



Al-Mustaqbal University / College of Engineering

Prosthetics & Orthotics Eng. Department

First Class

Subject (Physics)

Code (UOMU013015)

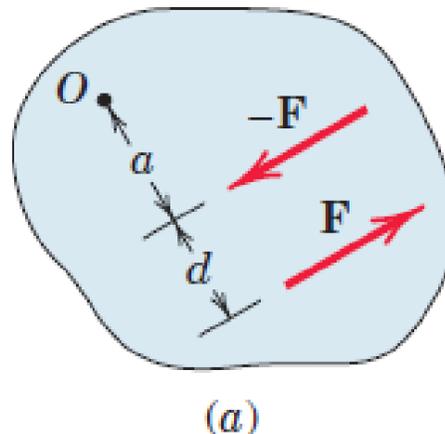
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1st term – Lecture 5



The couple

- The moment produced by two equal, opposite, and noncollinear forces is called a **couple**.
- Consider the action of two equal and opposite forces \mathbf{F} and $-\mathbf{F}$ a distance d apart, as shown in Fig *a*.
- These two forces cannot be **combined** into a single force because their sum in every direction is **zero**.



- Their only effect is to produce a tendency of rotation.
- The combined moment of the two forces about an axis normal to their plane and passing through point O is the couple M.



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$$M = F(a + d) - Fa$$

Or

$$M = Fd$$

Vector algebra method

■ The combined moment about point O of the forces forming the couple of Fig b is:

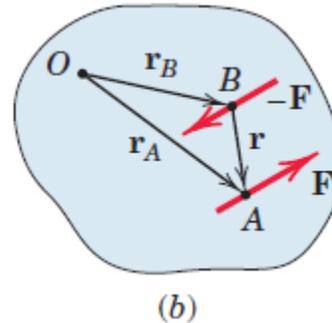
$$\mathbf{M} = \mathbf{r}_A \times \mathbf{F} + \mathbf{r}_B \times (-\mathbf{F})$$

$$= (\mathbf{r}_A - \mathbf{r}_B) \times \mathbf{F}$$

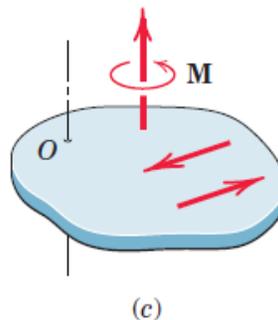
Because

$$\mathbf{r}_A - \mathbf{r}_B = \mathbf{r}$$

$$\mathbf{M} = \mathbf{r} \times \mathbf{F}$$

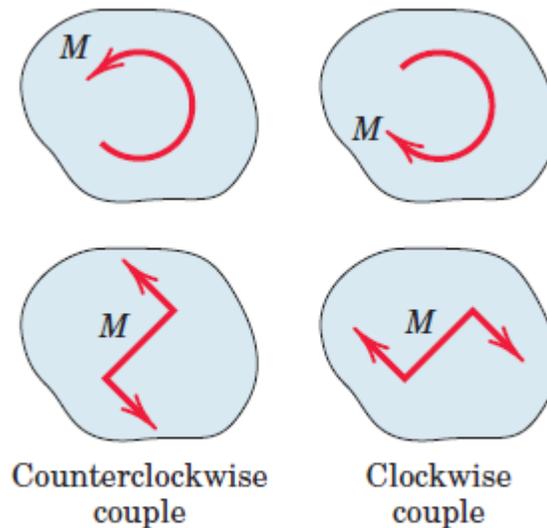


- we may represent \mathbf{M} by a free vector, as show in Fig c , where the direction of \mathbf{M} is normal to the plane of the couple and the sense of \mathbf{M} is established by the right-hand rule





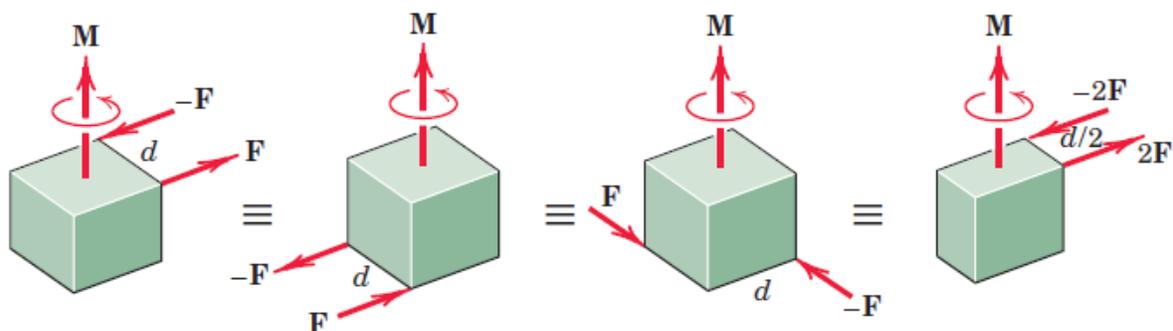
- The sense of a couple vector as clockwise or counterclockwise by one of the conventions shown in Fig *d*.



