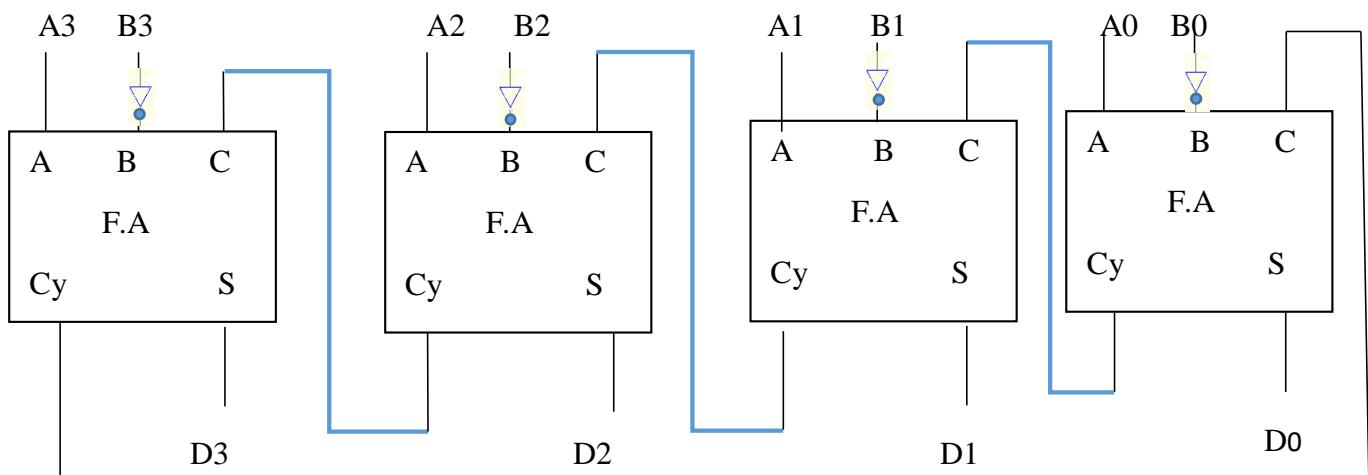
Ex3:

Design a logic circuit to subtract two 3-bit numbers using subtractors:



Ex4:

Design a logic circuit to subtract two 4-bit numbers using adders with 1's complement:



$$\begin{array}{r}
 \text{+} \quad \begin{array}{ccccc} A & A_3 & A_2 & A_1 & A_0 \\ B & \overline{B_3} & \overline{B_2} & \overline{B_1} & \overline{B_0} \\ \hline Cy & D_3 & D_2 & D_1 & D_0 \end{array} \\
 \leftarrow \\
 \begin{array}{ccccc} A & A_3 & A_2 & A_1 & A_0 \\ B & \overline{B_3} & \overline{B_2} & \overline{B_1} & \overline{B_0} \\ \hline Br & D_3 & D_2 & D_1 & D_0 \end{array}
 \end{array}$$

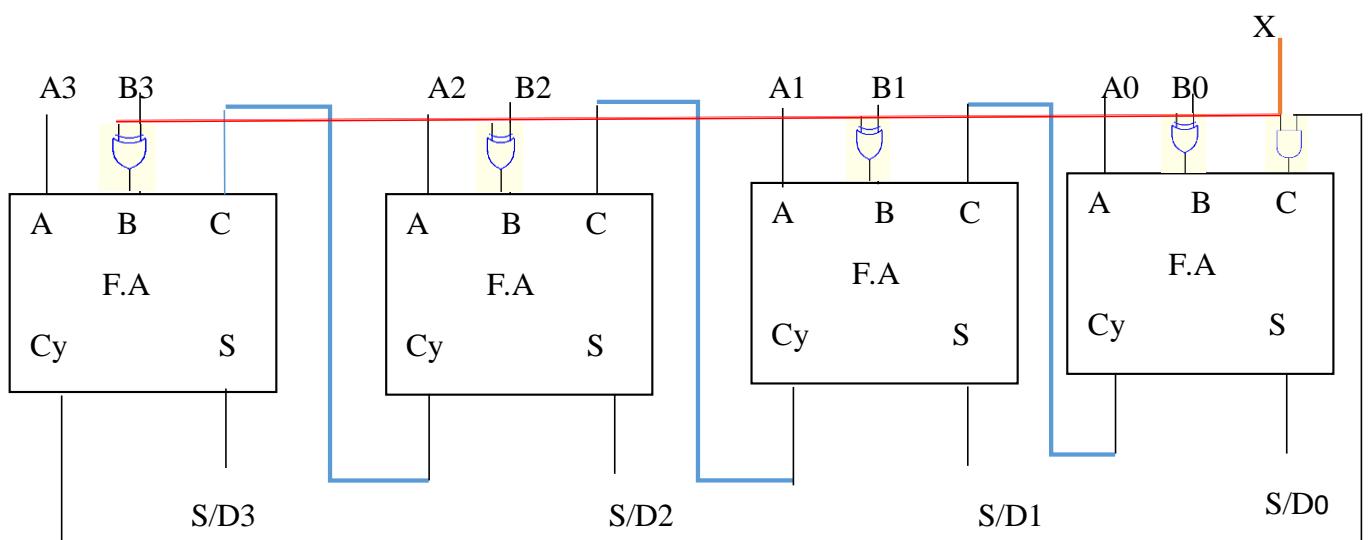
Ex5:

Design a logic circuit to Add/subtract two 4-bit numbers using Adders and logic gates:

Subtraction	Addition
$ \begin{array}{r} \text{+} \quad \begin{array}{ccccc} A & A_3 & A_2 & A_1 & A_0 \\ B & \overline{B_3} & \overline{B_2} & \overline{B_1} & \overline{B_0} \\ \hline Cy & D_3 & D_2 & D_1 & D_0 \end{array} \\ \leftarrow \\ \begin{array}{ccccc} A & A_3 & A_2 & A_1 & A_0 \\ B & \overline{B_3} & \overline{B_2} & \overline{B_1} & \overline{B_0} \\ \hline Cy & S_3 & S_2 & S_1 & S_0 \end{array} \end{array} $	
$ \begin{array}{r} \text{+} \quad \begin{array}{ccccc} A & A_3 & A_2 & A_1 & A_0 \\ B & \overline{B_3} & \overline{B_2} & \overline{B_1} & \overline{B_0} \\ \hline Cy & D_3 & D_2 & D_1 & D_0 \end{array} \\ \leftarrow \\ \begin{array}{ccccc} A & A_3 & A_2 & A_1 & A_0 \\ B & \overline{B_3} & \overline{B_2} & \overline{B_1} & \overline{B_0} \\ \hline Cy & S_3 & S_2 & S_1 & S_0 \end{array} \end{array} $	Addition Subtraction

X = 0 Addition A + B

X = 1 Subtraction A + \overline{B} (1's complement Subtraction)



Ex6:

Convert a subtraction of 4-bit numbers to comparator:

