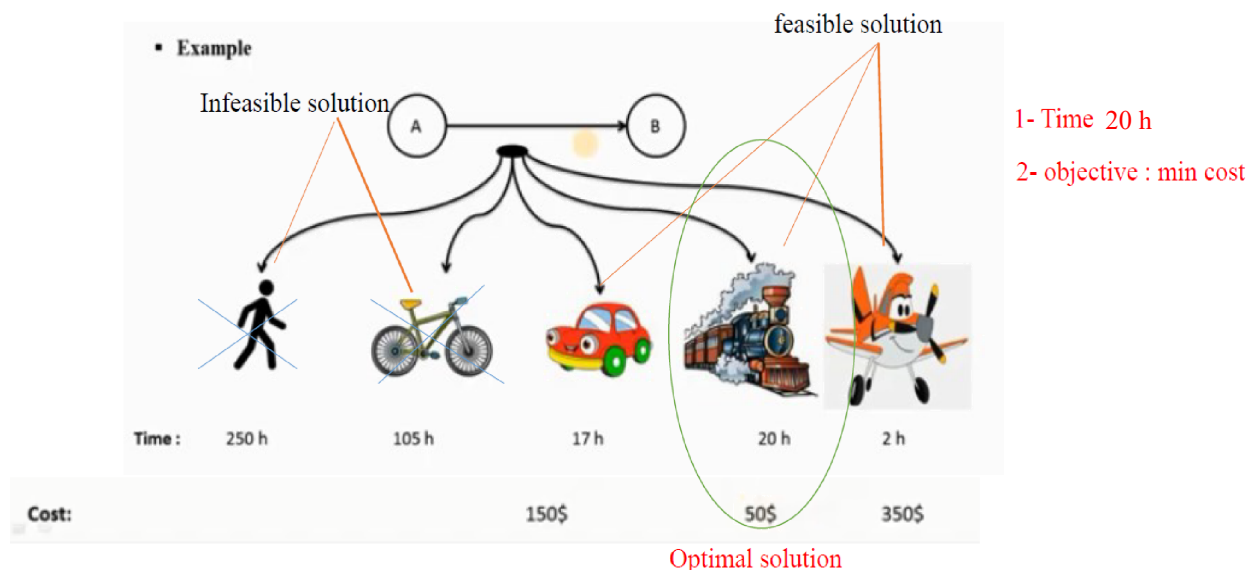


Introduction

- ❖ Finding the best solution among set of all feasible solutions.
- ❖ Deals with the problem of minimizing or maximizing a function with several variables subject to some constraints.
- ❖ Every, almost daily, solves optimisation problems in formal ways by using mental models.
- ❖ Optimisation plays a central rule in operation research, managing science and engineering.



• Best design

- solving for the number of pipes in a piping network that result in minimal pressure drop
- solving for the size of an engine block that results in the best combination of speed and efficiency (using some weighting on each of these metrics its importance)

❖ Lowest cost

- Find the combination of truck routs to transport a set amount of raw material between points that results in the lowest total cost (labour, truck maintained fuel)

❖ Highest efficiency

- Maximising the efficiency of a power production system by finding the right combination of inputs (flow rate, temperatures, pressure,...)

• In Chemical Engineering

- ❖ Utilize resource/energy/utility in the most efficiency way.
- ❖ Reduce waste generation; minimize the environmental impact.
- ❖ Determine the most desirable operating conditions; safe operation
- ❖ Meet product specification; maximize profit.
- ❖ deciding on the most effective allocation of limited resources
- ❖ choosing control variables that will cause a system to behave as desired.

Why optimize



- Some objectives in optimisation problems may be:

- minimise cost
- Maximise the profit
- planning production
- increase process efficiency



What is mean optimization?

- Optimization is an act, process or methodology of making something (system, design or decision) as fully perfect, functional and effective as possible to achieve optimum solution.
- A collective process of finding the best conditions required to achieve the best results from a given situation.
- It is one of the major quantitative tools in the machinery of decision-making. A wide variety of problems in the design, construction, operation and analysis of chemical plants can be resolved by optimization.

