

Al-Mustaqbal University

Department of Power Mechanical Techniques Engineering

(Refrigeration and Air Conditioning)

Class one - first semester



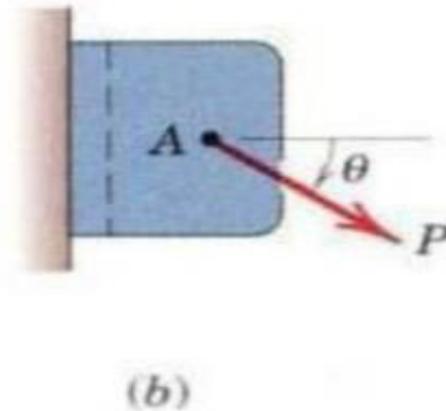
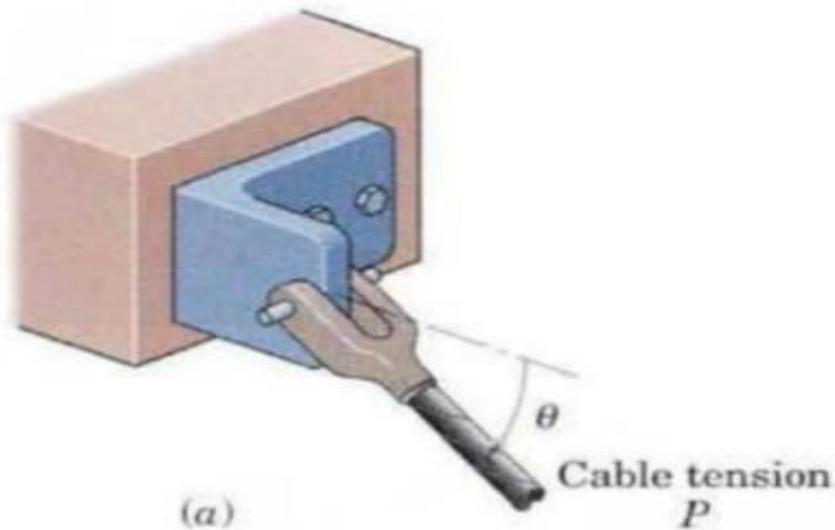
Engineering Mechanical

Lecture3: Force System

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Force System

Before dealing with a group or system of forces, it is necessary to examine the properties of a single force in some detail. The action of the cable tension on the bracket in Fig. 1a is represented in the side view, Fig. 1b, by the force vector P of magnitude P . The effect of this action on the bracket depends on P , the angle θ , and the location of the point of application A



Force System

Coplanar (in plane)

Non-Coplanar (in space)

