



Theory of structure

Stability and Determinacy of Structures

L2

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Stability and Determinacy of Frames

1- Open frames

$r < C+3$, unstable

$r = C+3$, determinate if stable

$r > C+3$, indeterminate if stable

Ex1:- Find the stability and determinacy of frame below

$$C_1 = m-1, C_1 = 2-1 = 1$$

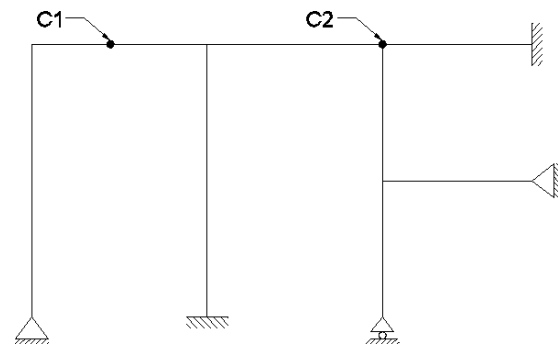
$$C_2 = m-1, C_2 = 3-1 = 2$$

$$C = C_1 + C_2, C = 3$$

$$r = 11$$

$$C+3 = 6$$

$r > C+3$, the frame is stable & indeterminate 5th degree.

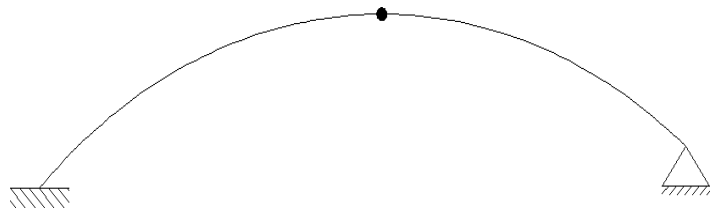


Ex2:-

$$r = 5$$

$$C = 2 - 1 = 1$$

$r > C + 3$, the frame is stable & indeterminate 1st degree.



Ex3:-

$$C_1 = m - 1, C_1 = 4 - 1 = 3$$

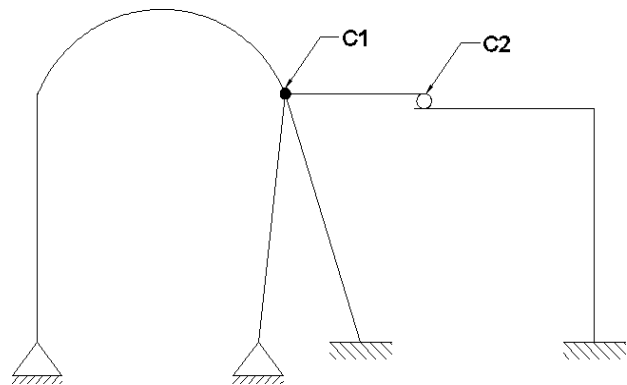
$$C_2 = 2$$

$$C = C_1 + C_2, C = 5$$

$$r = 10$$

$$C + 3 = 8$$

$r > C + 3$, the frame is stable & indeterminate 2nd degree.