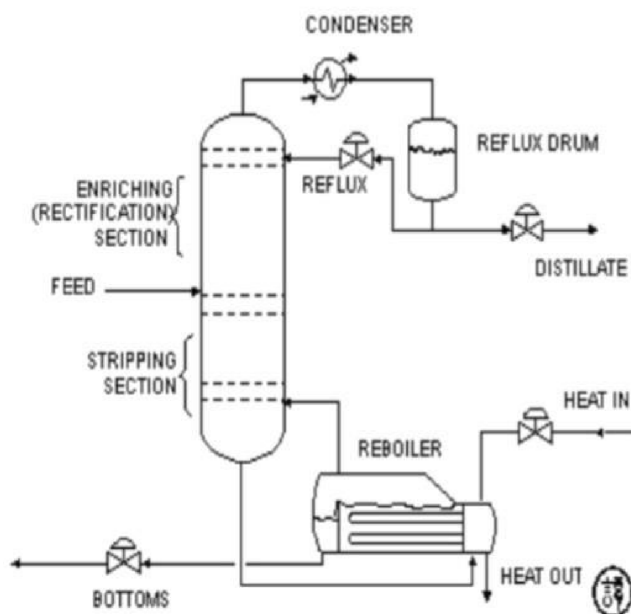
Some other important definitions:

- Optimum value: it is a technical term including quantities measurements and mathematical analysis to determine the best setting (maximum or minimum) of a dependent variables.
- Optimization procedure: it is the process of determining the optimum value (maximum or minimum) of some criterion function.
- Optimization problem: is the specification of the variables that need to be optimized.

The optimization is interested for the engineers. Why?

- Engineers work to improve the initial design of process and equipment.
- Engineers strive for enhancements in the operation, in order to realize:
 - 1- Largest production.
 - 2- Greatest profit.
 - 3- Minimum cost (least energy usage).

Distillation column parameters' that could enhance the equipment performance (optimal condition)



- Equipment size.
- Schedule maintenance and equipment replacement.
- Design of heat exchanger network.
- Operation planning scheduling.
- Control system.
- Long time between shutdown.



In plant operation, benefits arise from improved plant performance such as:

- Improved yields of valuable products or reduced yields of contaminations.
- Reduced energy consumption.
- Higher processing rates.
- Longer times between shutdowns.
- Reduced maintenance costs.
- Less equipment wear.
- Better staff utilization.

Example of applications of optimization:

- Determination of best sites for plant location.
- Routing of tankers for the distribution of crude and refined products.
- Pipeline sizing and layout.
- Equipment and entire plant design.
- Maintenance and equipment replacement scheduling.
- Operation of equipment, such as tubular reactors, columns, exchangers.....etc.
- Evaluation of plant data to construct a model of a process.
- Minimization of inventory charges.
- And many other



Statements of an optimization problem:

All optimization problem are stated in some standard form. You have to identify the essential elements of a given problem and translate them into a prescribed mathematical form.

- **Decisions:** items that need to be figured out to achieve max. efficiency.
- **The ranking function:** a method to make different choices of decisions.
- **Rules and restrictions:** specifying limitations on choices of decision values.
- **Parameters:** information necessary in specifying ranking function and rules.

Optimization models

Which is the mathematical representation of optimization problem to analyze or solve the optimization problem.

These models have:

1. **Objective function:** terms of design or decision variable and other problem or process parameters such as cost function. This function could be economical or technical. For example: economic objectives, maximize profit, minimize costs of production.
2. **constraints:** represent limitation on the choice of decision variables, either internal or external imposed by the designer.
3. **Parameters:** represent the given data.
4. **Decision (design) variables:** represent items that need to be determined and may involve many design variables.

Important note: there is no scope (room) for optimization, if all the design variable are fixed.

• **Example#1 (optimal design of a can)**

Design which will hold at least 500 ml of liquid. Height = [7 12] cm, radius = [3 7] cm? what is the dimensions for the cylindrical Can use the least amount? We can minimize the material by minimize the area A!.

So, objective function:

$$A = 2 \pi r^2 + 2 \pi r h$$

Area of two ends Lateral Area

Constraint:
 $V = \pi r^2 h \geq 500$

Bounds (Decision variables):

$$3 \leq r \leq 7$$

$$7 \leq h \leq 12$$

- What is the dimensions for the cylindrical can use the least amount?

- we can minimize the material by reduce the area, A.

