

Digital to Analog

Digital to Analog Converters

A digital to analog converter (DAC) converts a digital signal or values to an analog voltage or current output.

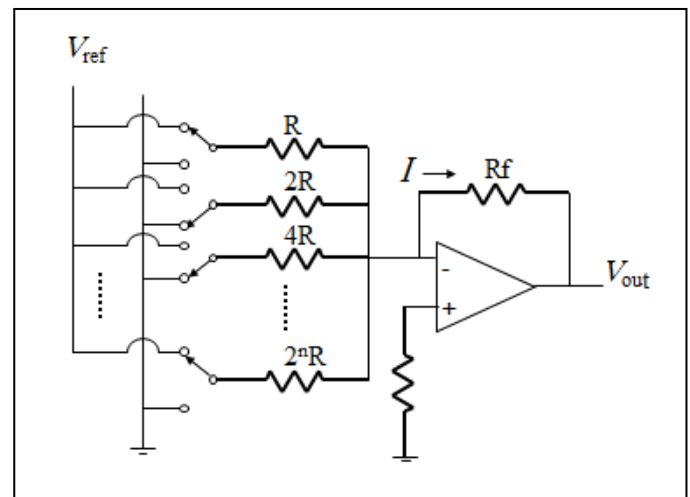
Types of DACs

There are two types of DAC and usually used switches, resistors, and op-amps to implement conversion, two types are:

- Binary Weighted Resistor.
- R-2R Ladder.

Binary Weighted Resistor:

- Weighted resistors are used to distinguish each bit from the most significant to the least significant.
- Switches are used to switch between V_{ref} and ground (bit high or low).
- $V_{out} = -IR_f$
- Voltages V_1 to V_n are either V_{ref} if corresponding bit is high or ground if corresponding bit is low
- V_1 is most significant bit
- V_n is least significant bit



$$V_{out} = -IR_f = -R_f \left(\frac{V_1}{R} + \frac{V_2}{2R} + \frac{V_3}{4R} + \dots + \frac{V_n}{2^{n-1}R} \right)$$

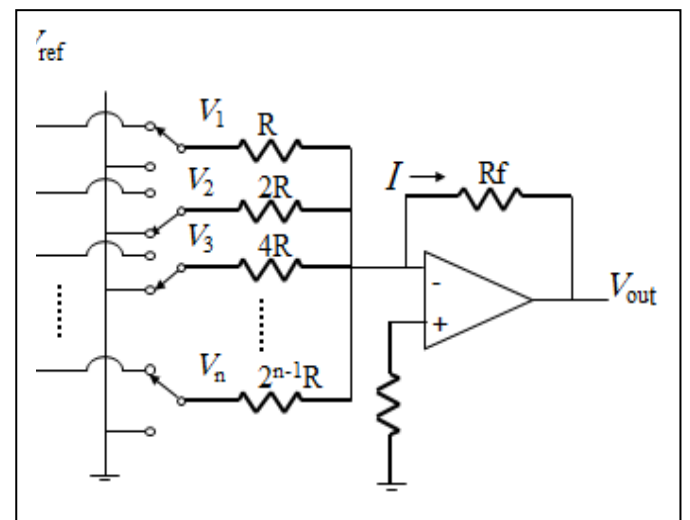
If $R_f = R/2$

$$V_{out} = -IR_f = - \left(\frac{V_1}{2} + \frac{V_2}{4} + \frac{V_3}{8} + \dots + \frac{V_n}{2^n} \right)$$

For example, a 4-Bit converter yields

$$V_{out} = -V_{ref} \left(b_3 \frac{1}{2} + b_2 \frac{1}{4} + b_1 \frac{1}{8} + b_0 \frac{1}{16} \right)$$

Where b_3 corresponds to Bit-3, b_2 to Bit-2, etc.

