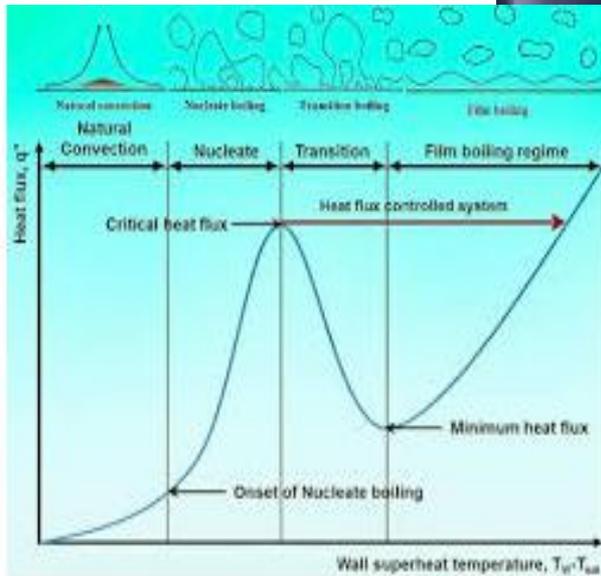


Boiling

Prof. Dr. Majid



Boiling

- **pool boiling** is the boiling of stationary fluids. In pool boiling, the fluid is not forced to flow by a mover such as a pump, and any motion of the fluid is due to natural convection currents and the motion of the bubbles under the influence of buoyancy. As a familiar example of pool boiling, consider the boiling of tap water in a pan on top of a stove. The water is initially at about 15°C , far below the saturation temperature of 100°C at standard atmospheric pressure

• Boiling Regimes and the Boiling Curve

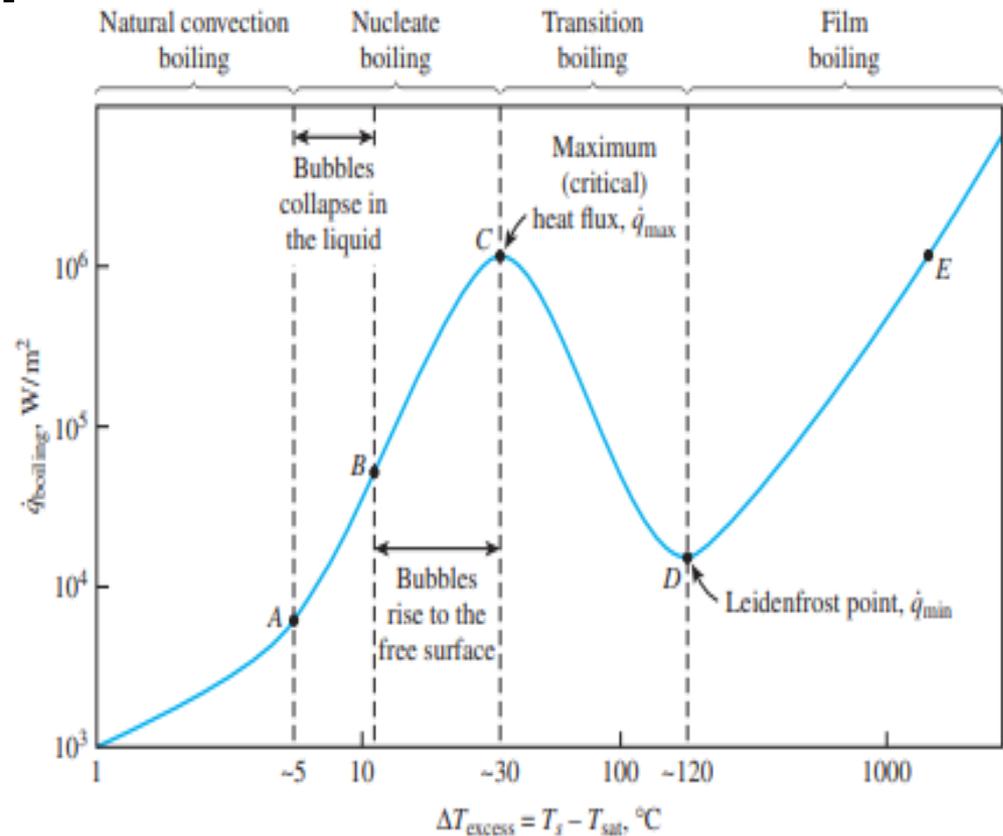
-A natural convection until boiling

A-C nucleate boiling

**Transition Boiling
(between Points C
and D)**

Film Boiling

(beyond Point D)