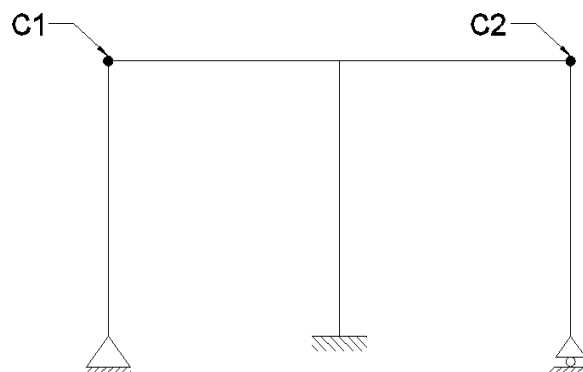


Ex4:-

$$r = 6$$

$$C = 2$$

$$r > C + 3$$



The frame is unstable because of internal geometric instability

2- Closed Frames:-

 $3b+r < 3j+c$, unstable

 $3b+r = 3j+c$, determinate if stable

 $3b+r > 3j+c$, indeterminate if stable

Where,

 $3b+r$ = unknown

 $3j+c$ = equations

b = No. of members

r = No. of reactions

j = No. of joints

Ex1:-

$b = 10$

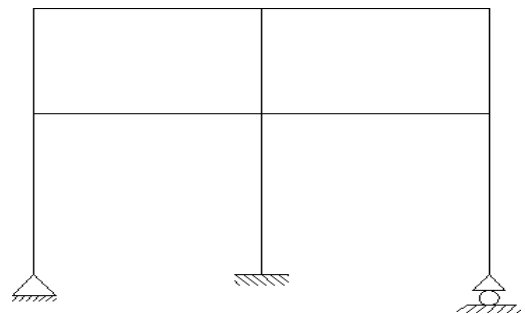
$r = 6$

$j = 9$

$3b+r = 36$

$3j+c = 27$

$3b+r > 3j+c$, stable & indeterminate 9th degree



Ex2:-

$b = 10$

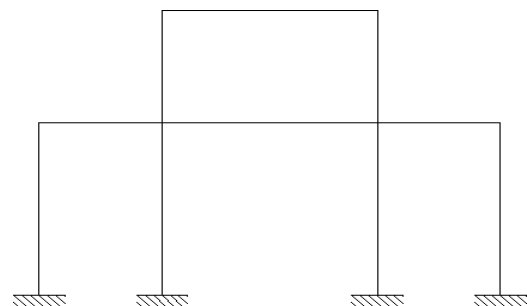
$r = 12$

$j = 10$

$3b+r = 42$

$3j+c = 30$

$3b+r > 3j+c$, stable & indeterminate 12th degree



Ex3:-

$$b = 4$$

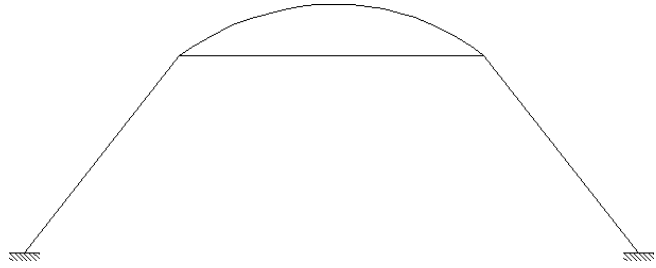
$$r = 6$$

$$j = 4$$

$$c = 0$$

$$3b+r = 18$$

$$3j+c = 12$$

 $3b+r > 3j+c$, stable & indeterminate 6th degree


Ex4:-

$$b = 9$$

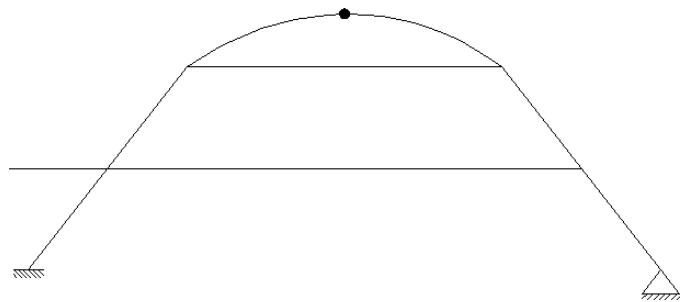
$$r = 5$$

$$j = 7$$

$$c = m-1 \Rightarrow c = 1$$

$$3b+r = 32$$

