

Transport Phenomena

Sheet No#2 Modeling

Q¹/ Develop an equation for the distance traveled by a freely falling body in time T assuming the distance depends upon the weight of the body, the acceleration of gravity, and the time.

Q²/ The Reynolds number (Re) is a function of density, viscosity, and velocity of a fluid and a characteristic length. Establish the Reynolds number relation by dimensional analysis.

Q³/ Determine the dynamic pressure exerted by a flowing incompressible fluid on an immersed object, assuming the pressure is a function of the density and the velocity.

Q⁴/ For an ideal liquid, express the flow Q through an orifice in terms of the density of the liquid, the diameter of the orifice, and the pressure difference.

Q⁵/ Assuming the drag force exerted by a flowing fluid on a body is a function of the density, viscosity, and velocity of the fluid and a characteristic length of the body, develop a general equation.

Table of dimension of several Quantities

		Solution:		
		(a)	(b)	
	Quantity	Symbol	<i>F-L-T</i>	<i>M-L-T</i>
(a)	Area A in ft^2 or m^2	A	L^2	L^2
(b)	Volume v in ft^3 or m^3	v	L^3	L^3
(c)	Velocity V in ft/sec or m/s	V	$L T^{-1}$	$L T^{-1}$
(d)	Acceleration a or g in ft/sec^2 or m/s^2	a, g	$L T^{-2}$	$L T^{-2}$
(e)	Angular velocity ω in rad/sec	ω	T^{-1}	T^{-1}
(f)	Force F in lb or N	F	F	$M L T^{-2}$
(g)	Mass M in slugs or kg	M	$F T^2 L^{-1}$	M
(h)	Specific weight γ in lb/ft^3 or N/m^3	γ	$F L^{-3}$	$M L^{-2} T^{-2}$
(i)	Density ρ in slugs/ft^3 or kg/m^3	ρ	$F T^2 L^{-4}$	$M L^{-3}$
(j)	Pressure p in lb/ft^2 or Pa	p	$F L^{-2}$	$M L^{-1} T^{-2}$
(k)	Absolute viscosity μ in $\text{lb}\cdot\text{sec}/\text{ft}^2$ or $\text{N}\cdot\text{s}/\text{m}^2$	μ	$F T L^{-2}$	$M L^{-1} T^{-1}$
(l)	Kinematic viscosity ν in ft^2/sec or m^2/s	ν	$L^2 T^{-1}$	$L^2 T^{-1}$
(m)	Modulus of elasticity E in lb/ft^2 or Pa	E	$F L^{-2}$	$M L^{-1} T^{-2}$
(n)	Power P in $\text{ft}\cdot\text{lb}/\text{sec}$ or $\text{N}\cdot\text{m}/\text{s}$	P	$F L T^{-1}$	$M L^2 T^{-3}$
(o)	Torque T in $\text{ft}\cdot\text{lb}$ or $\text{N}\cdot\text{m}$	T	$F L$	$M L^2 T^{-2}$
(p)	Rate of flow Q in ft^3/sec or m^3/s	Q	$L^3 T^{-1}$	$L^3 T^{-1}$
(q)	Shearing stress τ in lb/ft^2 or Pa	τ	$F L^{-2}$	$M L^{-1} T^{-2}$
(r)	Surface tension σ in lb/ft or N/m	σ	$F L^{-1}$	$M T^{-2}$
(s)	Weight W in lb or N	W	F	$M L T^{-2}$
(t)	Weight rate of flow W in lb/sec or N/s	W	$F T^{-1}$	$M L T^{-3}$