



Series-Parallel DC Circuits

Objective

This exercise will involve the analysis of basic series-parallel DC circuits with resistors. The use of simple series-only and parallel-only sub-circuits is examined as one technique to solve for desired currents and voltages.

Theory Overview

Simple series-parallel networks may be viewed as interconnected series and parallel sub-networks. Each of these sub-networks may be analyzed through basic series and parallel techniques such as the application of voltage divider and current divider rules along with Kirchhoff's voltage and current laws. It is important to identify the most simple series and parallel connections in order to jump to more complex interconnections.

Equipment

- | | |
|--------------------------------|-------------------------|
| (1) Adjustable DC power supply | model: _____ srn: _____ |
| (1) Digital multimeter | model: _____ srn: _____ |
| (1) 1 k Ω | _____ |
| (1) 2.2 k Ω | _____ |
| (1) 3.3 k Ω | _____ |
| (1) 4.7 k Ω | _____ |
| (1) 6.8 k Ω | _____ |

Schematics

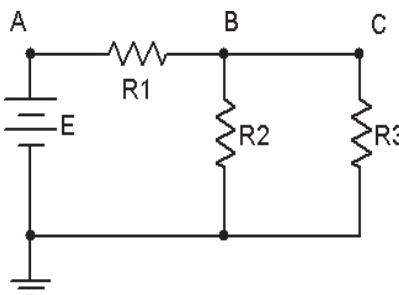


Figure 7.1

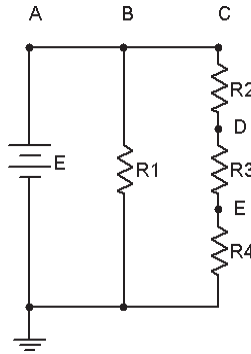


Figure 7.2

Procedure

1. Consider the circuit of Figure 7.1 with $R1 = 1\text{ k}$, $R2 = 2.2\text{ k}$, $R3 = 4.7\text{ k}$ and $E = 10\text{ volts}$. $R2$ is in parallel with $R3$. This combination is in series with $R1$. Therefore, the $R2, R3$ pair may be treated as a single resistance to form a series loop with $R1$. Based on this observation, determine the theoretical voltages at points A, B, and C with respect to ground. Record these values in Table 7.1. Construct the circuit. Set the DMM to read DC voltage and apply it to the circuit from point A to ground. Record this voltage in Table 7.1. Repeat the measurements at points B and C, determine the deviations, and record the values in Table 7.1.
2. Applying KCL to the parallel sub-network, the current entering node B (i.e., the current through $R1$) should equal the sum of the currents flowing through $R2$ and $R3$. These currents may be determined through Ohm's law and/or the current divider rule. Compute these currents and record them in Table 7.2. Using the DMM as an ammeter, measure these three currents and record the values along with deviations in Table 7.2.
3. Consider the circuit of Figure 7.2. $R2, R3$ and $R4$ create a series sub-network. This sub-network is in parallel with $R1$. By observation then, the voltages at nodes A, B and C should be identical as in any parallel circuit of similar construction. Due to the series connection, the same current flows through $R2, R3$ and $R4$. Further, the voltages across $R2, R3$ and $R4$ should sum up to the voltage at node C, as in any similarly constructed series network. Finally, via KCL, the current exiting the source must equal the sum of the currents entering $R1$ and $R2$.
4. Build the circuit of Figure 7.2 with $R1 = 3.3\text{ k}$, $R2 = 2.2\text{ k}$, $R3 = 4.7\text{ k}$, $R4 = 6.8\text{ k}$ and $E = 20\text{ volts}$. Using the series and parallel relations noted in Step 3, calculate the voltages at points B, C, D and E. Measure these potentials with the DMM, determine the deviations, and record the values in Table 7.3.



5. Calculate the currents leaving the source and flowing through R1 and R2. Record these values in Table 7.4. Using the DMM as an ammeter, measure those same currents, compute the deviations, and record the results in Table 7.4.

Simulation

6. Build the circuit of Figure 7.1 in a simulator. Using the virtual DMM as a voltmeter determine the voltages at nodes A, B and C, and compare these to the theoretical and measured values recorded in Table 7.1.
7. Build the circuit of Figure 7.2 in a simulator. Using the DC Operating Point simulation function, determine the voltages at nodes B, C, D and E, and compare these to the theoretical and measured values recorded in Table 7.3.

Data Tables

Voltage	Theory	Measured	Deviation
V_A			
V_B			
V_C			

Table 7.1

Current	Theory	Measured	Deviation
R_1			
R_2			
R_3			

Table 7.2



Voltage	Theory	Measured	Deviation
V_B			
V_C			
V_D			
V_E			

Table 7.3

Current	Theory	Measured	Deviation
Source			
R1			
R2			

Table 7.4



Questions

1. Are KVL and KCL satisfied in Tables 7.1 and 7.2?
2. Are KVL and KCL satisfied in Tables 7.3 and 7.4?
3. How would the voltages at A and B in Figure 7.1 change if a fourth resistor equal to 10 k was added in parallel with R3? What if this resistor was added in series with R3?
4. How would the currents through R1 and R2 in Figure 7.2 change if a fifth resistor equal to 10 k was added in series with R1? What if this resistor was added in parallel with R1?