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Al-Mustaqbal University / College of Engineering & Technology Department (Fuel & Energy)

Class (1st)

Subject (Mathematics1) / Code (UOMU027012)

(المشتقات: Lecturer (Derivatives

1stterm – Lect No. & Lect Name (#11, Derivative's Rule, Algebraic Deriv., Trig. Deriv., Velocity and Acceleration)

Derivative Rules = Feinh usla a derivative) raising col derivative is tinding a slope at any point-Before we go over the derivative Kutes, lots introduce the definition of the derivative Formula. Definition of the Derivative Formula : By using the limit process as de = f(x) = lim F(x+ax) - F(x) } -Fred find de of the following equation by namy F(x) = 5x - 2 501-F(x+ax) = 5(x+ax) -2 F(x) = 5x - 2plug the above two egs into eq & $\frac{df}{dx} = f'(x) = \lim_{\alpha k \to 0} \frac{5(x+\alpha k)-2 - (5x-2)}{\alpha k}$ = lim 8x+5 ax 12-8x+12

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find of For the following egs Sol. of F(K+ak) - F(K)	F(x) =	κ²
df - c'all - 6 f(K+ak) - f(K)		
df = p'(x) = lim f(x+ak) - f(x) ax		
$\star F(x+\alpha x) = (x+\alpha x)^2$		
$F(x) = x^2$		
- df $(x+\alpha x)^2 - x^2$ $(x+\alpha x)^2$	1(x+ax) -x2	
dx = anso ax = axso	ax	
= lim xx+ ax.x + ax.x + ax2-x1= li-	2X AK +	ak2
= lim ax (2x+ax) = lim (2x+	4X)	
$\frac{2}{\sqrt{\chi}} = 2\chi + 0 = \frac{2\chi}{2\chi}$	gine P.C 2	13.7
By your own exp. try to 12md	df for	the
	Tillian.	
	and the second second	
The state of the s		
	$\frac{df}{dx} = \lim_{\Delta x \to \infty} \frac{(x + \alpha x)^2 - x^2}{\Delta x} = \lim_{\Delta x \to \infty} \frac{(x + \alpha x)^2 - x^2}{\Delta x}$ $= \lim_{\Delta x \to \infty} \frac{x^2 + \alpha x \cdot x + \alpha x \cdot x + \alpha x^2 - x^2}{\Delta x} = \lim_{\Delta x \to \infty} \frac{(x + \alpha x)^2 - x^2}{\Delta x}$ $= \lim_{\Delta x \to \infty} \frac{\alpha x (2x + \alpha x)}{\Delta x} = \lim_{\Delta x \to \infty} (2x + \alpha x)$ $= \lim_{\Delta x \to \infty} \frac{\alpha x (2x + \alpha x)}{\Delta x} = \lim_{\Delta x \to \infty} (2x + \alpha x)$ $= \lim_{\Delta x \to \infty} \frac{\alpha x (2x + \alpha x)}{\Delta x} = \lim_{\Delta x \to \infty} (2x + \alpha x)$	$F(K) = \chi^{2}$ $\frac{df}{dK} = \lim_{\Delta K \to 0} \frac{(K + \Delta K)^{2} - K^{2}}{\Delta K} = \lim_{\Delta K \to 0} \frac{(K + \Delta K)(K + \Delta K) - K^{2}}{\Delta K}$ $= \lim_{\Delta K \to 0} \frac{\chi^{2} + \Delta K \cdot K + \Delta K \cdot K + \Delta K^{2} - \chi^{2}}{\Delta K} = \lim_{\Delta K \to 0} \frac{2K \Delta K + \Delta K}{\Delta K}$ $= \lim_{\Delta K \to 0} \frac{\Delta K}{\Delta K} = \lim_{\Delta K \to 0} \frac{2K \Delta K}{\Delta K} = \lim_{\Delta K \to 0} \frac{\Delta K}{\Delta K} = \lim_{\Delta K \to 0} \frac{2K \Delta K}{\Delta K} = \lim_{\Delta K \to 0} \frac{\Delta K}{$



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the Derivative River - Fairly 15/2
O constant derivative CIDI ácioles
$F(x) = \alpha \implies \frac{dF}{dx} = F(x) = 2eno$, $\alpha = constant$
2) varsable derivativo reil seine
$f(k) = x^n = \frac{df}{dk} = f'(k) = n x^{n-1}$, $n = ong no$
3) Multi-variable Funs soul, Find Very Tations
f(x)=h(x) = g(x) = dk = f'(x)= h'(x) = g'(x)
4) Quotient Funs Oils amo asimo
$f(x) = \frac{h(x)}{g(x)} \longrightarrow \frac{df}{dx} = f'(x) = \frac{g(x) - h'(x)}{(g(x))^2} - \frac{h(x) - g'(x)}{(g(x))^2}$
5) product Fings (ii) collection
 $F(x) = h(x) \cdot g(x) \Rightarrow \frac{dF}{dx} = f'(x) = h(x) - g'(x) + g(x) - h'(x)$
@ Power raised Finger on & see 215 asimo
$f(x) = [h(x)]^n \Rightarrow \frac{df}{dx} = f'(x) = n [h(x)]^{n-1} \cdot h'(x)$