Concurrent

Parallel

Non-Concurrent
Non-Parallel

Concurrent

Parallel

Non-Concurrent
Non-Parallel

Concurrent

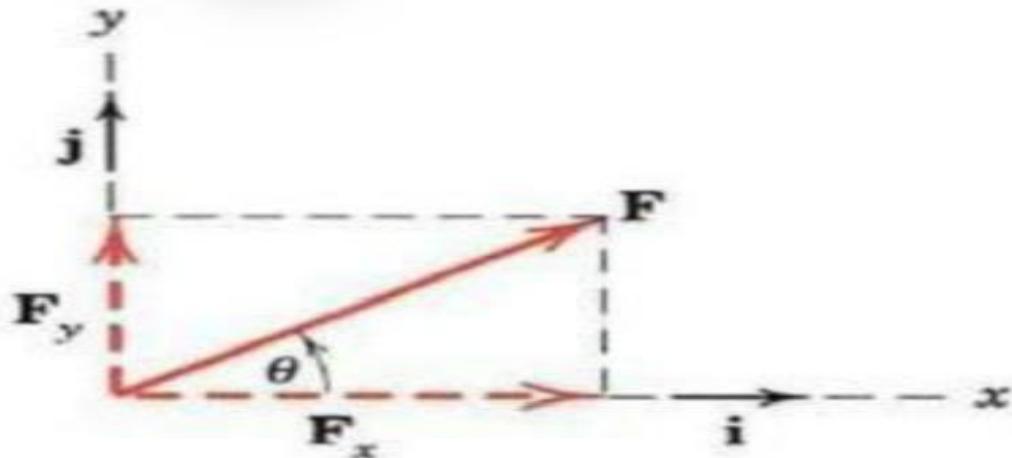
Parallel

Concurrent

Non-Concurrent
Non-Parallel

TWO-DIMENSIONAL FORCE SYSTEMS

- ▶ RECTANGULAR COMPONENTS
- ▶ The most common two-dimensional resolution of a force vector is into rectangular
- ▶ components. It follows from the parallelogram rule that the vector F of Fig. may be
- ▶ written as



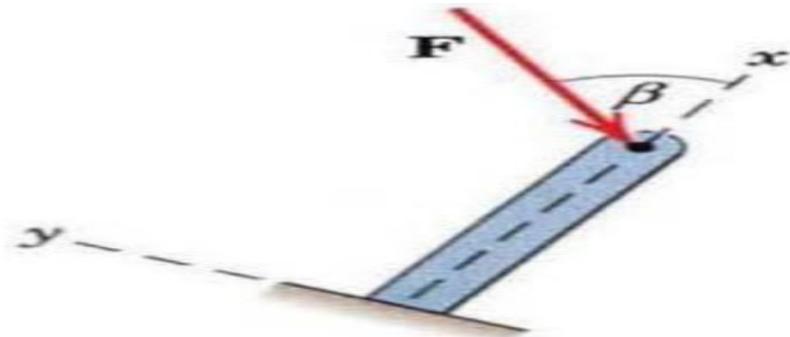
Force System

- ▶ The scalar components can be positive or negative, depending on the quadrant into which F points.

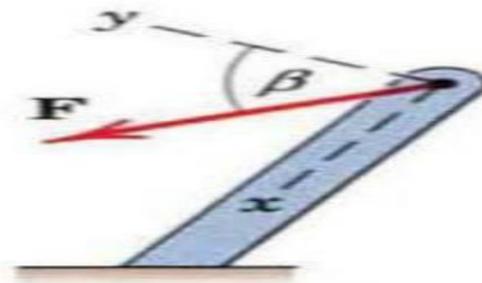
$$\begin{aligned} F_x &= F \cos \theta & F &= \sqrt{F_x^2 + F_y^2} \\ F_y &= F \sin \theta & \theta &= \tan^{-1} \frac{F_y}{F_x} \end{aligned}$$

- ▶ Determining the Components of a Force Dimensions are not always given in horizontal and vertical directions, angles need not be measured counterclockwise from the x-axis, and the origin of coordinates need not be on the line of action of a force

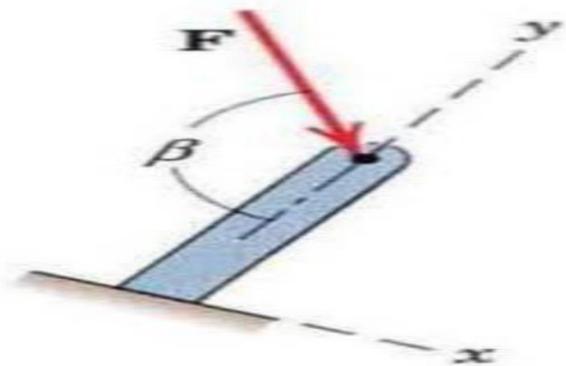
Force System



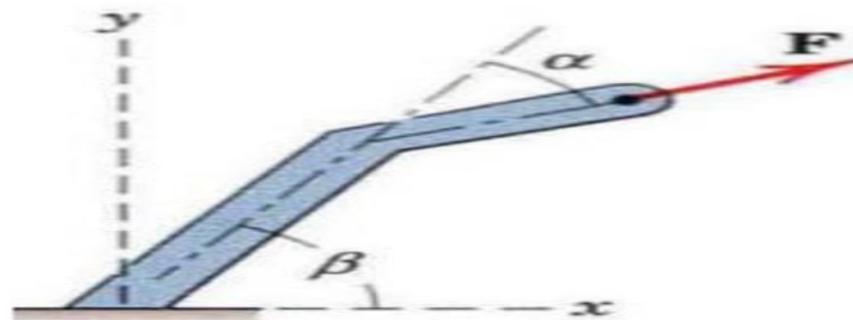
$$F_x = -F \cos \beta$$
$$F_y = -F \sin \beta$$