(d)

Equivalent couples

- The figure below shows four different configurations of the same couple M .





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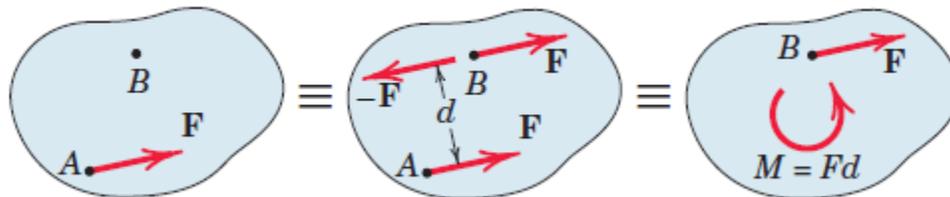
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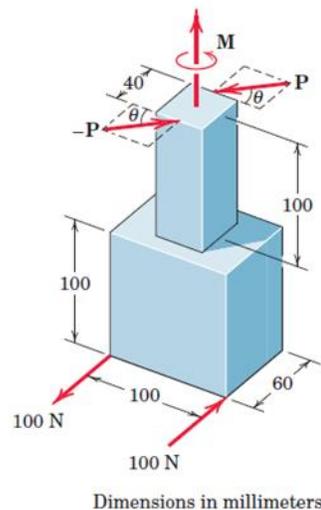
Force-couple system

■ We can represent the effect of a force more easily by replacing the given force by an equal parallel force and a couple to compensate for the change in the moment of the force.



Sample Problem 2/7

The rigid structural member is subjected to a couple consisting of the two 100-N forces. Replace this couple by an equivalent couple consisting of the two forces P and $-P$, each of which has a magnitude of 400 N. Determine the proper angle θ .





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Solution. The original couple is counterclockwise when the plane of the forces is viewed from above, and its magnitude is

$$[M = Fd]$$

$$M = 100(0.1) = 10 \text{ N}\cdot\text{m}$$

The forces \mathbf{P} and $-\mathbf{P}$ produce a counterclockwise couple

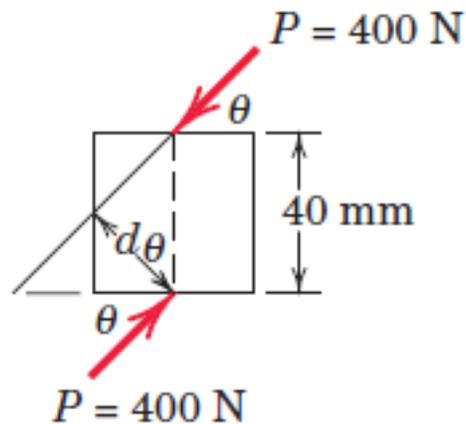
$$M = 400(0.040) \cos \theta$$

① Equating the two expressions gives

$$10 = (400)(0.040) \cos \theta$$

$$\theta = \cos^{-1} \frac{10}{16} = 51.3^\circ$$

Ans.





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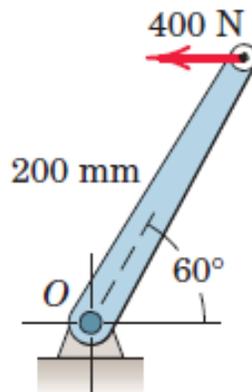
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Sample Problem 2/8

Replace the horizontal 400-N force acting on the lever by an equivalent system consisting of a force at O and a couple.



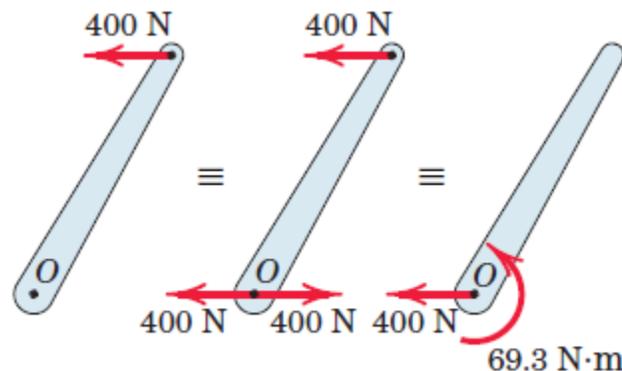
Solution. We apply two equal and opposite 400-N forces at O and identify the counterclockwise couple

$$[M = Fd]$$

$$M = 400(0.200 \sin 60^\circ) = 69.3 \text{ N}\cdot\text{m}$$

Ans.

