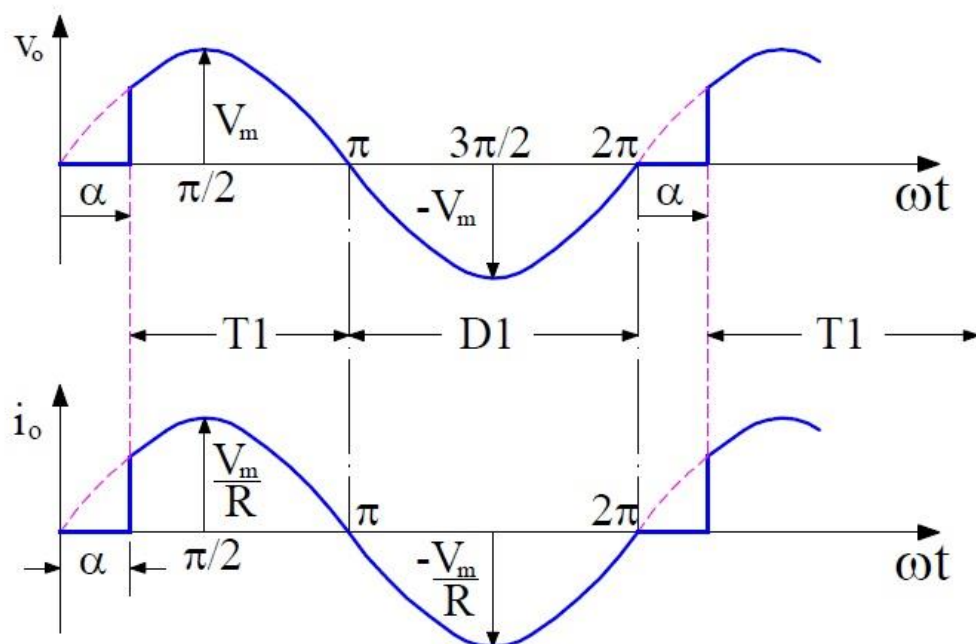
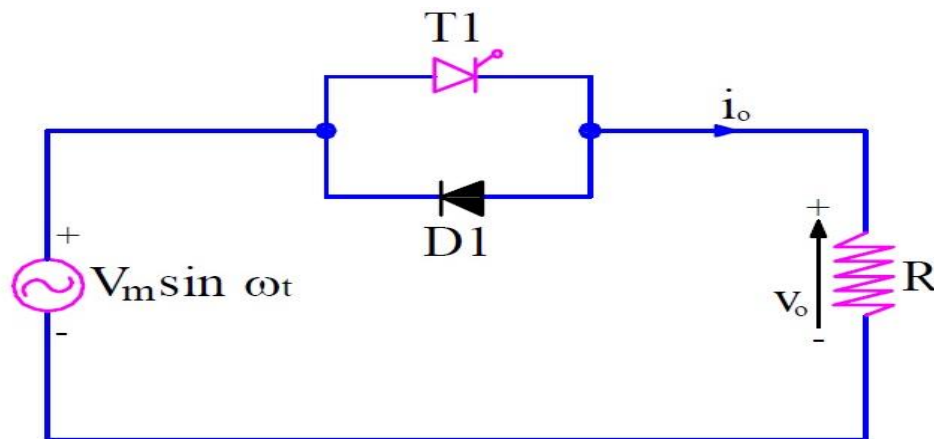


## AC TO AC CONVERTER

### SINGLE PHASE CONTROLLER ( PHASE CONTROL)

#### 1. UNIDIRECTIONAL CONTROLLER

A single phase half wave AC voltage controller comprises of a thyristor connected in anti-parallel with a power diode. The circuit diagram is shown in figure below.





