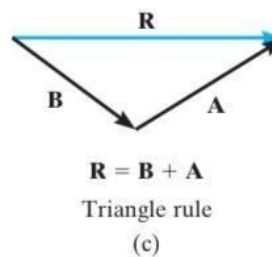
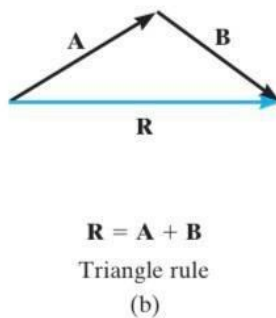
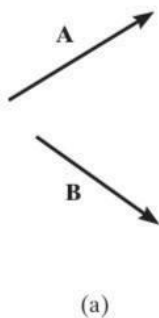
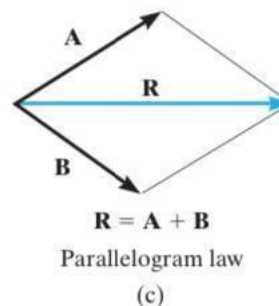
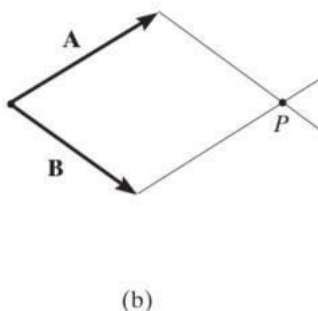
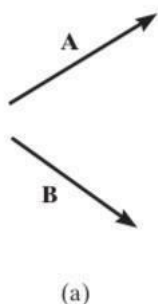




Vector Addition of Forces

Experimental evidence has shown that a force is a vector quantity since it has a specified magnitude, direction, and sense and it adds according to the parallelogram law. Two common problems in statics involve either finding the resultant force, knowing its components, or resolving a known force into two components. We will now describe how each of these problems is solved using the parallelogram law.





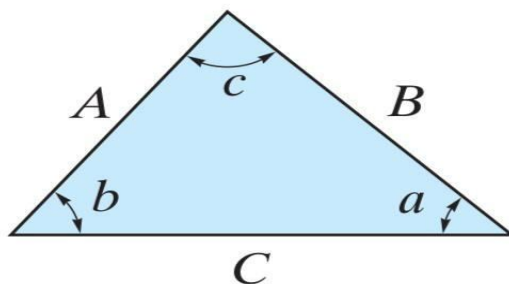
Class: 1st
2024- 2025
Subject: Mechanical Engineering
ASST .LEC. Teeb Basim Abbas



Trigonometry.

- Redraw a half portion of the parallelogram to illustrate the triangular head-to-tail addition of the components.

From this triangle, the magnitude of the resultant force can be determined using the law of cosines, and its direction is determined from the law of sines. The magnitudes of two force components are determined from the law of sines.



Cosine law:

$$C = \sqrt{A^2 + B^2 - 2AB \cos c}$$

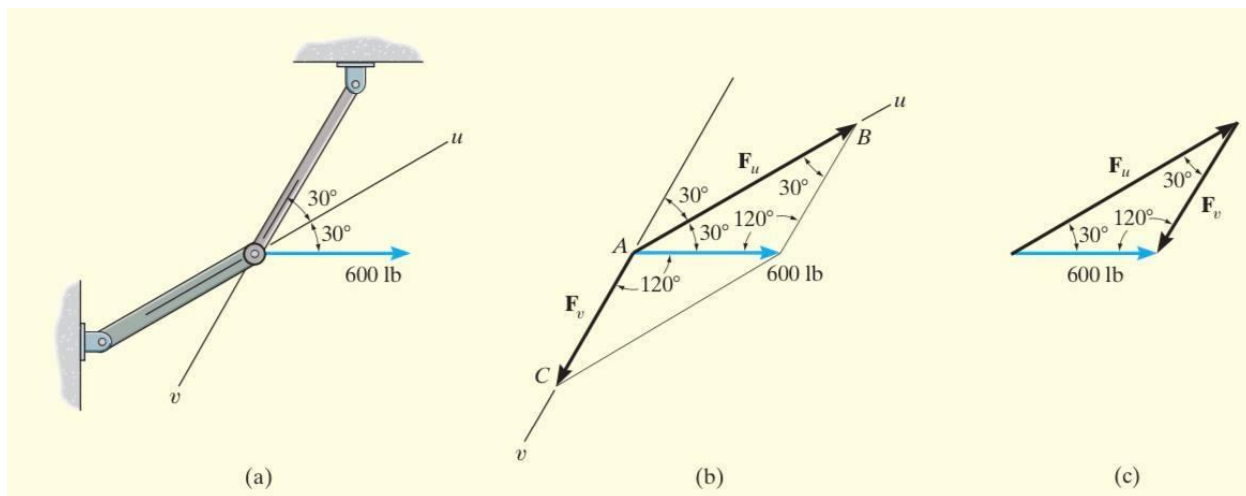
Sine law:

$$\frac{A}{\sin a} = \frac{B}{\sin b} = \frac{C}{\sin c}$$



Example 1

Resolve the horizontal 600-lb force in Fig, into components acting along the u and v axes and determine the magnitudes of these components.