$$3j+c = 22$$

 $3b+r > 3j+c$, stable & indeterminate 10th degree


Ex5:-

$$b = 10$$

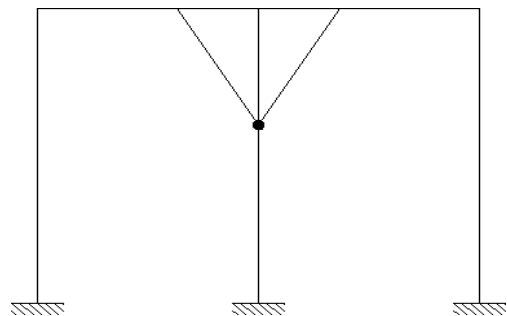
$$r = 9$$

$$j = 9$$

$$c = m-1 \Rightarrow c = 4-1 \Rightarrow c = 3$$

$$3b+r = 39$$

$$3j+c = 30$$

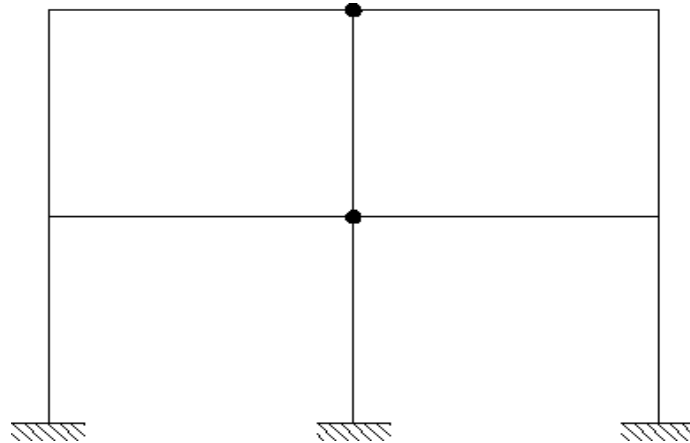
 $3b+r > 3j+c$, stable & indeterminate 9th degree


ملاحظة:- اذا جاء ال internal hinge في بداية او ن هاية الضلع فيحسب منه (c & j) اما

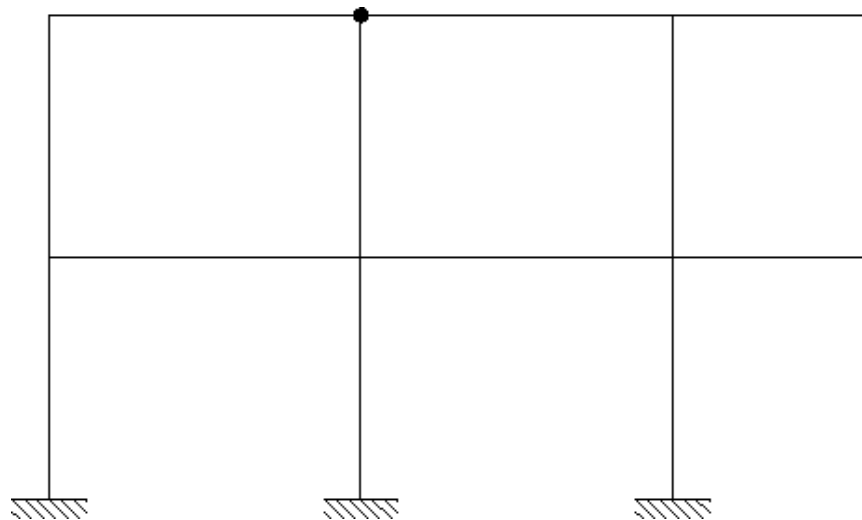
اذا جاء في داخل الضلع فيحسب منه c فقط

Home work:

H.W1: Find the stability and determinacy of frame below



H.W2: Find the stability and determinacy of frame below



Stability and Determinacy of Composite Structure

Unknowns	Equations
1- Each truss member give one unknown	1- each member carry moment give (3 equations)
2- reactions	2- each joint connect truss members only give (2 equations)
3- each joint connect member carry moment give unknown in these equation ($2*(m-1)$)	

Ex1:- Find the stability and determinacy of composite structure as shown below.