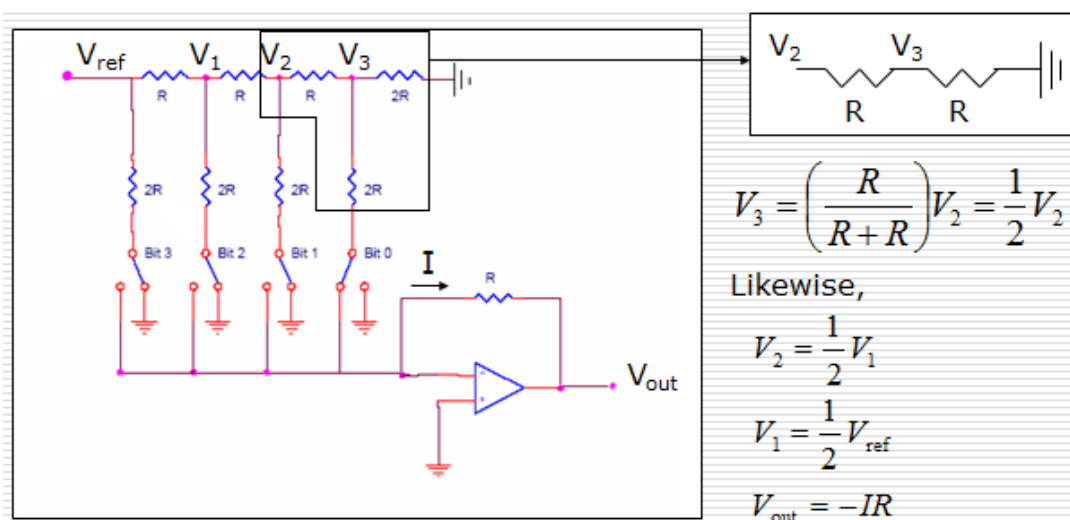
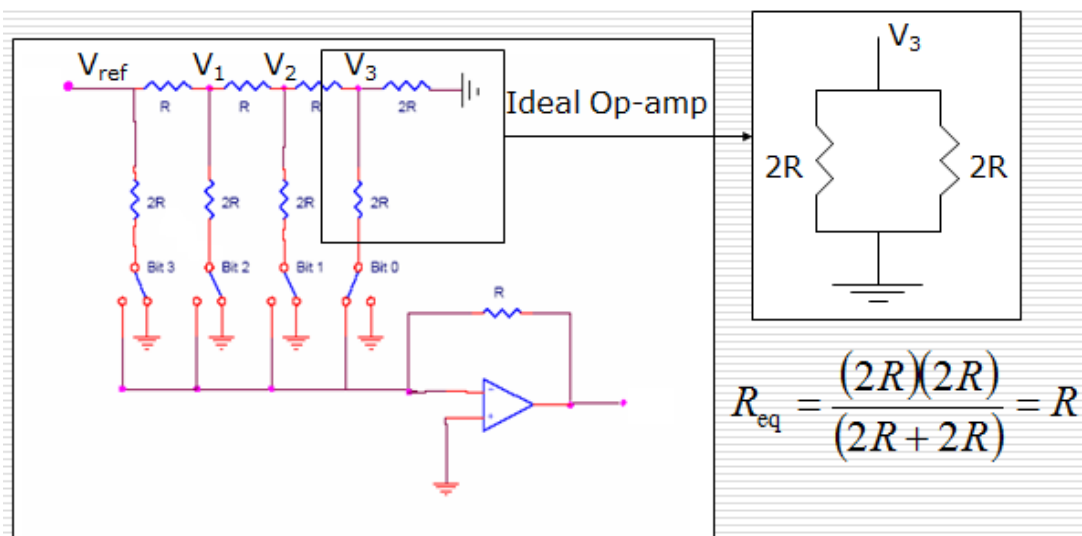
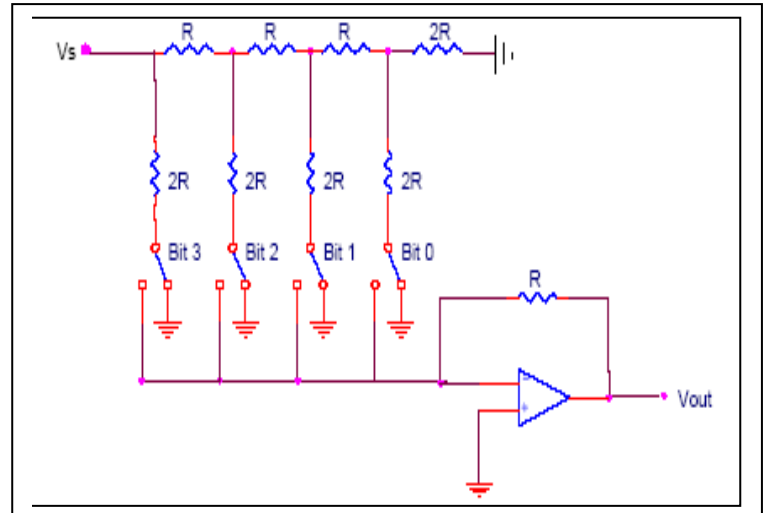