$$F_x = F \sin \beta$$
$$F_y = F \cos \beta$$



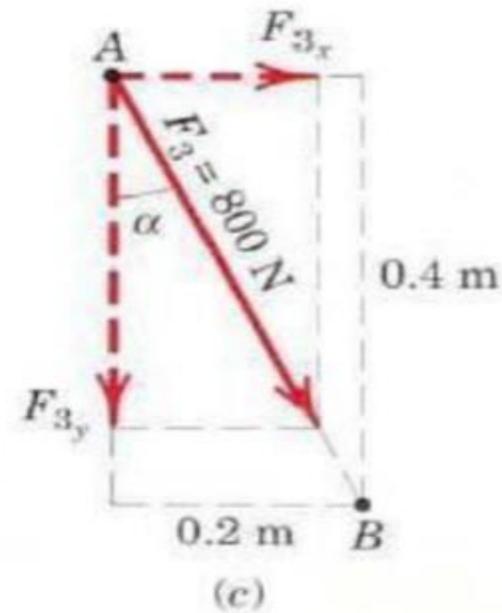
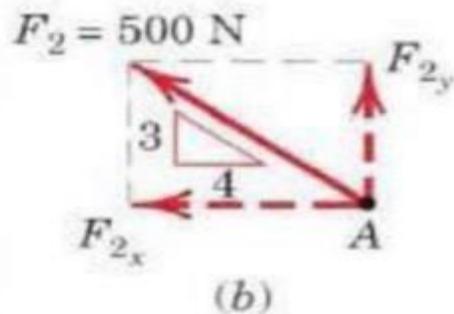
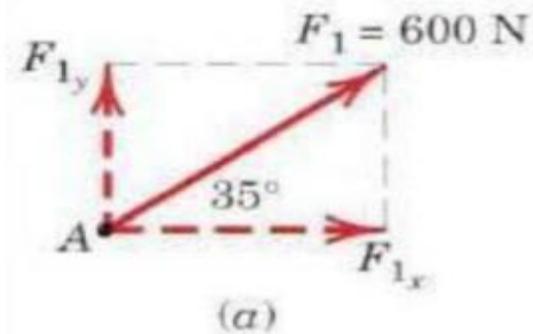
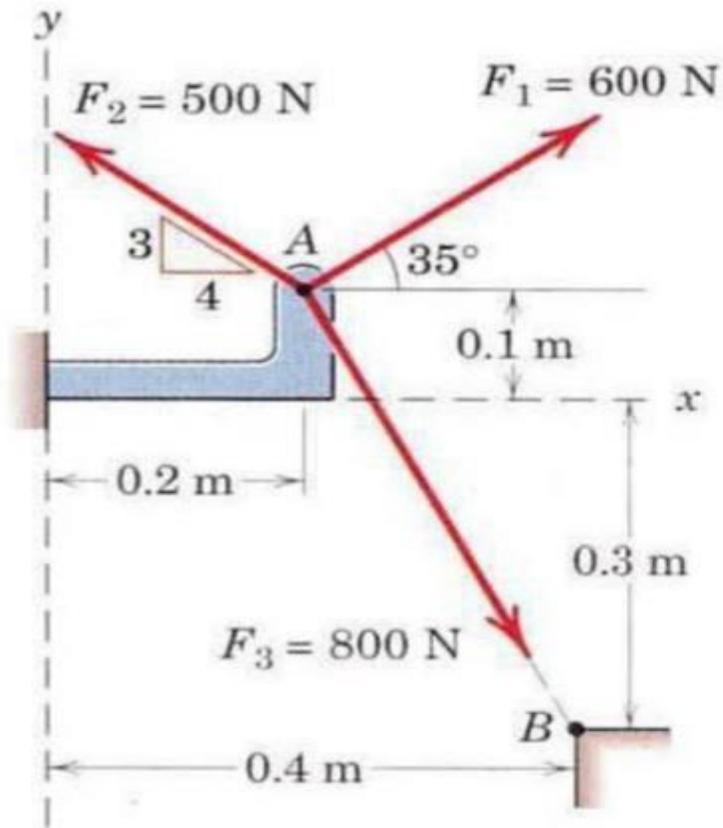
$$F_x = F \sin(\pi - \beta)$$
$$F_y = -F \cos(\pi - \beta)$$