- ① Thus, the original force is equivalent to the 400-N force at O and the 69.3-N·m couple as shown in the third of the three equivalent figures.





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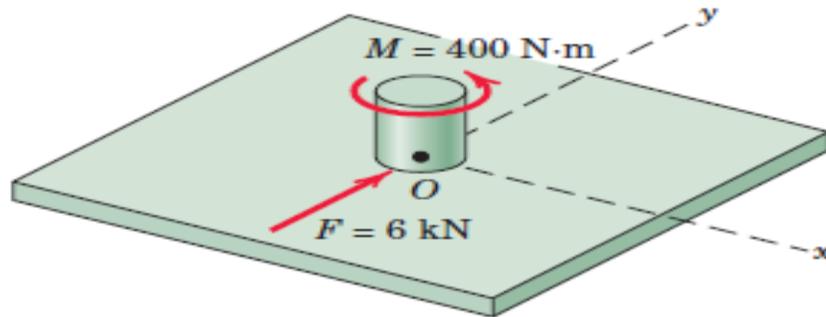
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2/60 The indicated force–couple system is applied to a small shaft at the center of the plate. Replace this system by a single force and specify the coordinate of the point on the x -axis through which the line of action of this resultant force passes.



Problem 2/60

2/60

$$R = 6 \text{ j kN}$$

$$x = \frac{400}{6000} = 0.0667 \text{ m}$$

$$x = 66.7 \text{ mm}$$



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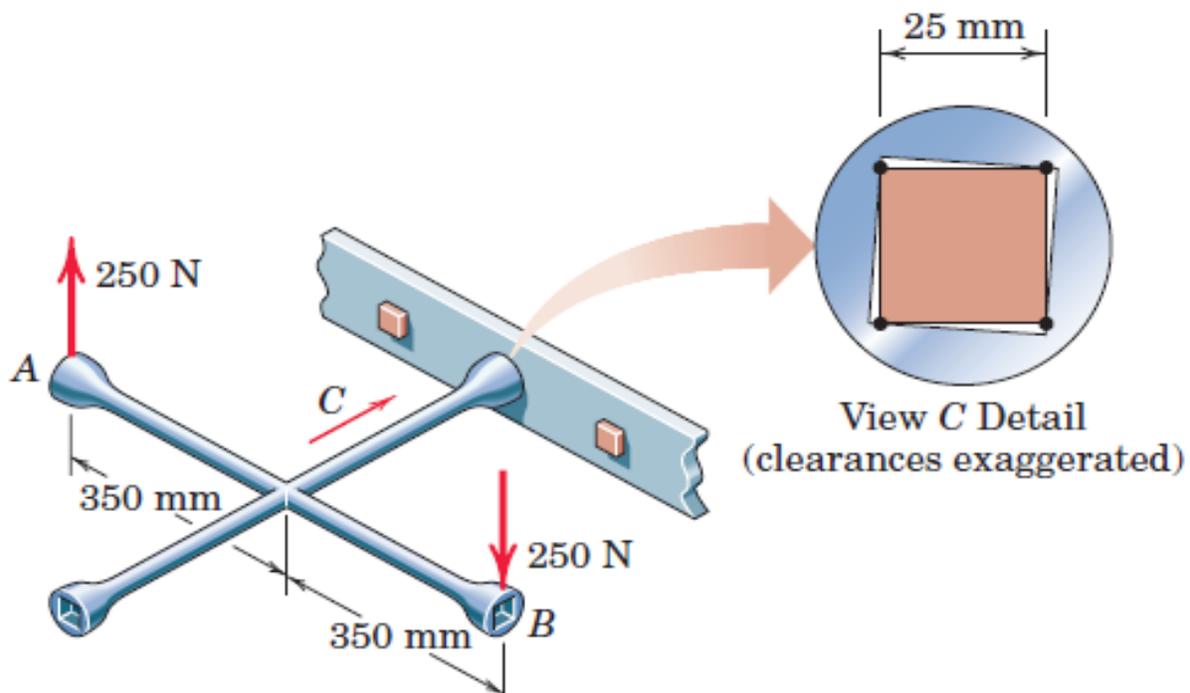
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2/65 A lug wrench is used to tighten a square-head bolt. If 250-N forces are applied to the wrench as shown, determine the magnitude F of the equal forces exerted on the four contact points on the 25-mm bolt head so that their external effect on the bolt is equivalent to that of the two 250-N forces. Assume that the forces are perpendicular to the flats of the bolt head.