Heat Transfer Correlations in Pool Boiling

For Nucleate Boiling

Nucleate boiling regime is between ($5^{\circ}C \leq \Delta T_{excess} \leq 30^{\circ}C$)

$$\dot{q}_{nucleate} = \mu_f h_{fg} \left[\frac{g(\rho_f - \rho_v)}{\sigma} \right]^{1/2} \left[\frac{Cp_f(T_w - T_{sat})}{C_{sf} h_{fg} Pr_f^n} \right]^3$$

Where $\dot{q}_{nucleate}$ = nucleate boiling heat flux W/m^2

μ_f = viscosity of liquid $kg/m \cdot sec$, h_{fg} = enthalpy of evaporation J/kg

ρ_f, ρ_v = density of liquid and vapor respectively in kg/m^3

σ = surface tension of liquid-vapor interface N/m

cp_f = specific heat of liquid $J/kg \cdot ^{\circ}C$, T_w = surface temperature of heater $^{\circ}C$

T_{sat} = saturation temperature of fluid $^{\circ}C$, Pr_f = Prandtl Number of liquid

C_{sf} = experimental constant that depends on surface-fluid compensation

n = experimental constant that depends on the fluid, $n=1$ for water and 1.7 for other liquids.

• Peak Heat Flux

- The maximum (or critical) heat flux in nucleate pool boiling was determined theoretically by S. S. Kutateladze in Russia in 1948 and N. Zuber in the United States in 1958 using quite different approaches, and is expressed as

- $$\dot{q}_{max} = C_{cr} h_{fg} \rho_v \left[\frac{\sigma g (\rho_f - \rho_v)}{\rho_v^2} \right]^{1/4} \quad (2)$$

- Where $C_{cr} = \text{constant}$ whose value depend on heater geometry
- $C_{cr} = 0.131$ for large horizontal cylinders and sphere
- $C_{cr} = 0.149$ for large horizontal plate

• Minimum Heat Flux

- Zuber [10] used stability theory to derive the following expression for the minimum heat flux .

- $$\dot{q}_{min} = 0.09 \rho_v h_{fg} \left[\frac{\sigma g (\rho_f - \rho_v)}{(\rho_f + \rho_v)^2} \right]^{1/4} \quad (3)$$

Film Boiling The Nusult number for film boiling on a horizontal cylinder or sphere of diameter D is given by

$$\overline{Nu}_D = \frac{\bar{h}D}{k_v} = C \left[\frac{g\rho_v(\rho_f - \rho_v)h'_{fg}}{\mu_f} \right]^{1/4} \quad (4)$$

Where k_v is the thermal conductivity of the vapor in W/m.K and

$$C = \begin{cases} 0.62 & \text{for horizontal cylinder} \\ 0.67 & \text{for spheres} \end{cases}$$

In film boiling the heat transfer by radiation is be considered

$$q_{film} = \bar{h}(T_w - T_{sat}) \quad (5)$$

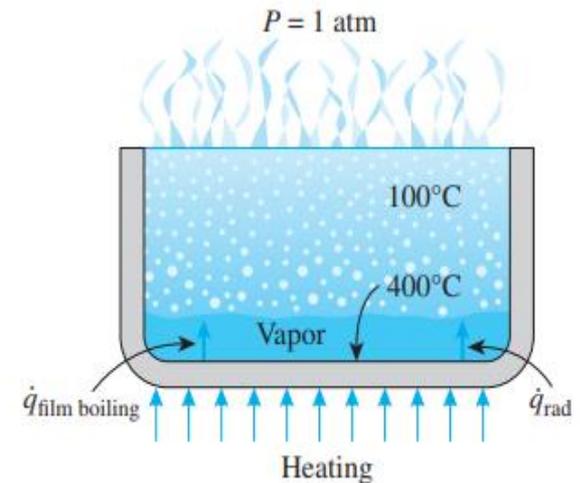
$$\dot{q}_{rad} = \varepsilon\sigma(T_w^4 - T_{sat}^4) \quad (6)$$