$$F_x = F \cos(\beta - \alpha)$$
$$F_y = F \sin(\beta - \alpha)$$

Problem 1

- ▶ The forces F_1 , F_2 , and F_3 all of which act on point A of the bracket, are specified in three different ways. Determine the x and y scalar components of each of the three forces.

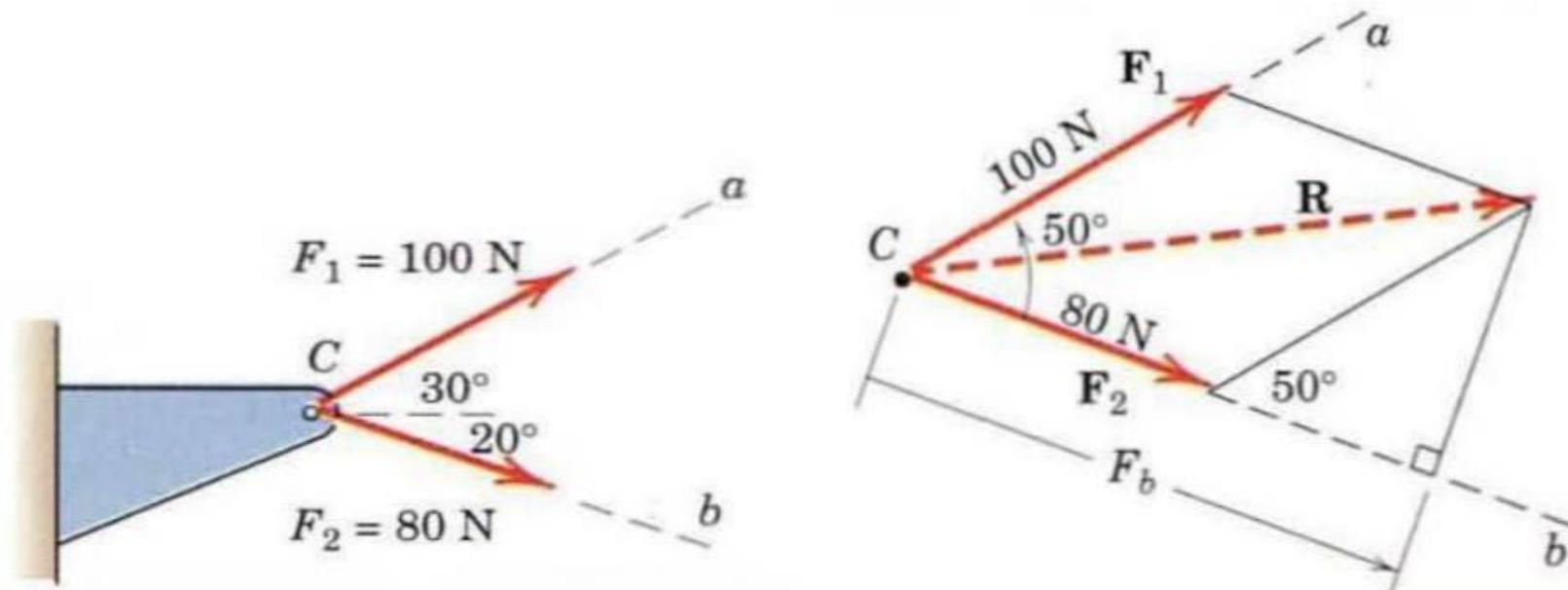


Solution

- ▶ Solution: The scalar components of F_1 from Fig. a, are $F_{1x} = 600 \cos 35^\circ = 491 \text{ N}$
- ▶ $F_{1y} = 600 \sin 35^\circ = 344 \text{ N}$
- ▶ The scalar components of F_2 from Fig. b, are
- ▶ $F_{2x} = -500(4/5) = -400 \text{ N}$
- ▶ $F_{2y} = 500(3/5) = 300 \text{ N}$
- ▶ $\theta = \tan^{-1} [0.2/0.4] = 26.6^\circ$
- ▶ Then $F_{3x} = F_3 \sin \theta = 800 \sin 26.6^\circ = 358 \text{ N}$ $F_{3y} = -F_3 \cos \theta = -800 \cos 26.6^\circ = -716 \text{ N}$

Problem 2