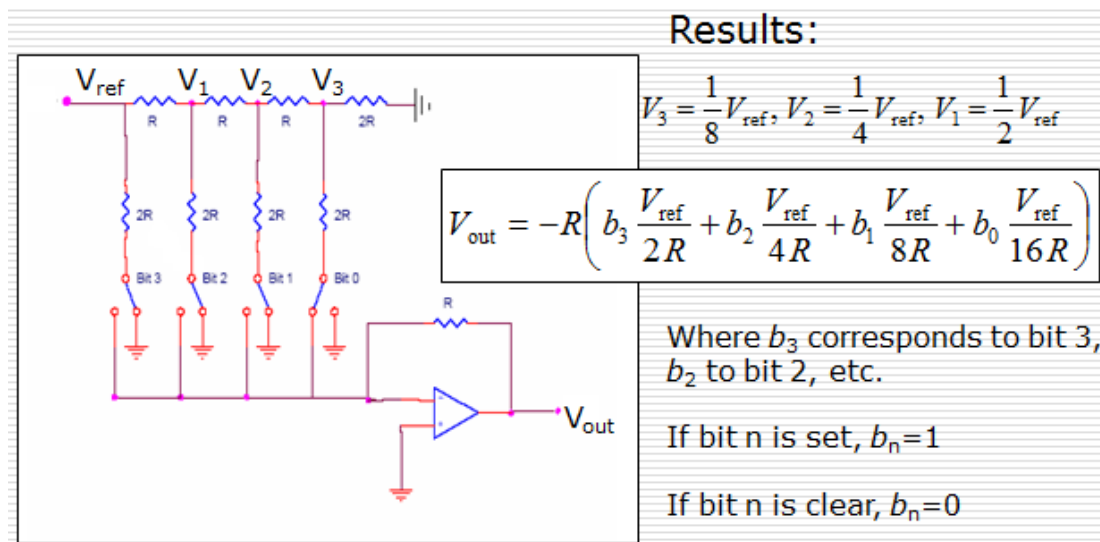
Advantages and Disadvantages

- Simple Construction, Fast Conversion.
- Limited to ~ 8 bits, large number of resistors, susceptible to noise, expensive and greater error.

R-2R Ladder:

- Each bit corresponds to a switch:
- If the bit is high, the corresponding switch is connected to the inverting input of the op-amp.
- If the bit is low, the corresponding switch is connected to ground.
- All bits pass through resistance of $2R$





For a 4-Bit R-2R Ladder

$$V_{\text{out}} = -V_{\text{ref}} \left(b_3 \frac{1}{2} + b_2 \frac{1}{4} + b_1 \frac{1}{8} + b_0 \frac{1}{16} \right)$$

For general n-Bit R-2R Ladder or Binary Weighted Resistor DAC

$$V_{\text{out}} = -V_{\text{ref}} \sum_{i=1}^n b_{n-i} \frac{1}{2^i}$$

Advantages and Disadvantages

- Only two resistors values (R and 2R), does not require high precision resistors.
- Lower conversion speed than binary weighted DAC.

Specifications of DACs

- Resolution
- Speed
- Linearity
- Settling Time
- Reference Voltages
- Errors

Resolution is the amount of variance in output voltage for every change of the LSB in the digital input.

How closely can we approximate the desired output signal (Higher Res. = finer detail=smaller Voltage divisions)

Common DAC has an 8-16 bit resolution $\text{Resolution} = V_{\text{LSB}} = \frac{V_{\text{ref}}}{2^N}$

where $N = \text{number of bits}$

Speed Rate of conversion of a single digital input to its analog equivalent.