Where ε is emissivity of the heating surface

And $\sigma = 5.67 \times 10^{-8} W/m^2 K^4$

And temperature here in K not $^{\circ} C$

$$\dot{q}_{tot} = \dot{q}_{film} + \frac{3}{4}\dot{q}_{rad} \quad (7)$$



Values of the coefficient C_{sf} and n for various fluid–surface combinations

Surface tension of liquid–vapor interface for water		Fluid–Heating Surface Combination	C_{sf}	n
$T, ^\circ\text{C}$	$\sigma, \text{N/m}^*$	Water–copper (polished)	0.0130	1.0
0	0.0757	Water–copper (scored)	0.0068	1.0
20	0.0727	Water–stainless steel (mechanically polished)	0.0130	1.0
40	0.0696	Water–stainless steel (ground and polished)	0.0060	1.0
60	0.0662	Water–stainless steel (teflon pitted)	0.0058	1.0
80	0.0627	Water–stainless steel (chemically etched)	0.0130	1.0
100	0.0589	Water–brass	0.0060	1.0
120	0.0550	Water–nickel	0.0060	1.0
140	0.0509	Water–platinum	0.0130	1.0
160	0.0466	<i>n</i> -Pentane–copper (polished)	0.0154	1.7
180	0.0422	<i>n</i> -Pentane–chromium	0.0150	1.7
200	0.0377	Benzene–chromium	0.1010	1.7
220	0.0331	Ethyl alcohol–chromium	0.0027	1.7
240	0.0284	Carbon tetrachloride–copper	0.0130	1.7
260	0.0237	Isopropanol–copper	0.0025	1.7
280	0.0190	Values of the coefficient C_{cf} for use in Eq. 10–3 for maximum heat flux (dimensionless parameter $L^* = L[g(\rho_l - \rho_v)/\sigma]^{1/2}$)		
300	0.0144	Heater Geometry	C_{cf}	Charac. Dimension of Heater, L
320	0.0099	Large horizontal flat heater	0.149	Width or diameter
340	0.0056	Small horizontal flat heater ¹	$18.9K_1$	Width or diameter
360	0.0019	Large horizontal cylinder	0.12	Radius
374	0.0	Small horizontal cylinder	$0.12L^{*-0.25}$	Radius
		Large sphere	0.11	Radius
		Small sphere	$0.227L^{*-0.5}$	Radius
				Range of L^*
				$L^* > 27$
				$9 < L^* < 20$
				$L^* > 1.2$
				$0.15 < L^* < 1.2$
				$L^* > 4.26$
				$0.15 < L^* < 4.26$

$$^1K_1 = \sigma/[g(\rho_l - \rho_v)A_{\text{heater}}]$$

Surface tension of some fluids (from Suryanarayana, 1995, originally based on data from Jasper, 1972)

Substance and Temp. Range	Surface Tension, $\sigma, \text{N/m}^*$ (T in $^\circ\text{C}$)
Ammonia, -75 to -40°C :	$0.0264 + 0.000223T$
Benzene, 10 to 80°C :	$0.0315 - 0.000129T$
Butane, -70 to -20°C :	$0.0149 - 0.000121T$
Carbon dioxide, -30 to -20°C :	$0.0043 - 0.000160T$
Ethyl alcohol, 10 to 70°C :	$0.0241 - 0.000083T$
Mercury, 5 to 200°C :	$0.4906 - 0.000205T$
Methyl alcohol, 10 to 60°C :	$0.0240 - 0.000077T$
Pentane, 10 to 30°C :	$0.0183 - 0.000110T$
Propane, -90 to -10°C :	$0.0092 - 0.000087T$

Example.1 The bottom of a copper pan, 150 mm in diameter, is maintained at 115°C by the heating element of an electric range. Estimate the power required to boil the water in this pan. Determine the evaporation rate. What is the ratio of the surface heat flux to the critical heat flux? What pan temperature is required to achieve the critical heat flux?

