



## How DES Works in Detail

DES is a **block cipher**--meaning it operates on plaintext blocks of a given size (64-bits) and returns ciphertext blocks of the same size. Thus DES results in a **permutation** among the  $2^{64}$  (read this as: "2 to the 64th power") possible arrangements of 64 bits, each of which may be either 0 or 1. Each block of 64 bits is divided into two blocks of 32 bits each, a left half block **L** and a right half block **R**. (This division is only used in certain operations.)

**Example:** Let **M** be the plain text message **M** = 0123456789ABCDEF, where **M** is in hexadecimal (base 16) format. Rewriting **M** in binary format, we get the 64-bit block of text:

**M** = 0000 0001 0010 0011 0100 0101 0110 0111 1000 1001 1010 1011 1100 1101 1110 1111

**L** = 0000 0001 0010 0011 0100 0101 0110 0111

**R** = 1000 1001 1010 1011 1100 1101 1110 1111

The first bit of **M** is "0". The last bit is "1". We read from left to right.

DES operates on the 64-bit blocks using *key* sizes of 56- bits. The keys are actually stored as being 64 bits long, **but every 8th bit in the key is not used (i.e. bits numbered 8, 16, 24, 32, 40, 48, 56, and 64).**

**M** = 0000 0001 0010 0011 0100 0101 0110 0111 1000 1001 1010 1011 1100 1101 1110 1111

However, we will nevertheless number the bits from 1 to 64, going left to right, in the following calculations. But, as you will see, the eight bits just mentioned get eliminated when we create subkeys.

**Example:** Let **K** be the hexadecimal key **K** = 133457799BBCDFF1. This gives us as the binary key (setting 1 = 0001, 3 = 0011, etc., and grouping together every eight bits, of which the last one in each group will be unused):

**K** = 0001 0011 0011 0100 0101 0111 0111 1001 1001 1011 1011 1100 1101 1111 1111 0001

**K** = 0001 0011 0011 0100 0101 0111 0111 1001 1001 1011 1011 1100 1101 1111 1111 0001

The DES algorithm uses the following steps:

**Step 1: Create 16 subkeys, each of which is 48 bits long.**

The 64-bit key is permuted according to the following table, **PC-1**. Since the first entry in the table is "57", this means that the 57th bit of the original key **K** becomes the first bit of the permuted key **K+**. The 49th bit of the original key becomes the second bit of the permuted key. The 4th bit of the original key is the last bit of the permuted key. Note only 56 bits of the original key appear in the permuted key.

### PC-1

57	49	41	33	25	17	9
1	58	50	42	34	26	18
10	2	59	51	43	35	27
19	11	3	60	52	44	36
63	55	47	39	31	23	15



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7 62 54 46 38 30 22  
14 6 61 53 45 37 29  
21 13 5 28 20 12 4

**Example:** From the original 64-bit key

**K** = 00010011 00110100 01010111 01111001 10011011 10111100 11011111 11110001

**K** = 0001 0011 0011 0100 0101 0111 0111 1001 1001 1011 1011 1100 1101 1111 1111 0001

we get the 56-bit permutation

**K**<sup>+</sup> = 1111000 0110011 0010101 0101111 0101010 1011001 1001111 0001111

**K**<sup>+</sup> = 1111000 0110011 0010101 0101111 0101010 1011001 1001111 0001111

Next, split this key into left and right halves, **C**<sub>0</sub> and **D**<sub>0</sub>, where each half has 28 bits.

**Example:** From the permuted key **K**<sup>+</sup>, we get

**C**<sub>0</sub> = 1111000 0110011 0010101 0101111

**D**<sub>0</sub> = 0101010 1011001 1001111 0001111

With **C**<sub>0</sub> and **D**<sub>0</sub> defined, we now create sixteen blocks **C**<sub>*n*</sub> and **D**<sub>*n*</sub>, 1 ≤ *n* ≤ 16. Each pair of blocks **C**<sub>*n*</sub> and **D**<sub>*n*</sub> is formed from the previous pair **C**<sub>*n-1*</sub> and **D**<sub>*n-1*</sub>, respectively, for *n* = 1, 2, ..., 16, using the following schedule of "left shifts" of the previous block. To do a left shift, move each bit one place to the left, except for the first bit, which is cycled to the end of the block.