- ▶ Forces F_1 and F_2 act on the bracket as shown Determine the projection F_b
- ▶ of their resultant R onto the b -axis.

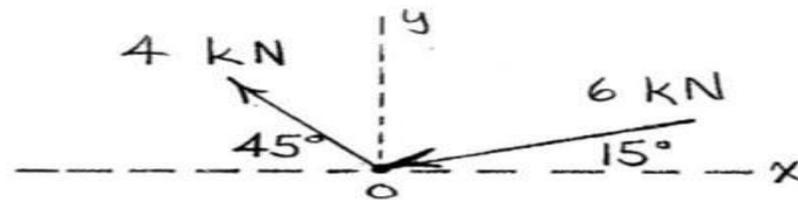
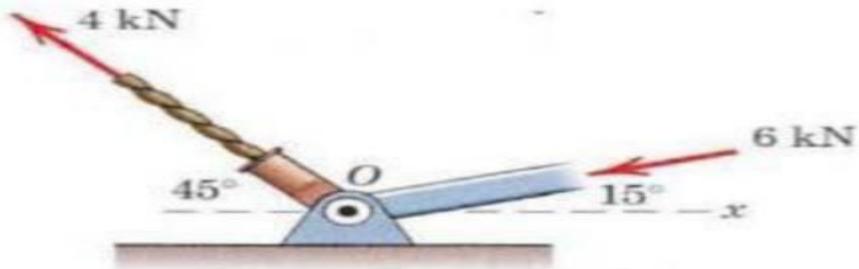


Solution.

- ▶ Solution. The parallelogram addition of F_1 and F_2 is shown in the figure.
- ▶ Using the law of cosines gives us $R^2 = (80)^2 + (100)^2 - 2(80)(100) \cos$
- ▶ 130
- ▶ $R = 163.4 \text{ N}$
- ▶ The figure also shows the orthogonal projection F_b of R onto the b -axis.
- ▶ Its length is
- ▶ $F_b = 80 + 100 \cos 50 = 144.3 \text{ N}$

Problem 3

- ▶ The two structural members, one of which is in tension and the other in compression, exert the indicated forces on joint O. Determine the magnitude of the resultant R of the two forces and the angle θ which R makes with the positive x-axis.



