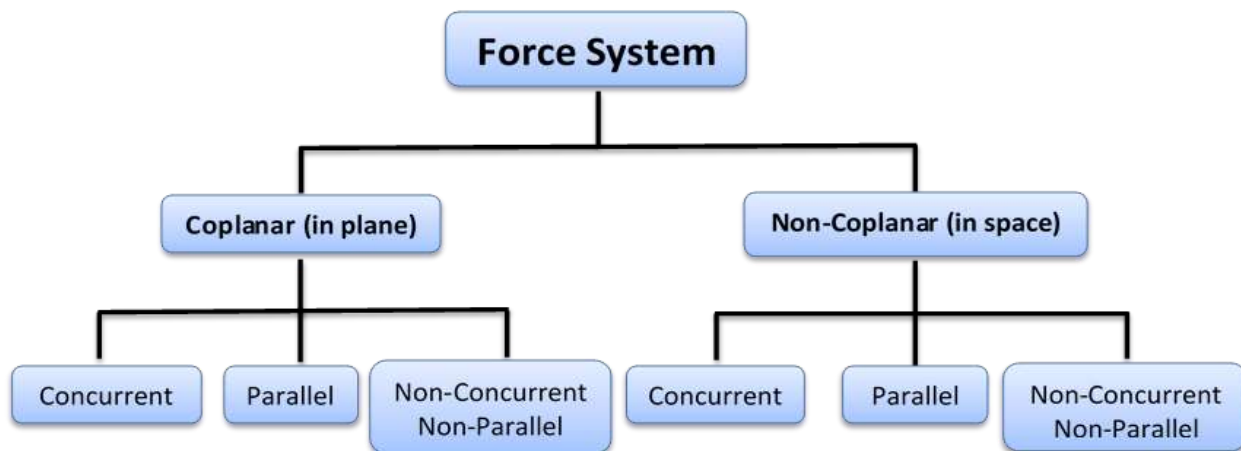
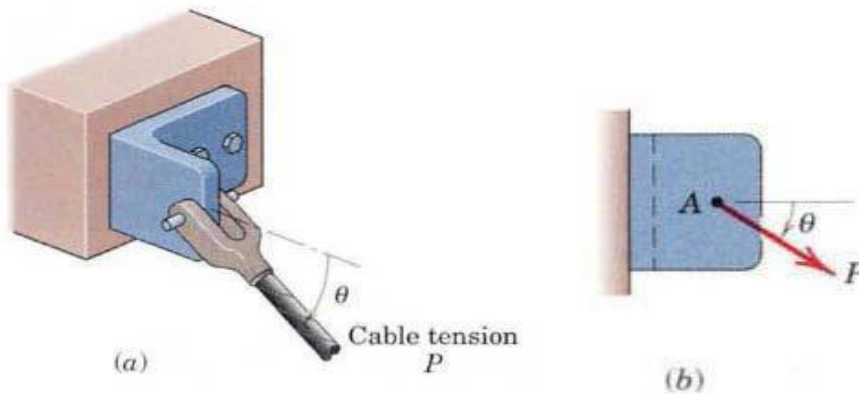


Force Systems

Before dealing with a group or *system* of forces, it is necessary to examine the properties of a single force in some detail. The action of the cable tension on the bracket in Fig. 1a is represented in the side view, Fig. 1b, by the force vector P of magnitude P . The effect of this action on the bracket depends on P , the angle θ , and the location of the point of application A

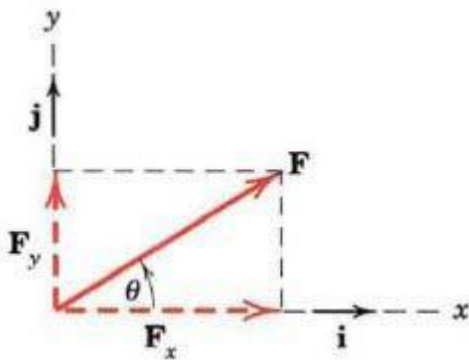




TWO-DIMENSIONAL FORCE SYSTEMS

RECTANGULAR COMPONENTS

The most common two-dimensional resolution of a force vector is into rectangular components. It follows from the parallelogram rule that the vector F of Fig. may be written as