Iteration Number	Number of Left Shifts
1	1
2	1
3	2
4	2
5	2
6	2
7	2
8	2
9	1



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10	2
11	2
12	2
13	2
14	2
15	2
16	1

This means, for example,  $C_3$  and  $D_3$  are obtained from  $C_2$  and  $D_2$ , respectively, by two left shifts, and  $C_{16}$  and  $D_{16}$  are obtained from  $C_{15}$  and  $D_{15}$ , respectively, by one left shift. In all cases, by a single left shift is meant a rotation of the bits one place to the left, so that after one left shift the bits in the 28 positions are the bits that were previously in positions 2, 3, ..., 28, 1.

**Example:** From original pair  $C_0$  and  $D_0$  we obtain:

$C_0 = 1111000011001100101010101111$

$D_0 = 0101010101100110011110001111$

$C_1 = 1110000110011001010101011111$  Shift 1 position to left

$D_1 = 1010101011001100111100011110$

$C_2 = 1100001100110010101010111111$  Shift 1 position to left

$D_2 = 0101010110011001111000111101$

$C_3 = 0000110011001010101011111111$  Shift 2 position to left

$D_3 = 0101011001100111100011110101$

$C_4 = 0011001100101010101111111100$  Shift 2 position to left

$D_4 = 0101100110011110001111010101$

$C_5 = 1100110010101010111111110000$  Shift 2 position to left

$D_5 = 0110011001111000111101010101$

$C_6 = 0011001010101011111111000011$  Shift 2 position to left

$D_6 = 1001100111100011110101010101$

$C_7 = 1100101010101111111100001100$  Shift 2 position to left

$D_7 = 0110011110001111010101010110$

$C_8 = 0010101010111111110000110011$  Shift 2 position to left

$D_8 = 1001111000111101010101011001$



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$C_9 = 010101010111111100001100110$  Shift 1 position to left

$D_9 = 0011110001111010101010110011$

$C_{10} = 010101011111110000110011001$  Shift 2 position to left

$D_{10} = 1111000111101010101011001100$

$C_{11} = 010101111111000011001100101$  Shift 2 position to left

$D_{11} = 1100011110101010101100110011$

$C_{12} = 010111111100001100110010101$  Shift 2 position to left

$D_{12} = 0001111010101010110011001111$

$C_{13} = 011111110000110011001010101$  Shift 2 position to left

$D_{13} = 0111101010101011001100111100$

$C_{14} = 111111000011001100101010101$  Shift 2 position to left

$D_{14} = 1110101010101100110011110001$

$C_{15} = 1111100001100110010101010111$  Shift 2 position to left

$D_{15} = 1010101010110011001111000111$

$C_{16} = 1111000011001100101010101111$  Shift 1 position to left

$D_{16} = 0101010101100110011110001111$

We now form the keys  $K_n$ , for  $1 \leq n \leq 16$ , by applying the following permutation table to each of the concatenated pairs  $C_n D_n$ . Each pair has 56 bits, but **PC-2** only uses 48 of these.

### PC-2

14	17	11	24	1	5
3	28	15	6	21	10
23	19	12	4	26	8
16	7	27	20	13	2
41	52	31	37	47	55
30	40	51	45	33	48
44	49	39	56	34	53
46	42	50	36	29	32

Therefore, the first bit of  $K_n$  is the 14th bit of  $C_n D_n$ , the second bit the 17th, and so on, ending with the 48th bit of  $K_n$  being the 32th bit of  $C_n D_n$ .