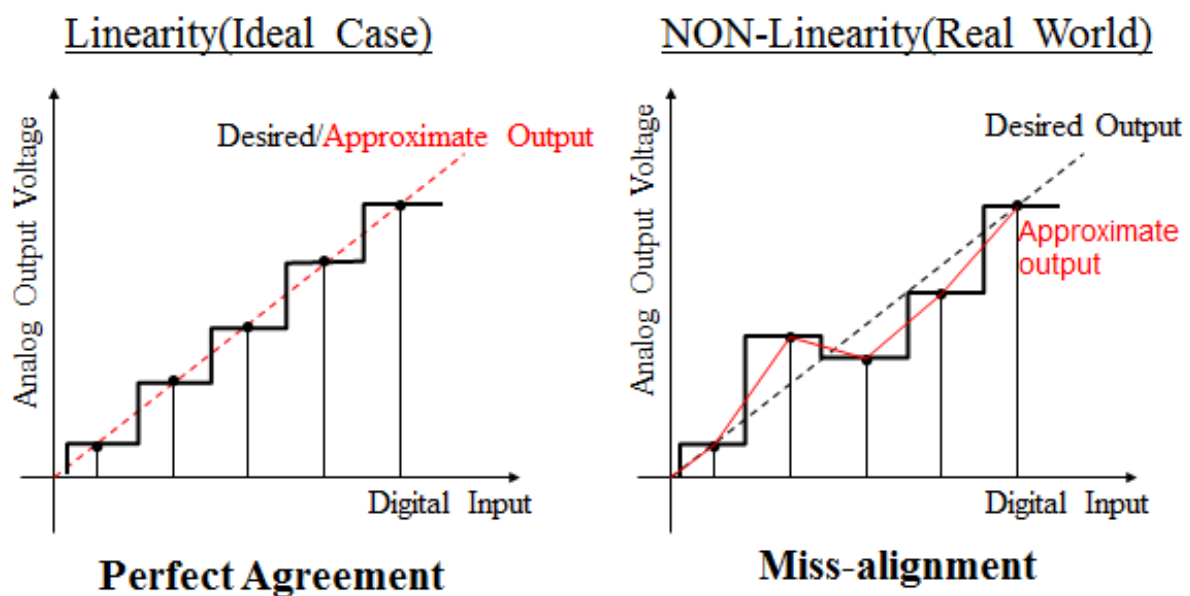
Conversion rate depends on:

- clock speed of input signal
- settling time of converter

When the input changes rapidly, the DAC conversion speed must be high.

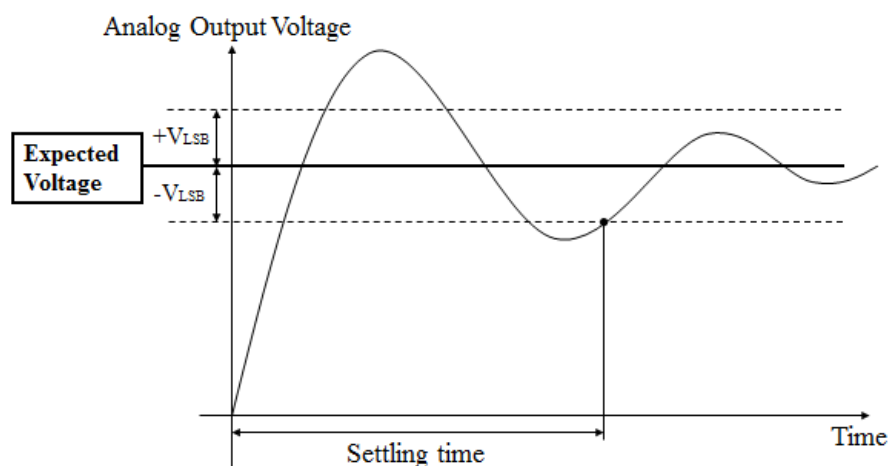
Linearity is the difference between the desired analog output and the actual output over the full range of expected values.

Ideally, a DAC should produce a linear relationship between a digital input and the analog output; this is not always the case.



Settling Time The time required for the input signal voltage to settle to the expected output voltage (within $\pm V_{LSB}$).

Any change in the input state will not be reflected in the output state immediately. There is a time lag, between the two events.