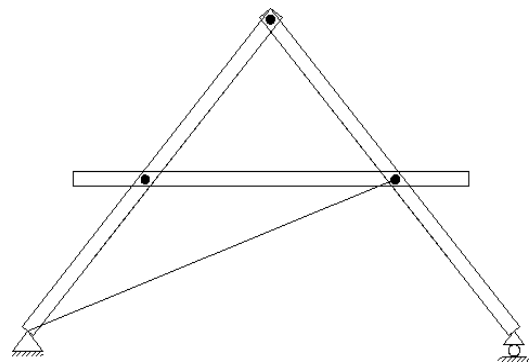
Solution:

Equations

$$(3*3) + 0 = 9$$

Unknowns

$$1 + 3 + (3*(2(2-1))) = 10$$



Unknowns > Equations, Stable & indeterminate 1st degree

Ex2:- Find the stability and determinacy of composite structure as shown below.

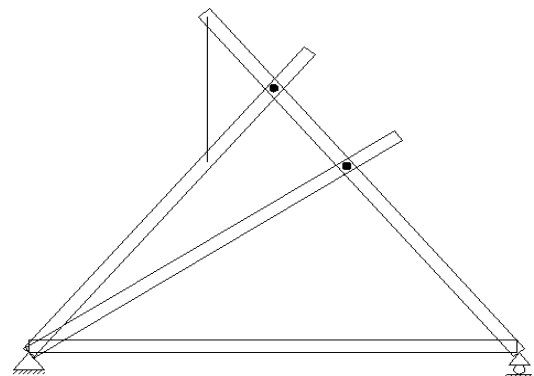
Solution:

Equations

$$(4*3) + 0 = 12$$

Unknowns

$$1 + 3 + (3*(2(2-1))) + (2(3-1)) = 14$$



Unknowns > Equations, Stable & indeterminate 2nd degree

Ex3:- Find the stability and determinacy of composite structure as shown below.

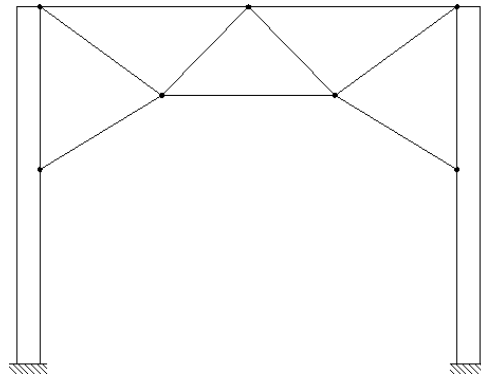
Solution:

Equations

$$(2*3) + (3*2) = 12$$

Unknowns

$$9+6+0 = 15$$



Unknowns > Equations, Stable & indeterminate 2nd degree

Ex4:- Find the stability and determinacy of composite structure as shown below.

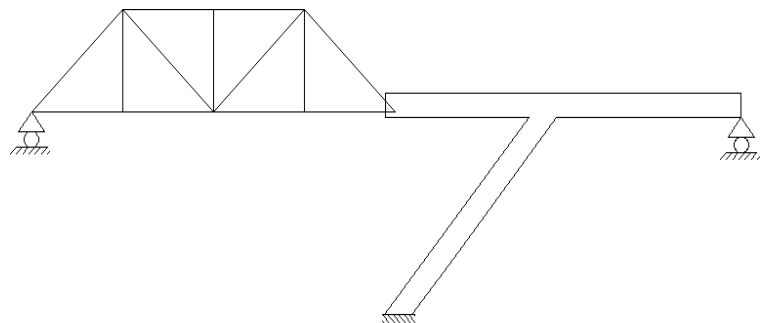
Solution:

Equations

$$(1*3) + (7*2) = 17$$

Unknowns

$$13+5+0 = 18$$



Unknowns > Equations, Stable & indeterminate 1st degree

H.w: Find the stability and determinacy of composite structure as shown below.