**Example:** For the first key we have  $C_1D_1 = 1110000\ 1100110\ 0101010\ 1011111\ 1010101\ 0110011\ 0011110\ 0011110$

which, after we apply the permutation **PC-2**, becomes

$K_1 = 000110\ 110000\ 001011\ 101111\ 111111\ 000111\ 000001\ 110010$

For the other keys we have

$K_2 = 011110\ 011010\ 111011\ 011001\ 110110\ 111100\ 100111\ 100101$

$K_3 = 010101\ 011111\ 110010\ 001010\ 010000\ 101100\ 111110\ 011001$

$K_4 = 011100\ 101010\ 110111\ 010110\ 110110\ 110011\ 010100\ 011101$

$K_5 = 011111\ 001110\ 110000\ 000111\ 111010\ 110101\ 001110\ 101000$

$K_6 = 011000\ 111010\ 010100\ 111110\ 010100\ 000111\ 101100\ 101111$

$K_7 = 111011\ 001000\ 010010\ 110111\ 111101\ 100001\ 100010\ 111100$

$K_8 = 111101\ 111000\ 101000\ 111010\ 110000\ 010011\ 101111\ 111011$

$K_9 = 111000\ 001101\ 101111\ 101011\ 111011\ 011110\ 011110\ 000001$

$K_{10} = 101100\ 011111\ 001101\ 000111\ 101110\ 100100\ 011001\ 001111$

$K_{11} = 001000\ 010101\ 111111\ 010011\ 110111\ 101101\ 001110\ 000110$

$K_{12} = 011101\ 010111\ 000111\ 110101\ 100101\ 000110\ 011111\ 101001$

$K_{13} = 100101\ 111100\ 010111\ 010001\ 111110\ 101011\ 101001\ 000001$

$K_{14} = 010111\ 110100\ 001110\ 110111\ 111100\ 101110\ 011100\ 111010$

$K_{15} = 101111\ 111001\ 000110\ 001101\ 001111\ 010011\ 111100\ 001010$

$K_{16} = 110010\ 110011\ 110110\ 001011\ 000011\ 100001\ 011111\ 110101$

So much for the subkeys. Now we look at the message itself.

## Step 2: Encode each 64-bit block of data.

There is an *initial permutation IP* of the 64 bits of the message data **M**. This rearranges the bits according to the following table, where the entries in the table show the new arrangement of the bits from their initial order. The 58th bit of **M** becomes the first bit of **IP**. The 50th bit of **M** becomes the second bit of **IP**. The 7th bit of **M** is the last bit of **IP**.

### IP

58	50	42	34	26	18	10	2
60	52	44	36	28	20	12	4
62	54	46	38	30	22	14	6
64	56	48	40	32	24	16	8
57	49	41	33	25	17	9	1
59	51	43	35	27	19	11	3



61 53 45 37 29 21 13 5

63 55 47 39 31 23 15 7

**Example:** Applying the initial permutation to the block of text **M**, given previously, we get

**M** = 0000 0001 0010 0011 0100 0101 0110 0111 1000 1001 1010 1011 1100 1101 1110 1111

**IP** = 1100 1100 0000 0000 1100 1100 1111 1111 1111 0000 1010 1010 1111 0000 1010 1010

Here the 58th bit of **M** is "1", which becomes the first bit of **IP**. The 50th bit of **M** is "1", which becomes the second bit of **IP**. The 7th bit of **M** is "0", which becomes the last bit of **IP**.

Next divide the permuted block **IP** into a left half **L<sub>0</sub>** of 32 bits, and a right half **R<sub>0</sub>** of 32 bits.

**Example:** From **IP**, we get **L<sub>0</sub>** and **R<sub>0</sub>**

**L<sub>0</sub>** = 1100 1100 0000 0000 1100 1100 1111 1111

**R<sub>0</sub>** = 1111 0000 1010 1010 1111 0000 1010 1010

We now proceed through 16 iterations, for  $1 \leq n \leq 16$ , using a function **f** which operates on two blocks--a data block of 32 bits and a key **K<sub>n</sub>** of 48 bits--to produce a block of 32 bits. **Let + denote XOR addition, (bit-by-bit addition modulo 2).** Then for **n** going from 1 to 16 we calculate

$$L_n = R_{n-1}$$

$$R_n = L_{n-1} + f(R_{n-1}, K_n)$$

This results in a final block, for  $n = 16$ , of **L<sub>16</sub>R<sub>16</sub>**. That is, in each iteration, we take the right 32 bits of the previous result and make them the left 32 bits of the current step. For the right 32 bits in the current step, we XOR the left 32 bits of the previous step with the calculation **f**.