Reference Voltages used to determine how each digital input will be assigned to each voltage division.

Types:

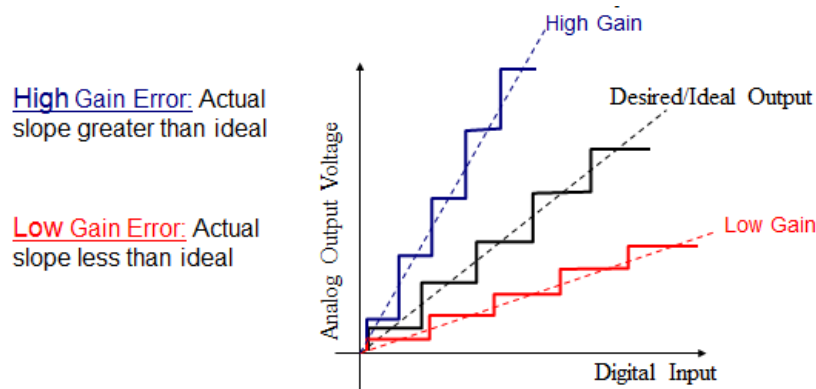
- Non-multiplier DAC: V_{ref} is fixed (internal, fixed, and defined by manufacturer).
- Multiplier DAC: V_{ref} provided by external source (external, variable, user specified).

Errors

Types of Errors Associated with DACs

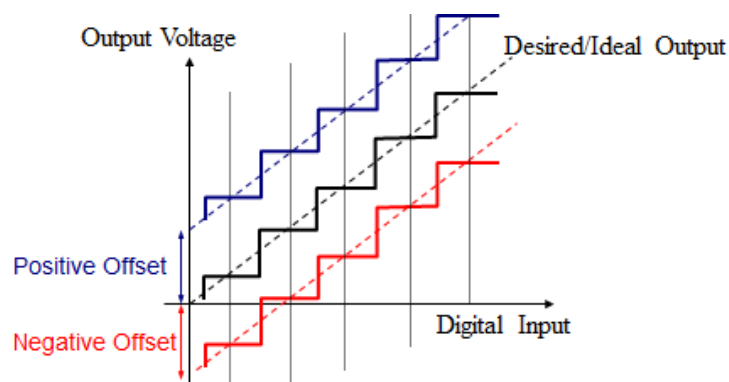
- Gain
- Offset
- Full Scale
- Resolution
- Non-Linearity
- Non-Monotonic

Gain Error: Difference in slope of the ideal curve and the actual DAC output.

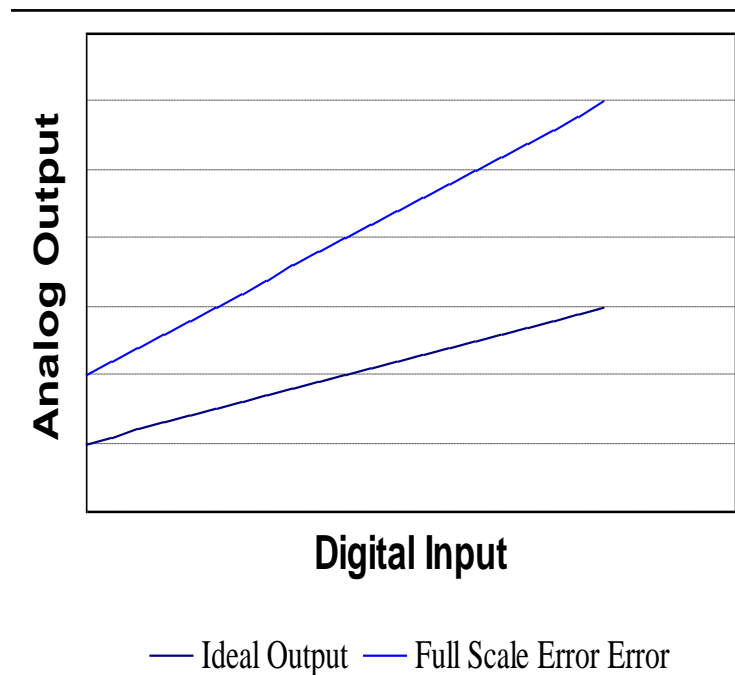


Offset Error: A constant voltage difference between the ideal DAC output and the actual.