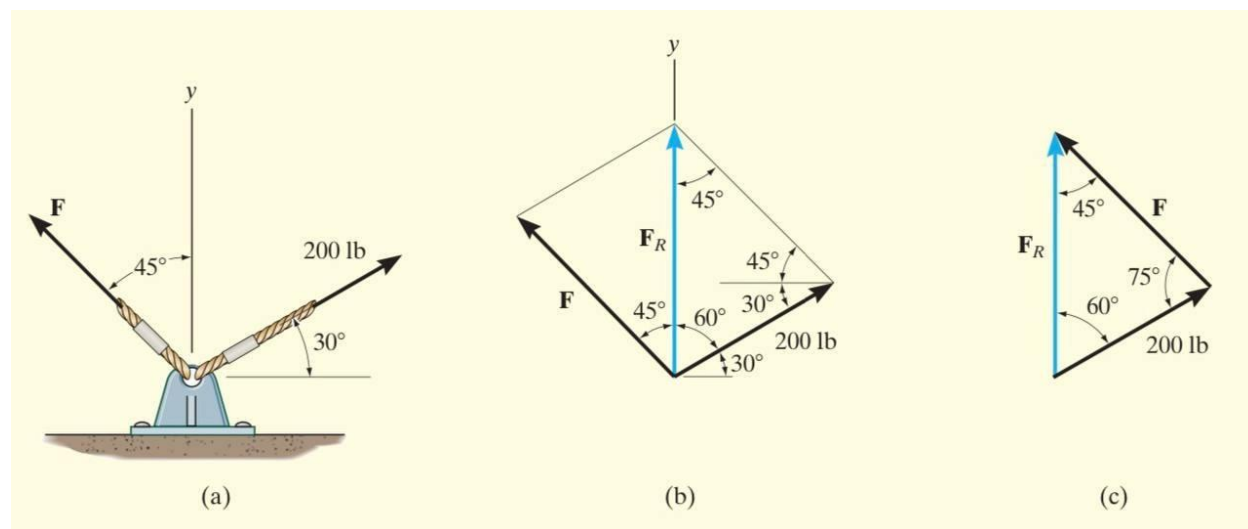
$$\frac{F_u}{\sin 120^\circ} = \frac{600 \text{ lb}}{\sin 30^\circ}$$
$$F_u = 1039 \text{ lb}$$

$$\frac{F_v}{\sin 30^\circ} = \frac{600 \text{ lb}}{\sin 30^\circ}$$
$$F_v = 600 \text{ lb}$$



Example 2

Determine the magnitude of the component force F in Fig and the magnitude of the resultant force F_R if F_R is directed along the positive y axis.



$$\frac{F}{\sin 60^\circ} = \frac{200\text{ lb}}{\sin 45^\circ}$$

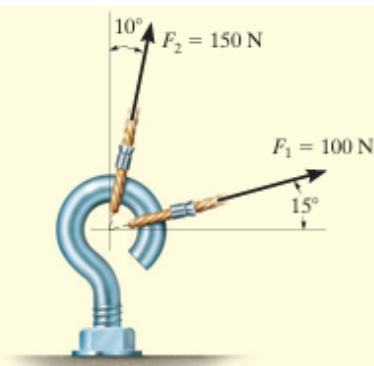
$$F = 245\text{ lb}$$

$$\frac{F_R}{\sin 75^\circ} = \frac{200\text{ lb}}{\sin 45^\circ}$$

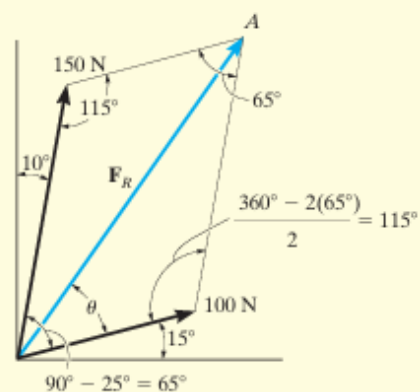
$$F_R = 273\text{ lb}$$

Example3

The screw eye in Fig. 2–11 a is subjected to two forces, F_1 and F_2 . Determine the magnitude and direction of the resultant force.



(a)



(b)

SOLUTION

Parallelogram Law. The parallelogram is formed by drawing a line from the head of F_1 that is parallel to F_2 , and another line from the head of F_2 that is parallel to F_1 . The resultant force F_R extends to where these lines intersect at point A, Fig. 2–11b. The two unknowns are the magnitude of F_R and the angle θ (theta).

Trigonometry. From the parallelogram, the vector triangle is constructed, Fig. 2–11c. Using the law of cosines

$$\begin{aligned} F_R &= \sqrt{(100 \text{ N})^2 + (150 \text{ N})^2 - 2(100 \text{ N})(150 \text{ N}) \cos 115^\circ} \\ &= \sqrt{10\,000 + 22\,500 - 30\,000(-0.4226)} = 212.6 \text{ N} \\ &= 213 \text{ N} \end{aligned}$$

Ans.

Applying the law of sines to determine θ ,

$$\begin{aligned} \frac{150 \text{ N}}{\sin \theta} &= \frac{212.6 \text{ N}}{\sin 115^\circ} & \sin \theta &= \frac{150 \text{ N}}{212.6 \text{ N}} (\sin 115^\circ) \\ \theta &= 39.8^\circ \end{aligned}$$

Thus, the direction ϕ (phi) of F_R , measured from the horizontal, is

$$\phi = 39.8^\circ + 15.0^\circ = 54.8^\circ$$

Ans.

NOTE: The results seem reasonable, since Fig. 2–11b shows F_R to have a magnitude larger than its components and a direction that is between them.



Fig. 2–11