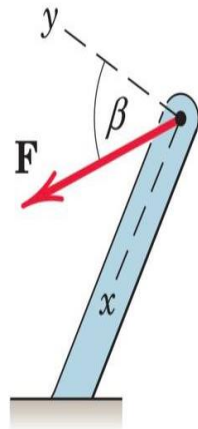


The scalar components can be positive or negative, depending on the quadrant into which F points.

$$F_x = F \cos \theta \quad F = \sqrt{F_x^2 + F_y^2}$$

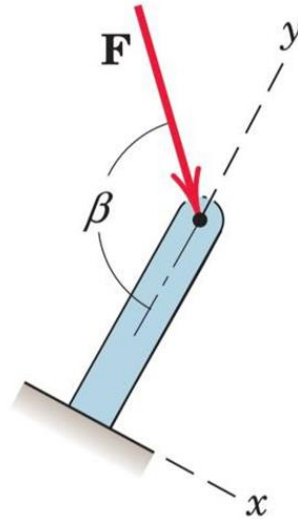
$$F_y = F \sin \theta \quad \theta = \tan^{-1} \frac{F_y}{F_x}$$

Determining the Components of a Force Dimensions are not always given in horizontal and vertical directions, angles need not be measured counterclockwise from the x-axis, and the origin of coordinates need not be on the line of action of a force