Solution: $D=150\text{mm}=0.15\text{m}$ copper pan $T_w=115^\circ\text{C}$,
 $T_{\text{sat}}=100^\circ\text{C}$ at 1atm

Requirements: 1-Power required to boil the water, 2- evaporating rate, 3- ratio of surface heat flux to the critical heat flux. 4- the temperature required to achieve the critical heat flux.

- **Properties:** the properties of water at 100°C, $\rho_f=957.9\text{kg/m}^3$, $\rho_v=0.5978\text{kg/m}^3$, $h_{fg}=2257\text{kJ/kg}$, $cp_f=4217\text{J/kg.K}$, $k_f=0.679\text{W/m.K}$, $\mu_f=0.282 \times 10^{-3}\text{kg/m.sec}$, $Pr=1.75$, $C_{sf}=0.0128$, $n=1.0$, $\sigma=0.0589\text{N/m}$.

- **Analysis:** The heat flux for boiling is

$$\dot{q}_{nucleate} = \mu_f h_{fg} \left[\frac{g(\rho_f - \rho_v)}{\sigma} \right]^{1/2} \left[\frac{cp_f(T_w - T_{sat})}{C_{sf} h_{fg} Pr_f^n} \right]^3$$

$$\begin{aligned} \dot{q}_{nucleate} &= 0.282 \times 10^{-3} \times 2257 \\ &\times 10^3 \left[\frac{9.81(957.9 - 0.5978)}{0.0587} \right]^{1/2} \left[\frac{4217(115 - 100)}{0.0128 \times 2257 \times 10^3 \times 1.75^{1.0}} \right]^3 \\ &= 498616 \text{W/m}^2 \end{aligned}$$

- The heat of nucleation

- $$\dot{Q} = \frac{\pi}{4} D^2 \dot{q}_{nucleate} = \frac{\pi}{4} (0.15)^2 \times 498616$$

$$= 8811.28W$$

- Mass of water evaporation

- $$\dot{m}_s = \frac{\dot{Q}}{h_{fg}} = \frac{8811.28}{2257 \times 10^3} \times 3600 = 14.0kg/hr$$

- The maximum heat flux:

- $$\dot{q}_{max} = Ch_{fg}\rho_v \left[\frac{\sigma g(\rho_f - \rho_v)}{\rho_v^2} \right]^{1/4}$$
- $$\dot{q}_{max} = 0.149 \times 2257 \times 10^3$$

$$\times 0.5978 \left[\frac{0.0589 \times 9.81(957.9 - 0.5978)}{(0.5978)^2} \right]^{1/4} = 1260.968kW$$

$$/m^2$$

- $$\frac{\dot{q}_{nucleate}}{\dot{q}_{max}} = \frac{498616}{1260968.1} = 0.395$$

- For maximum heat flux \dot{q}_{max}

$$= \mu_f h_{fg} \left[\frac{g(\rho_f - \rho_v)}{\sigma} \right]^{1/2} \left[\frac{c p_f (T_w - T_{sat})}{C_{sf} h_{fg} Pr_f^n} \right]^3$$
- $\dot{q}_{nucleate} = 0.282 \times 10^{-3} \times 2257$

$$\times 10^3 \left[\frac{9.81(957.9 - 0.5978)}{0.0587} \right]^{1/2} \left[\frac{4217(T_w - T_{sat})}{0.0128 \times 2257 \times 10^3 \cdot 1.75^{1.0}} \right]^3$$

$$= 1260968.1$$
- $\Delta T_e = 20.43^\circ C$