- The voltage axis intercept of the DAC output curve is different than the ideal.

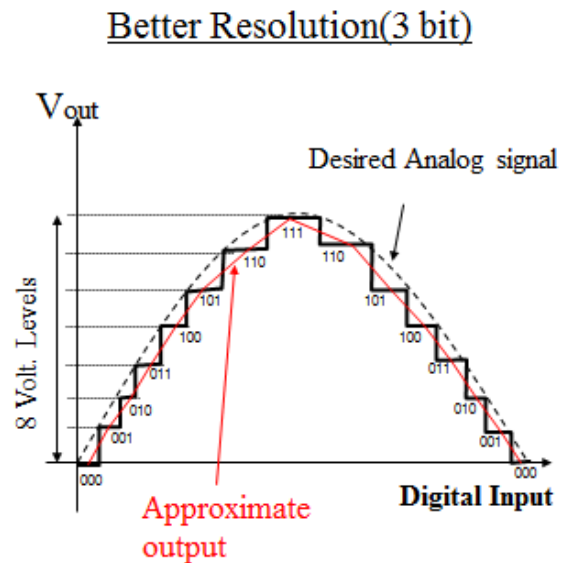
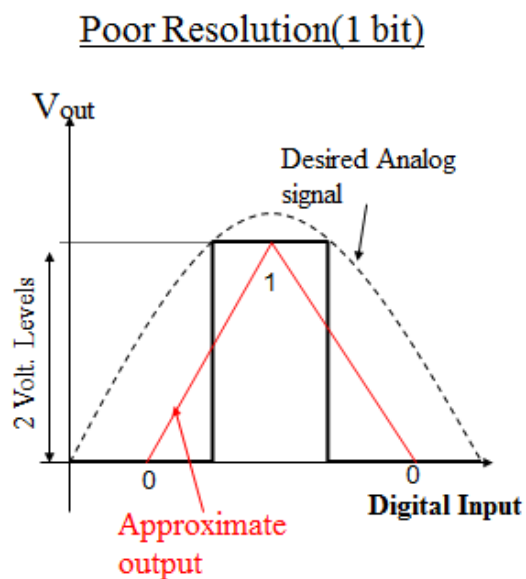


Full Scale Error: Occurs when the actual signal has both gain and offset errors.



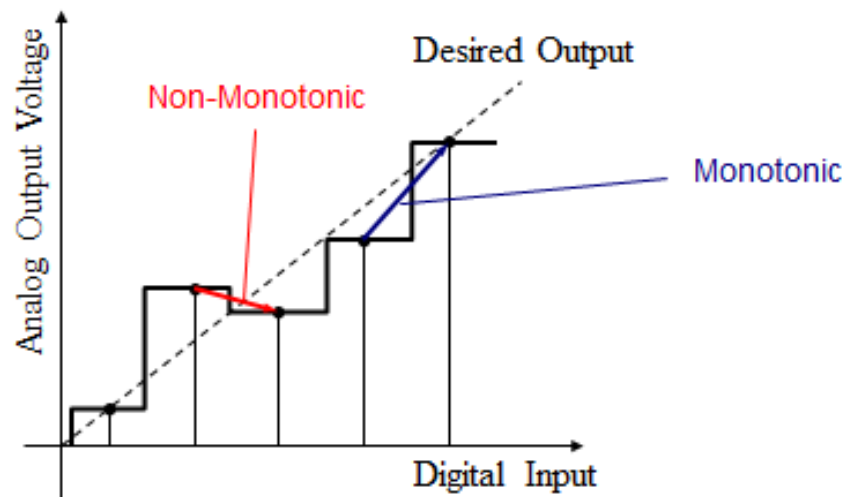
Resolution Error: Poor representation of ideal output due to poor resolution.

Size of voltage divisions affects the resolution



Non-Linearity Error: Occurs when analog output of signal is non-linear.

Non-Monotonic: A decrease in output voltage with an increase in the digital input.



Applications of DACs:

- Function Generators/Oscilloscopes.
- Digital Motor Control.
- Computer Printers.
- Sound Equipment (e.g. CD/MP3 Players, etc.).
- Electronic Cruise Control.
- Digital Thermostat.