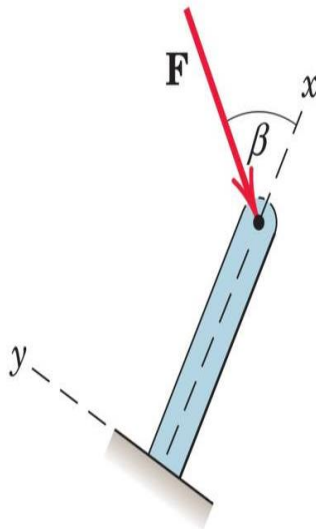
$$F_x = F \sin \beta$$

$$F_y = F \cos \beta$$



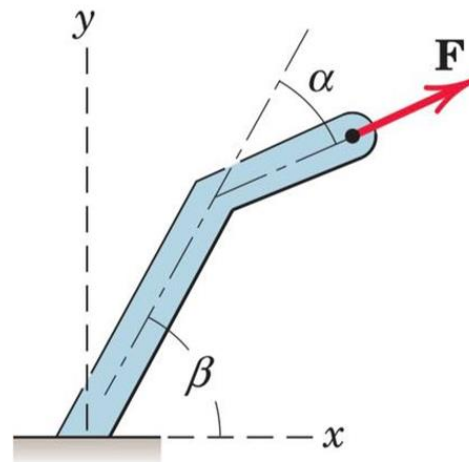
$$F_x = F \sin (\pi - \beta)$$

$$F_y = -F \cos (\pi - \beta)$$



$$F_x = -F \cos \beta$$

$$F_y = -F \sin \beta$$



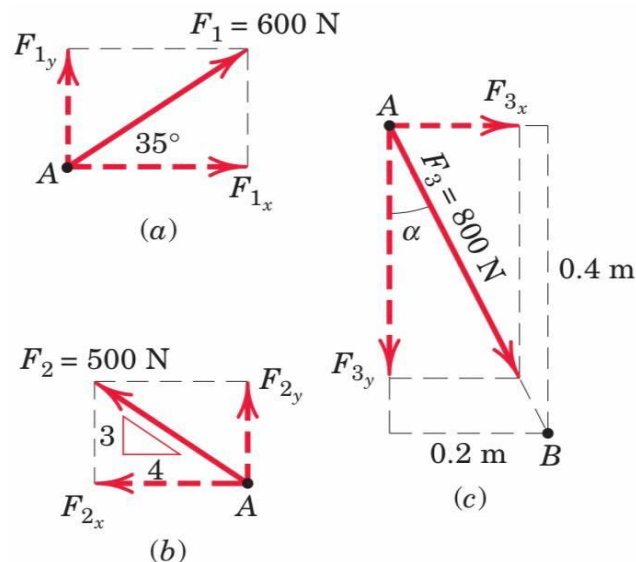
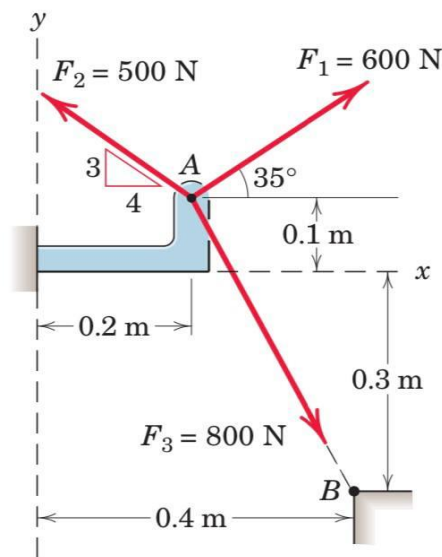
$$F_x = F \cos (\beta - \alpha)$$

$$F_y = F \sin (\beta - \alpha)$$



Problem 1

The forces F_1 , F_2 , and F_3 all of which act on point A of the bracket, are specified in three different ways. Determine the x and y scalar components of each of the three forces.





Solution:

The scalar components of F_1 from Fig. a, are

$$F_{1x} = 600 \cos 35^\circ = 491 \text{ N}$$

$$F_{1y} = 600 \sin 35^\circ = 344 \text{ N}$$

The scalar components of F_2 from Fig. b, are

$$F_{2x} = -500(4/5) = -400 \text{ N}$$

$$F_{2y} = 500(3/5) = 300 \text{ N}$$

$$\alpha = \tan^{-1} [0.2/0.4]$$

$$= 26.6^\circ$$

Then

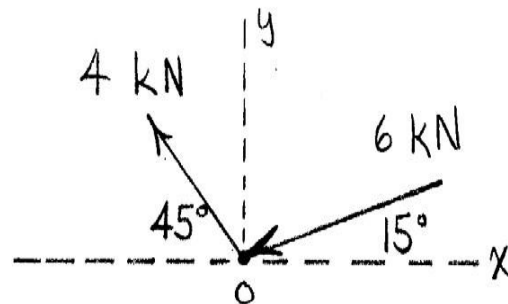
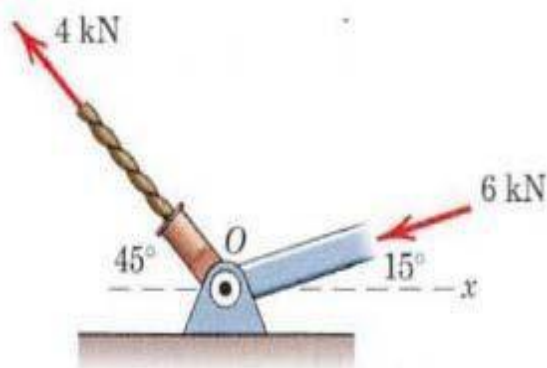
$$F_{3x} = F_3 \sin \alpha = 800 \sin 26.6^\circ = 358 \text{ N}$$

$$F_{3y} = -F_3 \cos \alpha = -800 \cos 26.6^\circ = -716 \text{ N}$$



Problem 2

The two structural members, one of which is in tension and the other in compression, exert the indicated forces on joint O. Determine the magnitude of the resultant R of the two forces and the angle θ which R makes with the positive. xaxis.



Solution:

$$R_x = F_x = -4 \cos 45^\circ - 6 \cos 15^\circ = -8.62 \text{ N}$$

$$R_y = F_y = 4 \sin 45^\circ - 6 \sin 15^\circ = 1.276 \text{ N}$$

$$R = \sqrt{R_x^2 + R_y^2}$$

$$= 8.72 \text{ KN}$$

$$\alpha = \tan^{-1} [R_x / R_y]$$

$$= 171.6^\circ$$