$$R_x = \sum F_x = -4 \cos 45^\circ - 6 \cos 15^\circ = -8.62 \text{ kN}$$

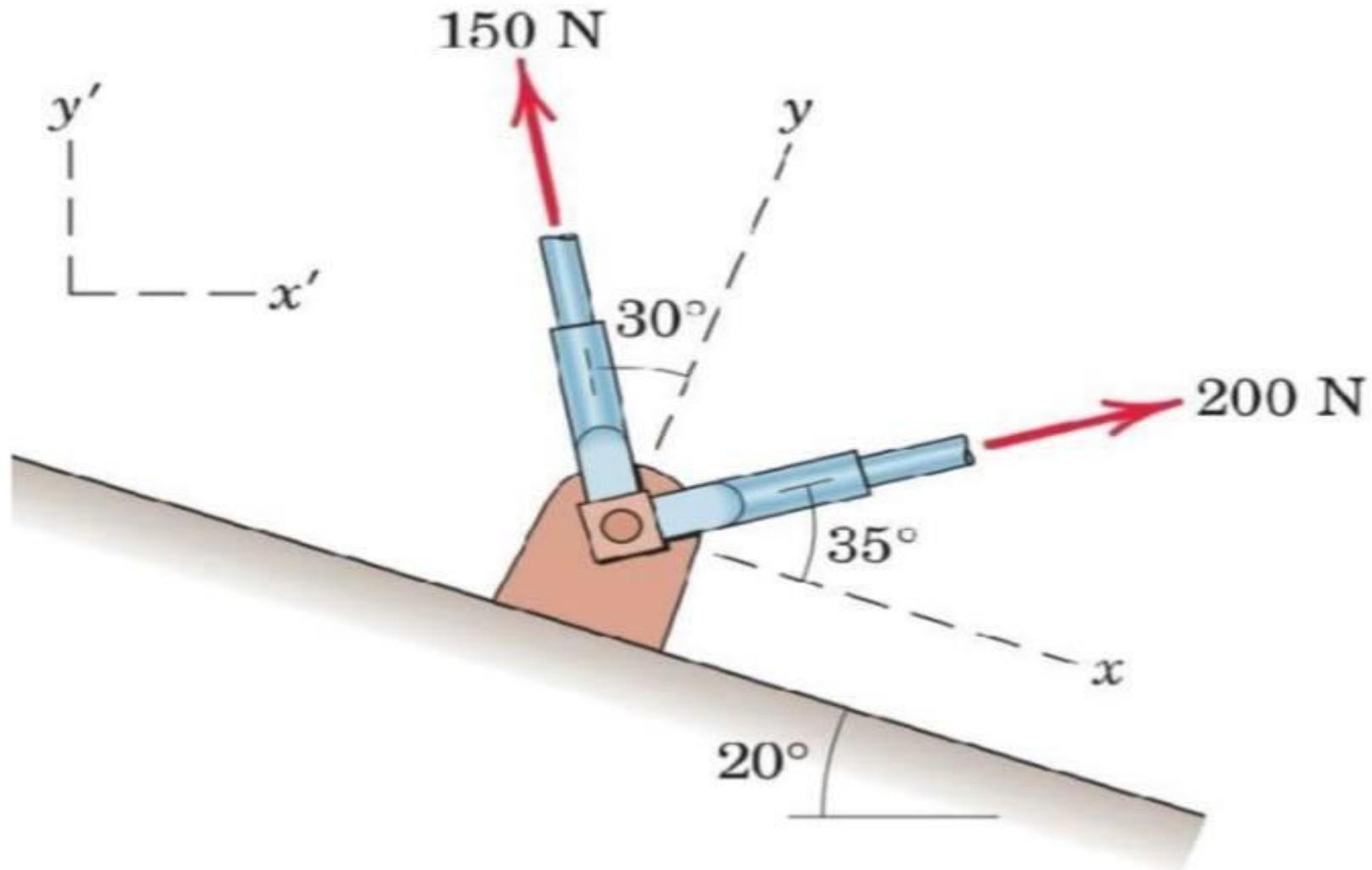
$$R_y = \sum F_y = 4 \sin 45^\circ - 6 \sin 15^\circ = 1.276 \text{ kN}$$

$$R = \sqrt{R_x^2 + R_y^2} = \underline{8.72 \text{ kN}}$$

$$\theta = \tan^{-1} \left(\frac{R_y}{R_x} \right) = \tan^{-1} \left(\frac{1.276}{-8.62} \right) = \underline{171.6^\circ}$$

H.W

- ▶ Determine the resultant R of the two forces applied to the bracket





***Thank you
for listening***