**Example:** For  $n = 1$ , we have

**K<sub>1</sub>** = 000110 110000 001011 101111 111111 000111 000001 110010

**L<sub>1</sub>** = **R<sub>0</sub>** = 1111 0000 1010 1010 1111 0000 1010 1010

**R<sub>1</sub>** = **L<sub>0</sub>** + **f(R<sub>0</sub>, K<sub>1</sub>)**

It remains to explain how the function **f** works. To calculate **f**, we first expand each block **R<sub>n-1</sub>** from 32 bits to 48 bits. This is done by using a selection table that repeats some of the bits in **R<sub>n-1</sub>**. We'll call the use of this selection table the function **E**. Thus **E(R<sub>n-1</sub>)** has a 32 bit input block, and a 48 bit output block.

Let **E** be such that the 48 bits of its output, written as 8 blocks of 6 bits each, are obtained by selecting the bits in its inputs in order according to the following table:

## E BIT-SELECTION TABLE

32 1 2 3 4 5



4	5	6	7	8	9
8	9	10	11	12	13
12	13	14	15	16	17
16	17	18	19	20	21
20	21	22	23	24	25
24	25	26	27	28	29
28	29	30	31	32	1

Thus, the first three bits of  $E(R_{n-1})$  are the bits in positions 32, 1 and 2 of  $R_{n-1}$  while the last 2 bits of  $E(R_{n-1})$  are the bits in positions 32 and 1.

**Example:** We calculate  $E(R_0)$  from  $R_0$  as follows:

$R_0 = 1111\ 0000\ 1010\ 1010\ 1111\ 0000\ 1010\ 1010$

$E(R_0) = 011110\ 100001\ 010101\ 010101\ 011110\ 100001\ 010101\ 010101$

(Note that each block of 4 original bits has been expanded to a block of 6 output bits.)

Next in the  $f$  calculation, we XOR the output  $E(R_{n-1})$  with the key  $K_n$ :

$K_n + E(R_{n-1})$ .

**Example:** For  $K_1$ ,  $E(R_0)$ , we have

$K_1 = 000110\ 110000\ 001011\ 101111\ 111111\ 000111\ 000001\ 110010$

$E(R_0) = 011110\ 100001\ 010101\ 010101\ 011110\ 100001\ 010101\ 010101$

$K_1 + E(R_0) = 011000\ 010001\ 011110\ 111010\ 100001\ 100110\ 010100\ 100111$ .

We have not yet finished calculating the function  $f$ . To this point we have expanded  $R_{n-1}$  from 32 bits to 48 bits, using the selection table, and XORed the result with the key  $K_n$ . We now have 48 bits, or eight groups of six bits. We now do something strange with each group of six bits: we use them as addresses in tables called "**S boxes**". Each group of six bits will give us an address in a different S box. Located at that address will be a 4 bit number. This 4 bit number will replace the original 6 bits. The net result is that the eight groups of 6 bits are transformed into eight groups of 4 bits (the 4-bit outputs from the S boxes) for 32 bits total.

Write the previous result, which is 48 bits, in the form:

$K_n + E(R_{n-1}) = B_1B_2B_3B_4B_5B_6B_7B_8$ ,

where each  $B_i$  is a group of six bits. We now calculate

$S_1(B_1)S_2(B_2)S_3(B_3)S_4(B_4)S_5(B_5)S_6(B_6)S_7(B_7)S_8(B_8)$



where  $S_i(B_i)$  refers to the output of the  $i$ -th  $S$  box.