if input voltage,  $v_s = V_m \sin \omega t = \sqrt{2} V_s \sin \omega t$   
delay angle of thyristor  $T_1$ ,  $\omega t = \alpha$

the rms output voltage,

$$\begin{aligned} V_o &= \left\{ \frac{1}{2\pi} \left[ \int_{\alpha}^{\pi} 2V_s^2 \sin^2 \omega t \, d(\omega t) + \int_{\pi}^{2\pi} 2V_s^2 \sin^2 \omega t \, d(\omega t) \right] \right\}^{1/2} \\ &= \left\{ \frac{2V_s^2}{4\pi} \left[ \int_{\alpha}^{\pi} (1 - \cos 2\omega t) \, d(\omega t) + \int_{\pi}^{2\pi} (1 - \cos 2\omega t) \, d(\omega t) \right] \right\}^{1/2} \\ &= V_s \left[ \frac{1}{2\pi} \left( 2\pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} \end{aligned}$$

the average value of output voltage,

$$\begin{aligned} V_{dc} &= \frac{1}{2\pi} \left[ \int_{\alpha}^{\pi} \sqrt{2} V_s \sin \omega t \, d(\omega t) + \int_{\pi}^{2\pi} \sqrt{2} V_s \sin \omega t \, d(\omega t) \right] \\ &= \frac{\sqrt{2} V_s}{2\pi} (\cos \alpha - 1) \end{aligned}$$

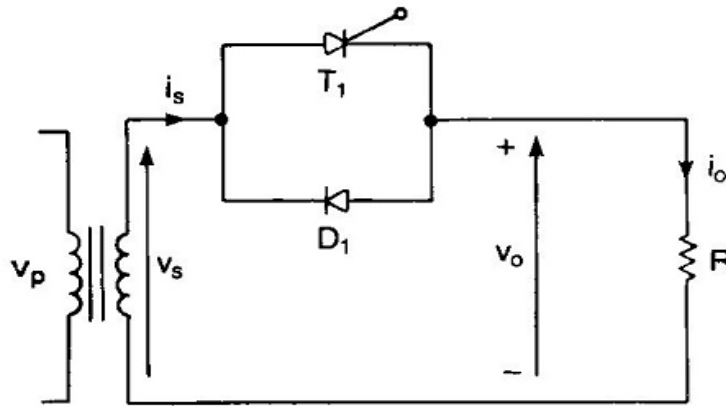
$$\text{If, } \alpha = 0 \rightarrow \pi : V_o = V_s \rightarrow \frac{V_s}{\sqrt{2}}, \quad V_{dc} = 0 \rightarrow \frac{-\sqrt{2} V_s}{\pi}$$

### EXAMPLE 1:-

A single-phase ac voltage controller in figure has a resistive load of  $R=10\Omega$  and the input voltage is  $V_s=120\text{V}$ , 60Hz.

The delay angle of thyristor  $T_1$  is  $\alpha=\pi/2$ . Determine,

- The rms value of output voltage  $V_o$
- The input power factor  $PF$
- The average input current



$$R = 10\Omega, V_s = 120\text{ V}, V_m = \sqrt{2} \times 120 = 169.7\text{ V}, \alpha = \frac{\pi}{2}$$

(a) the rms value of output voltage,

$$V_o = V_s \left[ \frac{1}{2\pi} \left( 2\pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} = 120 \sqrt{\frac{3}{4}} = 103.92\text{ V}$$

(b) the rms load current,

$$I_o = \frac{V_o}{R} = \frac{103.92}{10} = 10.392\text{ A}$$

$$\text{the load power, } P_o = I_o^2 R = 10.392^2 \times 10 = 1079.94\text{ W}$$

$$VA = V_s I_s = V_s I_o = 120 \times 10.392 = 1247.04\text{ VA}$$

the input power factor,

$$PF = \frac{P_o}{VA} = \frac{V_o}{V_s} = \left[ \frac{1}{2\pi} \left( 2\pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} = \sqrt{\frac{3}{4}} = \frac{1079.94}{1247.04} \\ = 0.866 \text{ (lagging)}$$