Ans. $F = 3500$ N



Problem 2/65



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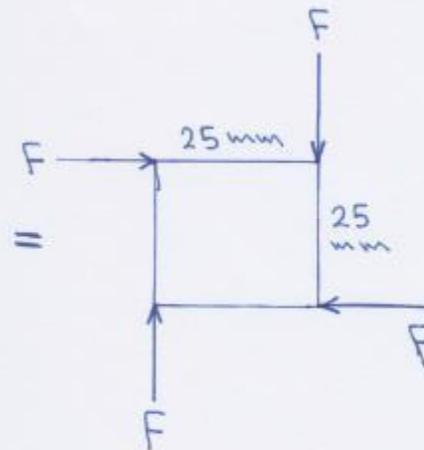
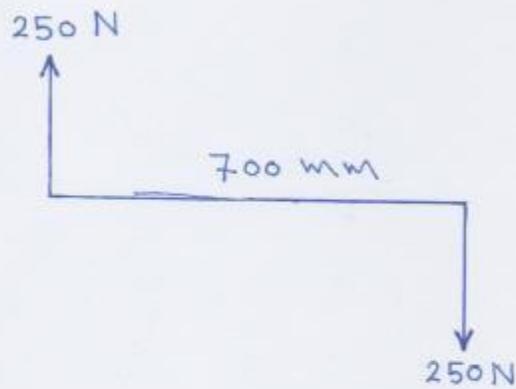
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2 / 65



$$M = 250 (0.7) = 2 F (0.25)$$

$$F = 350 \text{ N}$$



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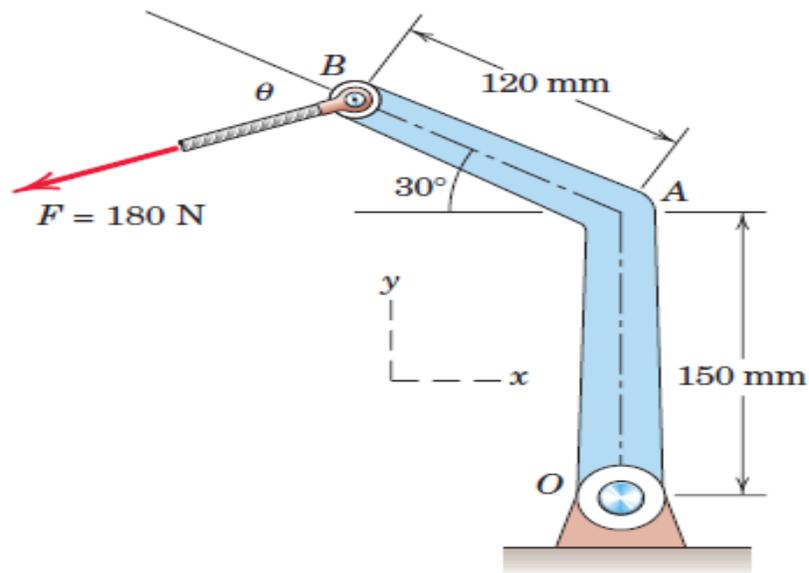
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2/67 The 180-N force is applied to the end of body OAB . If $\theta = 50^\circ$, determine the equivalent force-couple system at the shaft axis O .

Ans. $\mathbf{F} = -169.1\mathbf{i} - 61.6\mathbf{j}$ N, $M_O = 41.9$ N·m CCW



Problem 2/67



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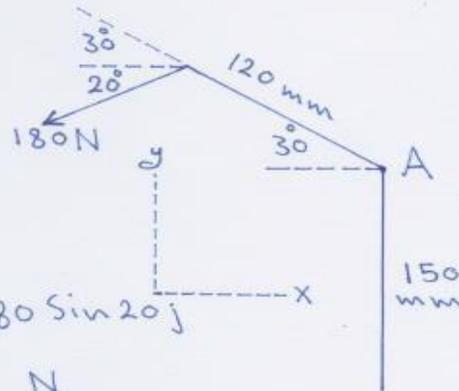
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2/67



$$F = F_x i + F_y j$$

$$= -180 \cos 20^\circ i - 180 \sin 20^\circ j$$

$$= -169.1 i - 61.6 N$$

$$\curvearrowright M_o = F_x (150 + 120 \sin 30^\circ) + F_y (120 \cos 30^\circ)$$

$$= 169.1(150 + 120 \sin 30^\circ) + 61.6(120 \cos 30^\circ)$$

$$= 41900 \text{ N}\cdot\text{mm} \quad \text{or} \quad 41.9 \text{ N}\cdot\text{m} \text{ CCW}$$