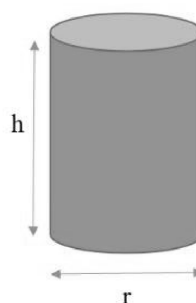


Figure 1. dimensions of can.

Example#2 (The optimal pipe diameter)

- Determination of optimal pipe diameter that uses for pumping a given amount of fluid from one point to another.

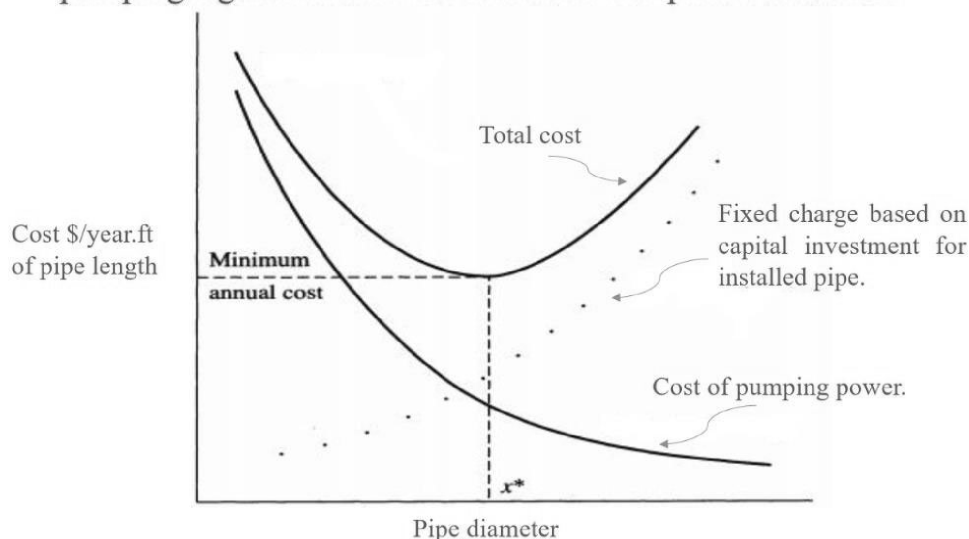


Figure 2. determination of optimum economic pipe diameter for constant mass through rates. (x^* = optimum diameter)



Notes:

- Total cost = pumping cost + fixed cost for the installed piping system.
- Pumping cost increase with decreased size of pipe diameter, why?
- Final results that can be accomplished by using an infinite number of different pipe diameters are the same.
- The fixed charges (installed) for the pipeline become lower when smaller pipe diameters are used, why?
- The optimum economic diameter is found where the sum of the pumping costs and fixed costs for the pipeline becomes a minimum.
- Even though, the engineer must choose the cheapest design by considering the quality of the product and the operation as well as the total cost.

Example#3 (the optimal insulation thickness)

- Additional insulation should save money through reducing heat losses.
- But, the insulation material can be expensive?
- So, we need the optimal amount of insulation.

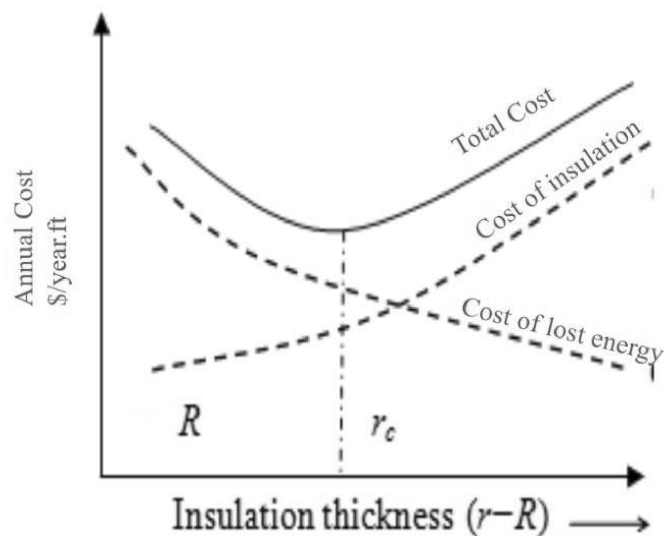


Figure 3. The effect of insulation thickness on total cost (x^* = optimum thickness)