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- 1	Examples 1:-
	1- F(x) = 4 -> F'(k) = Zero
	$2-F(x)=\chi$ \Rightarrow $f'(x)=1$
	3-F(x) = x4 => F'(x) = 4 x3
	$F(x) = 5x^3 \implies F(x) = 5x^2 = 15x^2$
-	6 CC = 2/2 = 2/2 = 2/2 = 1 3/4
	$6 - F(x) = \sqrt{x} \implies F'(x) = -3 \times = -3$
	$7 - F(x) = \sqrt[5]{x^2} \implies F(x) = x^{\frac{2}{5}} \implies F(0) = \frac{2}{5}x^{\frac{2}{5}-1} = \frac{2}{5}x^{\frac{2}{5}-1} = \frac{2}{5}x^{\frac{2}{5}} = \frac{2}{5}x^{\frac{2}{$
•	$8 - F(x) = 3x^5 + 7x \implies F(x) = 3 * 5 x + 7 = 15 x + 7$
	$q - F(x) = (x^4 - x^2 + 1)(5x^6 - 3x) \Rightarrow F(x) = (x^4 - x^2 + 1)(30x^5 - 3) +$
	(5x6-3x)(4x3-2x)
	$10 - F(x) = \frac{x^3 + 1}{x^4 + 1} \implies F'(x) = \frac{(x^4 + 1)(3x^2) - (x^3 + 1)(4x^3)}{(x^4 + 1)^2}$
	$\frac{10-F(\chi)}{\chi^4+1} \longrightarrow F(\chi) - \frac{1}{(\chi^4+1)^2}$
	11- F(x)= (x3+x2+x+1) => F(x)=5(x3+x2+x+1)*(3x2+2x+1)
125	
	12 FOR - 122-2X-1 = F(X) = 2X-2
	$ 2-F(x) = \sqrt{\chi^2-2\chi+1} \implies f'(x) = \frac{2\chi-2}{2\sqrt{\chi^2-2\chi+1}}$
	EX @/ Find the derivative of the quotient Pun
	at $x = 1$, $f(x) = \frac{x^3+1}{x^4}$
	$\alpha r = 1$, $r(x) = \frac{1}{\chi^4 + 1}$
-	(30L)
	2 - (14x) (3x13) - (13x1) (4x13)
	From GK3 # 10 = F'(x) = (14+1) (3+13) - (13+1) (4+13)
-	K-1
	2*3-2*4 6-8
2.6	2 4
	= 21

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	Trigonometric Derivatives azilzijdenjalazio
	- F(x) = 32x -> F'(x) = cosx
	$2 F(x) = \cos x \implies F^{1}(x) = -3 \sin x$
3	F(x) = tank -> F'(x) - see2x
	$f = F(x) = \cot x \longrightarrow F'(x) = -\csc^2 x$
	5-F(x) = seex => F'(x) = seex bank
	$G - F(x) = \csc x \longrightarrow F'(x) = -\csc x$ cot x
	EXE) Find the derivative of the ogs
	[Sobs
	F'(x) = dF = 5 cosx - 4 sec2x
	ENG) Find dx [8 seex - 5 cosx]
	501-1
	F'(K) = 8 seex tank - 5 (- sink) F'(K) = 8 seex tank + 5 sink
0	(SKD) Find of [2 cotx - 7 ESCX]
	1501-J
	f'(w = 2(-cse2x) -7 (-csex cotx)
	F'CH = -2 CSC2K +7 CSK Cotx

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-	Derivative Applications 563	ا حاقيه
	IF the time is denoted by to a location or a displacement Function (is	, and s(t) is
	Then,	
	velocity = V(t) = s'(t)	(السرعة)
	- Acceleration = a(t) = V'(t)	(1 (1 (1 (1)
	Velocity is gonna have a sign	associated wi
	it either Dositive or nagative,	i-e either
	moving to the roput or to the	e left or 11
	beer aur of apper les cie addle or	21 4 0 of Teyen
	على من الله عبد الله وسايد الما على كلا و	معيد اوا كان الحي الم
	ينون ميتعدا و اوا عام ١٥١ عام ١٥٥٠	رج ا دا کا ما ایم
	We have anothe torm, named	by speed,
-	which is always positive, so	we need to
	take the absolute value v	elocity to ge
	the speed	
	speed = \V(H)]	
	" Els " up a cod vill or sped so " als	عطا وها في تقو
	وكرة هو الحجر والذي كون موجيد واك" م	و کون مارما" ۱
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	EX) The following equation of motion descripe
	The obsplacement (in meter) of a particle moving in a straight line
	$5=5t^3+3t+8$ wher t is measured in seconds
	a- Find the volocity after t=2 seconds? b- Find the acceleration after t=2 seconds?
	[-Solution]
a	$V(t) = 5^{(t)} = 5(3t^2) + 3$ = 15t ² +3
	after 2 seconds => t=2
	$V(2) = 15(2)^{2} + 3 = 15 * 4 + 3$ V(2) = 63 M/see Ans @
<u>b</u>	a(t) = v'(t) = 5''(t) = 15 (2t)
	$= 30t$ $= (2) = 30(2) = 60 \text{ m/see}^2 \text{Ans} 60$