To repeat, each of the functions  $S_1, S_2, \dots, S_8$ , takes a 6-bit block as input and yields a 4-bit block as output. The table to determine  $S_1$  is shown and explained below:

<b>S1</b>															
<b>Column Number</b>															
<b>Row</b>															
<b>No.</b>	<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>	<b>11</b>	<b>12</b>	<b>13</b>	<b>14 15</b>
<b>0</b>	14	4	13	1	2	15	11	8	3	10	6	12	5	9	0 7
<b>1</b>	0	15	7	4	14	2	13	1	10	6	12	11	9	5	3 8
<b>2</b>	4	1	14	8	13	6	2	11	15	12	9	7	3	10	5 0
<b>3</b>	15	12	8	2	4	9	1	7	5	11	3	14	10	0	6 13

If  $S_1$  is the function defined in this table and  $B$  is a block of 6 bits, then  $S_1(B)$  is determined as follows: The first and last bits of  $B$  represent in base 2 a number in the decimal range 0 to 3 (or binary 00 to 11). Let that number be  $i$ . The middle 4 bits of  $B$  represent in base 2 a number in the decimal range 0 to 15 (binary 0000 to 1111). Let that number be  $j$ . Look up in the table the number in the  $i$ -th row and  $j$ -th column. It is a number in the range 0 to 15 and is uniquely represented by a 4 bit block. That block is the output  $S_1(B)$  of  $S_1$  for the input  $B$ . For example, for input block  $B = 011011$  the first bit is "0" and the last bit "1" giving 01 as the row. This is row 1. The middle four bits are "1101". This is the binary equivalent of decimal 13, so the column is column number 13. In row 1, column 13 appears 5. This determines the output; 5 is binary 0101, so that the output is 0101. Hence  $S_1(011011) = 0101$ .

The tables defining the functions  $S_1, \dots, S_8$  are the following:

<b>S1</b>															
14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7
0	15	7	4	14	2	13	1	10	6	12	11	9	5	3	8
4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0
15	12	8	2	4	9	1	7	5	11	3	14	10	0	6	13

**S2**





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15 1 8 14 6 11 3 4 9 7 2 13 12 0 5 10  
3 13 4 7 15 2 8 14 12 0 1 10 6 9 11 5  
0 14 7 11 10 4 13 1 5 8 12 6 9 3 2 15  
13 8 10 1 3 15 4 2 11 6 7 12 0 5 14 9

### S3

10 0 9 14 6 3 15 5 1 13 12 7 11 4 2 8  
13 7 0 9 3 4 6 10 2 8 5 14 12 11 15 1  
13 6 4 9 8 15 3 0 11 1 2 12 5 10 14 7  
1 10 13 0 6 9 8 7 4 15 14 3 11 5 2 12

### S4

7 13 14 3 0 6 9 10 1 2 8 5 11 12 4 15  
13 8 11 5 6 15 0 3 4 7 2 12 1 10 14 9  
10 6 9 0 12 11 7 13 15 1 3 14 5 2 8 4  
3 15 0 6 10 1 13 8 9 4 5 11 12 7 2 14

### S5

2 12 4 1 7 10 11 6 8 5 3 15 13 0 14 9  
14 11 2 12 4 7 13 1 5 0 15 10 3 9 8 6  
4 2 1 11 10 13 7 8 15 9 12 5 6 3 0 14  
11 8 12 7 1 14 2 13 6 15 0 9 10 4 5 3

### S6

12 1 10 15 9 2 6 8 0 13 3 4 14 7 5 11  
10 15 4 2 7 12 9 5 6 1 13 14 0 11 3 8  
9 14 15 5 2 8 12 3 7 0 4 10 1 13 11 6  
4 3 2 12 9 5 15 10 11 14 1 7 6 0 8 13

### S7

4 11 2 14 15 0 8 13 3 12 9 7 5 10 6 1



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13 0 11 7 4 9 1 10 14 3 5 12 2 15 8 6  
 1 4 11 13 12 3 7 14 10 15 6 8 0 5 9 2  
 6 11 13 8 1 4 10 7 9 5 0 15 14 2 3 12

