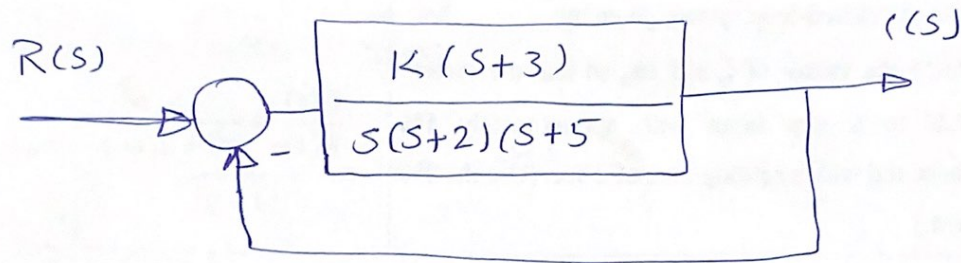


Q2/ Plot the root loci For the closed loop Control System with



1 poles and Zeros

From open loop $G(s)H(s) = 0$

$$\frac{K(s+3)}{s(s+2)(s+5)} = 0$$

* poles/

$$\left. \begin{array}{l} s=0 \\ s=-2 \\ s=-5 \end{array} \right\} \text{No. of poles} = 3$$

* Zeros

$$s = -3 \quad \left. \right\} \text{No. of zeros} = 1$$

2 No. of Asymptotes

$$= \text{No. of poles} - \text{No. of zeros}$$

$$= 3 - 1 = 2$$

3] Angle of Asymptotes

$$\theta = \frac{(2x+1) \times 180}{\text{No. of poles} - \text{No. of zeros}} \quad ; \quad x = 0, 1$$

$$\theta_1 = \frac{2(0)+1}{3-1} \times 180^\circ = 90^\circ$$

$$\theta_2 = \frac{2(1)+1}{3-1} \times 180^\circ = 270^\circ$$

4] Centroid of Asymptotics

$$= \frac{\sum \text{real part. of poles} - \sum \text{real part of zeros}}{\text{No. of poles} - \text{No. of zeros}}$$

$$= \frac{(-2-5) - (-3)}{3-1}$$

$$= \frac{-4}{2} = -2$$

5 Break away point

From characteristic eq.

$$1 + G(s)H(s) = 0$$

$$1 + \frac{K(s+3)}{s(s+2)(s+5)} = 0$$

$$\frac{s(s+2)(s+5) + K(s+3)}{s(s+2)(s+5)} = 0$$

$$(s^2 + 2s)(s+5) + K(s+3) = 0$$

$$s^3 + 5s^2 + 2s^2 + 10s + K(s+3) = 0$$

$$K = - \frac{s^3 + 7s^2 + 10s}{s+3}$$

$$\frac{dK}{ds} = - \frac{(s+3)(2s^2 + 14s + 10) - (s^3 + 7s^2 + 10s)(1)}{(s+3)^2} = 0$$

$$0 = 3s^3 + 14s^2 + 10s + 9s^2 + 42s + 30 - s^3 - 7s^2 - 10s$$

$$0 = 2s^3 + 16s^2 + 42s + 30$$

$$s = -1.136 \rightarrow \text{break away point.}$$

$$\left. \begin{array}{l} s = -3.4 + 1.191i \\ s = -3.4 - 1.191i \end{array} \right\} \rightarrow \text{No break away point} \\ \text{because complex conjugate}$$

6] Intersection with imaginary

There is no intersection with imaginary because of angles of asymptotes don't cross the imaginary axis. i.e $\theta_1 = 90^\circ$; $\theta_2 = 270^\circ$

7] Angle of departure

There is no. angle of departure, because there is no complex conjugate poles.