(c) *the average output voltage,*

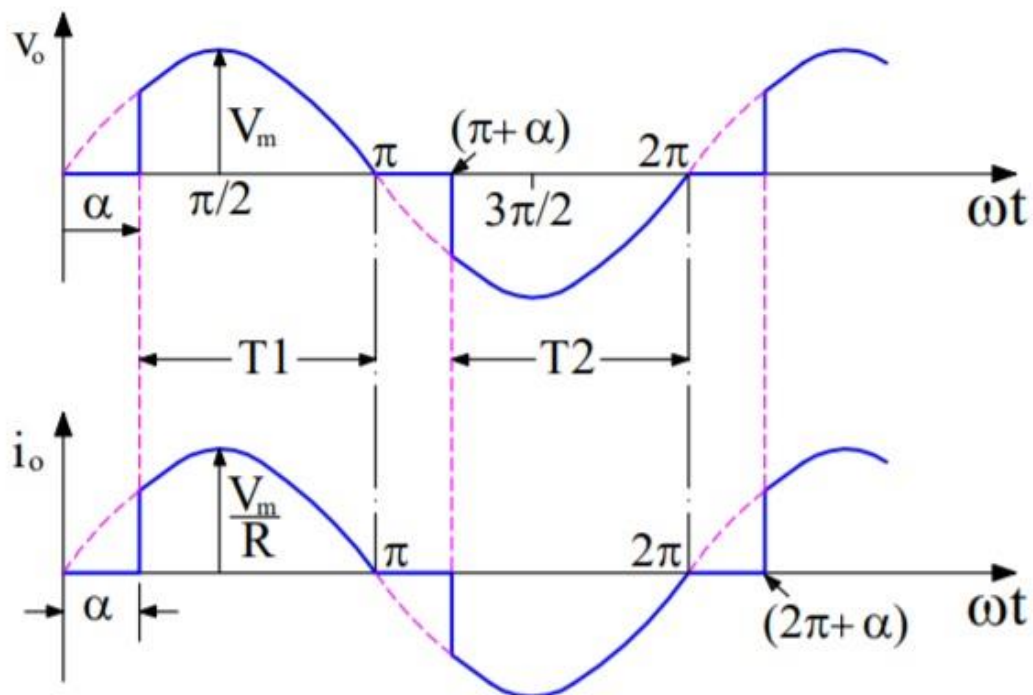
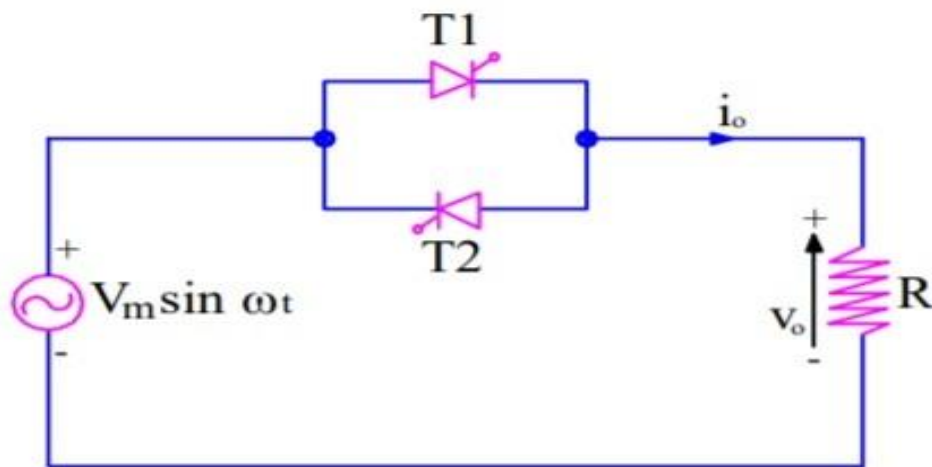
$$V_{dc} = \frac{\sqrt{2} V_s}{2\pi} (\cos \alpha - 1) = -120 \times \frac{\sqrt{2}}{2\pi} = -27 \text{ V}$$

*the average input current*

$$I_D = \frac{V_{dc}}{R} = -\frac{27}{10} = -2.7 \text{ A}$$

## 2. BIDIRECTIONAL CONTROLLER

A single phase full wave AC voltage controller comprises of two thyristor connected in anti-parallel. The circuit diagram is shown in figure below.



if input voltage,  $v_s = V_m \sin \omega t = \sqrt{2} V_s \sin \omega t$

delay angle of thyristor  $T_1$  and  $T_2$ ,  $\alpha_1 = \alpha_2 = \alpha$

the rms output voltage,

$$V_o = \left[ \frac{2}{2\pi} \int_{\alpha}^{\pi} 2V_s^2 \sin^2 \omega t \, d(\omega t) \right]^{1/2} = \left[ \frac{4V_s^2}{4\pi} \int_{\alpha}^{\pi} (1 - \cos 2\omega t) \, d(\omega t) \right]^{1/2}$$

$$= V_s \left[ \frac{1}{\pi} \left( \pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2}$$

