# Chapter 5 : Small scale multipath propagation

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# Chapter 5

### **5.1 Small-scale fading**

**Small-scale fading:** is used to describe the rapid fluctuations of the amplitude of a radio signal over a short period of time or travel distance.

- Fading is caused by interference between *two or more versions of the transmitted signal* which arrive at the receiver at slightly different times.
- These waves are called *multipath waves*, combine at the receiver antenna to give a resultant signal which can vary widely in amplitude and phase, depending on the distribution of the intensity and relative propagation time of waves and the bandwidth of the transmitted signal.

### **5.2 Small-scale fading effects:**

- 1. Rapid changes in signal strength over a small travel distance or time interval.
- 2. Random frequency modulation due to varying Doppler shifts on different multipath signals.
- 3. Time dispersion caused by multipath propagation delays.

# 5.3 Factors influencing (causes of) small-scale fading:

- **Multipath propagation:** reflecting objects and scatters create a changing environment that affects the signal in amplitude, phase and time.
- **Speed of the mobile:** the relative motion between the mobile and the BS causes Doppler shifts, on each of the multipath components.
- Speed of surrounding objects: moving objects cause time-varying Doppler shifts.
- **Transmission bandwidth of the signal:** if the transmitted signal bandwidth is greater than the bandwidth of the channel, the signal will be distorted.

**Coherent bandwidth** of the <u>channel</u> is a measure of the frequency difference for which the signal is not distorted in amplitude (the channel does not distort the signal).

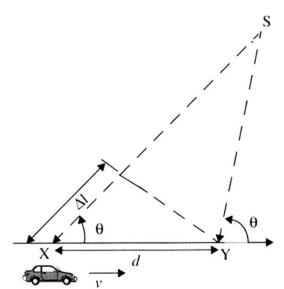
# 5.4 Doppler shift

Consider a mobile terminal moving at a constant velocity v, along a path segment having length d between points X and Y, while it receives signal from a remote source S.

The path length difference between S and points *X* and *Y*:

$$\Delta l = d\cos\theta = v\Delta t\cos\theta$$

where  $\Delta t$  is the time required for the mobile to travel from X to Y.



• The phase change in the received signal

$$\Delta \emptyset = \frac{2\pi \Delta l}{\lambda} = \frac{2\pi v \Delta t}{\lambda} \cos \theta$$

• The Doppler shift can be calculated using

$$f_D = \frac{1}{2\pi} \frac{\Delta \emptyset}{\Delta t} = \frac{v}{\lambda} \cos \theta$$

# ■ The Doppler shift depends on:

- 1. Mobile velocity
- 2. Carrier frequency
- 3. Angle between the direction of motion and the direction of arrival of the wave

- ➤ Doppler shift is *positive* if the mobile is moving *towards* the source.
- > Doppler shift is *negative* if the mobile is moving *away* from the source.

### Example:

Consider a transmitter which radiates a sinusoidal carrier frequency of 1850 MHz. For a vehicle moving at 96.6 km/h, compute the received carrier frequency if the mobile is moving

- a) Directly towards the transmitter,
- b) Directly away from the transmitter,
- c) In a direction which is perpendicular to the direction of arrival of the transmitted signal.

#### Solution:

Given:

$$f = 1850 \text{ MHz},$$
  
 $v = 96.6 \text{ km/h} = 96.6 \times (1000 / 3600) = 26.82 \text{ m/s}$   
 $\lambda = c / f = 3 \times 10^8 / 1850 \times 10^6 = 0.162 \text{m}$ 

(a)

The vehicle is moving directly towards the transmitter, meaning that  $\theta = 0^{\circ}$ .

The Doppler shift in this case is positive.

Doppler frequency 
$$f_D = \frac{v}{\lambda}\cos\theta = \frac{26.82}{0.162}\cos(0) = 165 Hz$$

The received frequency =  $f + f_D = 1850 \times 10^6 + 165 = 1850.000165 MHz$ 

(b)

The vehicle is moving directly away from the transmitter, meaning that  $\theta = 180^{\circ}$ .

The Doppler shift in this case is negative.

Doppler frequency 
$$f_D = \frac{v}{\lambda}\cos\theta = \frac{26.82}{0.162}\cos(180) = -165Hz$$

The received frequency =  $f + f_D = 1850 \times 10^6 - 165 = 1849.999834 MHz$ 

(c)

The vehicle is moving perpendicular to the angle of arrival of the transmitted signal, meaning that  $\theta = 90^{\circ}$ .

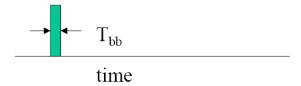
Doppler frequency 
$$f_D = \frac{v}{\lambda}\cos\theta = \frac{26.82}{0.162}\cos(90) = 0$$
 Hz

There is no Doppler shift.

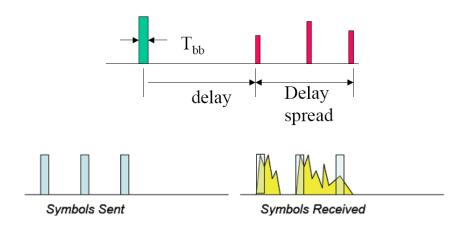
The received signal frequency is the same as the transmitted frequency (f = 1850 MHz).

## 5.5 Determining the impulse response of a channel

- Transmit a narrowband pulse into the channel



- Measure replicas of the pulse that traverse different paths between transmitter and receiver



- A mobile radio channel may be modeled as a linear filter with a time-varying impulse response
- The time variation is due to receiver motion in space
- The filtering is caused by the summation of amplitudes and delays of multiple arriving waves, due to multipath