### S8

13 2 8 4 6 15 11 1 10 9 3 14 5 0 12 7  
 1 15 13 8 10 3 7 4 12 5 6 11 0 14 9 2  
 7 11 4 1 9 12 14 2 0 6 10 13 15 3 5 8  
 2 1 14 7 4 10 8 13 15 12 9 0 3 5 6 11

**Example:** For the first round, we obtain as the output of the eight **S** boxes:

$$K_1 + E(R_0) = 011000\ 010001\ 011110\ 111010\ 100001\ 100110\ 010100\ 100111.$$

$$S_1(B_1)S_2(B_2)S_3(B_3)S_4(B_4)S_5(B_5)S_6(B_6)S_7(B_7)S_8(B_8) = 0101\ 1100\ 1000\ 0010\ 1011\ 0101\ 1001\ 0111$$

The final stage in the calculation of  $f$  is to do a permutation **P** of the **S**-box output to obtain the final value of  $f$ :

$$f = P(S_1(B_1)S_2(B_2)...S_8(B_8))$$

The permutation **P** is defined in the following table. **P** yields a 32-bit output from a 32-bit input by permuting the bits of the input block.

### P

16 7 20 21  
 29 12 28 17  
 1 15 23 26  
 5 18 31 10  
 2 8 24 14  
 32 27 3 9  
 19 13 30 6  
 22 11 4 25

**Example:** From the output of the eight **S** boxes:



$$S_1(B_1)S_2(B_2)S_3(B_3)S_4(B_4)S_5(B_5)S_6(B_6)S_7(B_7)S_8(B_8) = 0101\ 1100\ 1000\ 0010\ 1011\ 0101\ 1001\ 0111$$

we get

$$f = 0010\ 0011\ 0100\ 1010\ 1010\ 1001\ 1011\ 1011$$

$$R_1 = L_0 + f(R_0, K_1)$$

$$\begin{aligned} &= 1100\ 1100\ 0000\ 0000\ 1100\ 1100\ 1111\ 1111 \\ &+ 0010\ 0011\ 0100\ 1010\ 1010\ 1001\ 1011\ 1011 \\ &= 1110\ 1111\ 0100\ 1010\ 0110\ 0101\ 0100\ 0100 \end{aligned}$$

In the next round, we will have  $L_2 = R_1$ , which is the block we just calculated, and then we must calculate  $R_2 = L_1 + f(R_1, K_2)$ , and so on for 16 rounds. At the end of the sixteenth round we have the blocks  $L_{16}$  and  $R_{16}$ . We then *reverse* the order of the two blocks into the 64-bit block

$$R_{16}L_{16}$$

and apply a final permutation  $IP^{-1}$  as defined by the following table:

$IP^{-1}$

40	8	48	16	56	24	64	32
39	7	47	15	55	23	63	31
38	6	46	14	54	22	62	30
37	5	45	13	53	21	61	29
36	4	44	12	52	20	60	28
35	3	43	11	51	19	59	27
34	2	42	10	50	18	58	26
33	1	41	9	49	17	57	25

That is, the output of the algorithm has bit 40 of the output block as its first bit, bit 8 as its second bit, and so on, until bit 25 of the output block is the last bit of the output.

**Example:** If we process all 16 blocks using the method defined previously, we get, on the 16th round,

$$L_{16} = 0100\ 0011\ 0100\ 0010\ 0011\ 0010\ 0011\ 0100$$

$$R_{16} = 0000\ 1010\ 0100\ 1100\ 1101\ 1001\ 1001\ 0101$$

We reverse the order of these two blocks and apply the final permutation to



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$R_{16}L_{16} = 00001010\ 01001100\ 11011001\ 10010101\ 01000011\ 01000010\ 00110010\ 00110100$

$IP^{-1} = 10000101\ 11101000\ 00010011\ 01010100\ 00001111\ 00001010\ 10110100\ 00000101$

which in hexadecimal format is

85E813540F0AB405.

This is the encrypted form of  $\mathbf{M} = 0123456789ABCDEF$ : namely,  $\mathbf{C} = 85E813540F0AB405$ .

Decryption is simply the inverse of encryption, following the same steps as above, but reversing the order in which the subkeys are applied.