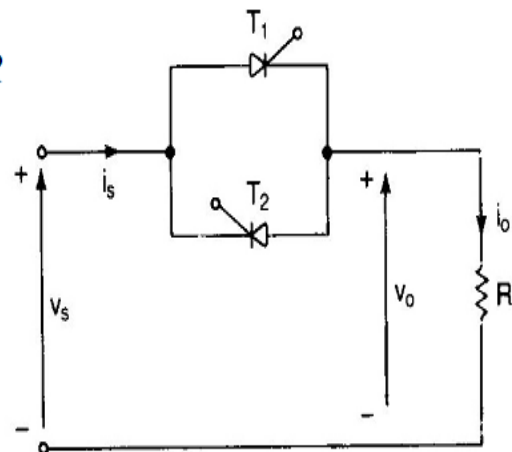
If,  $\alpha = 0 \rightarrow \pi : V_o = V_s \rightarrow 0$

### EXAMPLE 2:-

A single-phase full-wave ac voltage controller in figure has a resistive load of  $R=10\Omega$  and the input voltage is  $V_s=120V(\text{rms})$ , 60Hz. The delay angle of thyristors  $T_1$  and  $T_2$  are equal :

$\alpha_1 = \alpha_2 = \pi/2$ . Determine,

- The rms output voltage  $V_o$
- The input power factor  $PF$
- The average current of thyristors  $I_A$
- The rms current of thyristors  $I_R$





$$R = 10\Omega, V_s = 120\text{ V}, V_m = \sqrt{2} \times 120 = 169.7\text{ V}, \alpha = \frac{\pi}{2}$$

(a) the rms value of output voltage,

$$V_o = V_s \left[ \frac{1}{\pi} \left( \pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} = \frac{120}{\sqrt{2}} = 84.85\text{ V}$$

(b) the rms load current,

$$I_o = \frac{V_o}{R} = \frac{84.85}{10} = 8.485\text{ A}$$

$$\text{the load power, } P_o = I_o^2 R = 8.485^2 \times 10 = 719.95\text{ W}$$

$$VA = V_s I_s = V_s I_o = 120 \times 8.485 = 1018.2\text{ W}$$

the input power factor,

$$PF = \frac{P_o}{VA} = \frac{V_o}{V_s} = \left[ \frac{1}{\pi} \left( \pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} = \frac{1}{\sqrt{2}} = \frac{719.95}{1018.2} \\ = 0.707 \text{ (lagging)}$$

(c) the average thyristor current,

$$I_A = \frac{1}{2\pi R} \int_{\alpha}^{\pi} \sqrt{2} V_s \sin \omega t \, d(\omega t) = \frac{\sqrt{2} V_s}{2\pi R} (\cos \alpha + 1) \\ = \sqrt{2} \times \frac{120}{2\pi \times 10} = 2.7\text{ A}$$



(d) the rms value of the thyristor current ,

$$\begin{aligned} I_R &= \left[ \frac{1}{2\pi R^2} \int_{\alpha}^{\pi} 2V_s^2 \sin^2 \omega t \, d(\omega t) \right]^{1/2} \\ &= \left[ \frac{V_s}{4\pi R^2} \int_{\alpha}^{\pi} (1 - \cos 2\omega t) \, d(\omega t) \right]^{1/2} \\ &= \frac{V_s}{\sqrt{2} R} \left[ \frac{1}{\pi} (\pi - \alpha + \frac{\sin 2\alpha}{2}) \right]^{1/2} \\ &= \frac{120}{2 \times 10} = 6 \text{ A} \end{aligned}$$

### EXAMPLE 3:-

The single-phase ac voltage controller bidirectional has a 120-V rms 60-Hz source. The load resistance is 15  $\Omega$ . Determine (a) the delay angle required to deliver 500 W to the load, (b) the rms source current, (c) the rms and average currents in the thyristor, (d) the power factor.

### EXAMPLE 4:-

The load of an ac voltage controller is resistive, with  $R = 1.2 \Omega$ . The input voltage is  $V_s = 120 \text{ V (rms)}$ , 60 Hz. Plot the PF against the delay angle for single-phase half-wave and full-wave controllers.